

# ***Fiber-Reinforced Polymer Reinforcement for Concrete Structures***



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## **ACI Design Guide for Flexural and Shear Strengthening of URM Walls with FRP Systems**

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**Synopsis:** The American Concrete Institute (ACI) Committee 440 has recently published a design guide for strengthening of masonry with FRP systems. This paper summarizes and provides comments on the design protocols recommended by ACI 440 for flexural and shear strengthening with FRP systems of unreinforced masonry wall (URM). The development of the design protocols were based on calibration of bond reduction factors derived by a database of test results. This paper presents the rationale behind this approach, the calibration procedure, and its implementation in design protocols for flexural and shear strengthening of URM walls.

**Keywords:** Design, Fiber Reinforced Polymer (FRP), Flexure, Shear, Strengthening, Unreinforced Masonry

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## INTRODUCTION

Unreinforced masonry (URM) structures are prone to extensive damage followed by failure and collapse when subjected to loads resulting from wind, earthquake and other natural or man-made events. Recent earthquakes have clearly demonstrated that the development of effective strategies for the strengthening of masonry is an urgent need. As a response to these challenges, fiber reinforced polymer (FRP) composites may offer technically and economically viable solutions.

The increasing need of FRP materials for the strengthening and upgrade of masonry has motivated the engineering community to produce guides for the proper design, handling and installation of the externally bonded FRP systems. In 2010, the American Concrete Institute (ACI) Committee 440 published "Guide for the Design and Construction of Externally Bonded FRP Systems for Unreinforced Masonry Structures" (ACI 440.7R-10).

## **RESEARCH SIGNIFICANCE**

The development of the design protocols included in ACI 440.7R-10 were, in part, based on calibration of bond reduction factors derived by a database of test results found in the literature. This paper describes the rationale behind this approach, the calibration procedure, and its implementation in design protocols for flexural and shear strengthening of URM walls.

## **BACKGROUND**

### **FRP Flexural Strengthening**

The structural performance of URM walls subject to out-of-plane loading is highly dependent on the tensile strength of masonry and magnitude of the in-plane (axial) compressive forces acting on the wall. URM walls can span in one or two directions depending on the boundary conditions. When subject to out-of-plane loads, initial cracks form at or near the ends of the walls. These cracks are typically located at the base of the wall. After the initial cracking occurs, the wall behaves as a simply-supported element until further cracks develop about mid-height. These cracks typically extend along the mortar bed joints and lead to failure of the wall.

FRP systems can significantly increase the flexural strength of URM walls. Because of the reversed stresses caused by out-of-plane loads due to high wind pressures (windward and leeward) and earthquake excitations, FRP flexural strengthening of URM walls require installation of FRP systems on both wall faces.

FRP composite systems are very effective for strengthening of URM walls that can behave as simply- supported elements, or very nearly so, such as the case of slender walls. FRP composites can also be effective for strengthening of “stocky” walls provided that these are not built between rigid supports (reinforced concrete or steel beams), or that floor or roof structure framing into the wall create a simply-supported boundary conditions (e.g. floor framing consisting of metal deck supported by open-web joists).

Walls with low  $h/t$  ratios, typically less than 12, and built between rigid supports can develop arching action. Basically, as a stocky wall bends due to the out-of-plane loads, the wall is restrained from rotation at the supports. This action induces an in-plane compressive force, which depending on the stiffness of the supports can significantly increase the wall resistance to out-of-plane loads. Walls able to develop arching do not typically require to be strengthened, and therefore are not addressed by ACI 440.7R-10.

### **FRP Shear Strengthening**

The structural behavior of URM walls subject to in-plane loads depends on several parameters including geometry such as dimensions and thickness, construction type such as bond pattern, and type and strength of masonry units and mortar; axial

loading, and boundary conditions. Walls under in-plane loads can have the following four modes of failure: diagonal tension, bed-joint sliding, toe crushing and rocking. The first three modes of failure are force-controlled failures, whereas rocking is a deformation-controlled failure. Deformation-controlled failures are more ductile than force-controlled failures. A URM wall failing due to rocking (deformation-controlled failure) has the ability to absorb more energy after initial cracking than URM walls failing due to force-controlled failures. Thus, any approach for strengthening of URM walls should be aimed at precluding the occurrence of force-controlled failures, or in its defect it should provide ductility to the wall so this is able to significantly before failure.

FRP composite systems are effective to increase the shear strength of URM walls by preventing or delaying the occurrence of bed-joint sliding failure, if the cracks are oriented along the wall diagonal (i.e. stepped cracking), and diagonal tension failure. FRP composites can also provide pseudo-ductility to URM walls.

There is limited research on infill walls (walls built within reinforced concrete or steel frames) strengthened with FRP; and therefore, strengthening of infill walls is not covered by ACI 440.7R-10. In general the in-plane behavior of infill walls is dependent of the relative stiffness ratio between the masonry and the surrounding frame, aspect ratio of the wall, and occurrence of premature failures such as crushing of corners in contact with the frame.

#### **EFFECTIVE STRAIN IN THE FRP REINFORCEMENT AT ULTIMATE**

FRP debonding from the masonry substrate is the most common mode of failure in a URM wall strengthened with FRP systems. Thus, for design purposes, rather than attempting to predict the bond failure, the strain in the FRP laminates can be limited to prevent failure. Since the contribution of FRP to the flexural and shear capacities of the FRP-strengthened is dependant of the strain developed in the FRP, it is reasonable to express the effective strain in the FRP laminate or bar,  $\epsilon_{fe}$ , as the product  $\kappa_m \epsilon_{fu}$  for flexural strengthening and  $\kappa_v \epsilon_{fu}$  for shear strengthening, where  $\kappa_m$  and  $\kappa_v$  are bond-dependent coefficients for flexure and shear, respectively, and  $\epsilon_{fu}$  is the design rupture strain of FRP.

The methodology to arrive to a set of efficiency coefficients involved collecting test data available in the literature, analyze trends and calibrate appropriate  $\kappa_m$  and  $\kappa_v$  values (Tables 1 through 4). The data base included masonry specimens built with concrete masonry units (CMU), concrete bricks, clay bricks, and strengthened with carbon FRP (CFRP), glass FRP (GFRP) and aramid FRP (AFRP) in the form of externally-bonded laminates or near-surface-mounted (NSM) bars.

Table 1 -- Database for calibration of  $\kappa_m$  – FRP Laminates  
(1 in.=25.4 mm, 1 in<sup>2</sup>= 645 mm<sup>2</sup>, 1 ksi = 6.895 MPa, 1 ft-kips=1.35kN-m)

| No. | Source   | Specimen | Geometry |                        | Masonry    |                         |                        | FRP  |                        |                                      |                         |                         |                                   | Experimental Results          |                   |
|-----|----------|----------|----------|------------------------|------------|-------------------------|------------------------|------|------------------------|--------------------------------------|-------------------------|-------------------------|-----------------------------------|-------------------------------|-------------------|
|     |          |          | h/t      | b <sub>m</sub><br>(in) | Type       | f <sub>m</sub><br>(ksi) | t <sub>m</sub><br>(in) | FRP  | t <sub>r</sub><br>(in) | A <sub>f</sub><br>(in <sup>2</sup> ) | f <sub>0</sub><br>(ksi) | E <sub>r</sub><br>(ksi) | ε <sub>f<sub>u</sub></sub><br>(%) | M <sub>exp</sub><br>(ft-kips) | Failure           |
| 1   | Hamilton |          | 8.55     | 24                     | CMU        | 2.08                    | 7.75                   | GFRP | 0.014                  | 0.039                                | 220.0                   | 10500                   | 1.50                              | 2.5                           | Debonding         |
| 2   | Tumialan | COG3     | 12.3     | 24                     | CMU        | 1.5                     | 3.75                   | GFRP | 0.014                  | 0.042                                | 220.0                   | 10500                   | 2.1                               | 1.5                           | Debonding         |
| 3   | Tumialan | COG3R    | 12.3     | 24                     | CMU        | 1.5                     | 3.75                   | GFRP | 0.014                  | 0.042                                | 220.0                   | 10500                   | 2.1                               | 2.0                           | Debonding         |
| 4   | Tumialan | COG5     | 12.3     | 24                     | CMU        | 1.5                     | 3.75                   | GFRP | 0.014                  | 0.070                                | 220.0                   | 10500                   | 2.1                               | 2.5                           | Debonding         |
| 5   | Tumialan | COG7     | 12.3     | 24                     | CMU        | 1.5                     | 3.75                   | GFRP | 0.014                  | 0.098                                | 220.0                   | 10500                   | 2.1                               | 2.8                           | Shear-Debonding   |
| 6   | Tumialan | COA3     | 12.3     | 24                     | CMU        | 1.5                     | 3.75                   | AFRP | 0.011                  | 0.033                                | 290.0                   | 17000                   | 1.7                               | 1.9                           | Debonding         |
| 7   | Tumialan | COA5     | 12.3     | 24                     | CMU        | 1.5                     | 3.75                   | AFRP | 0.011                  | 0.055                                | 290.0                   | 17000                   | 1.7                               | 2.6                           | Debonding         |
| 8   | Tumialan | CLG3     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | GFRP | 0.014                  | 0.042                                | 220.0                   | 10500                   | 2.1                               | 2.4                           | Debonding         |
| 9   | Tumialan | CLG5     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | GFRP | 0.014                  | 0.070                                | 220.0                   | 10500                   | 2.1                               | 3.6                           | Debonding         |
| 10  | Tumialan | CLG7     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | GFRP | 0.014                  | 0.098                                | 220.0                   | 10500                   | 2.1                               | 4.9                           | Debonding         |
| 11  | Tumialan | CLG7R    | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | GFRP | 0.014                  | 0.098                                | 220.0                   | 10500                   | 2.1                               | 5.5                           | Shear-Debonding   |
| 12  | Tumialan | CLA3     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | AFRP | 0.011                  | 0.033                                | 290.0                   | 17000                   | 1.7                               | 2.2                           | Debonding         |
| 13  | Tumialan | CLA7     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | AFRP | 0.011                  | 0.077                                | 290.0                   | 17000                   | 1.7                               | 4.5                           | Debonding         |
| 14  | Tumialan | CLA9     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | AFRP | 0.011                  | 0.099                                | 290.0                   | 17000                   | 1.7                               | 6.2                           | Rupture           |
| 15  | Albert   | ----     | 19.2     | 48                     | CMU        | 1.06                    | 7.75                   | GFRP | 0.014                  | 0.280                                | 220.0                   | 10500                   | 2.1                               | 15.6                          | Shear-Debonding   |
| 16  | Albert   | ----     | 18.6     | 48.2                   | CMU        | 1.06                    | 7.75                   | CFRP | 0.007                  | 0.130                                | 372.0                   | 28570                   | 1.3                               | 21.8                          | Shear-Debonding   |
| 17  | Albert   | ----     | 18.6     | 48.2                   | CMU        | 1.94                    | 7.75                   | CFRP | 0.007                  | 0.130                                | 372.0                   | 28570                   | 1.3                               | 18.1                          | Shear-Debonding   |
| 18  | Albert   | ----     | 18.6     | 48.2                   | CMU        | 1.94                    | 7.75                   | CFRP | 0.007                  | 0.065                                | 372.0                   | 28570                   | 1.3                               | 9.1                           | Debonding         |
| 19  | Hamilton | ----     | 8.55     | 24                     | CMU        | 1.58                    | 7.75                   | GFRP | 0.014                  | 0.039                                | 220.0                   | 10500                   | 2.10                              | 3.1                           | Rupture           |
| 20  | Hamilton | ----     | 22.75    | 24                     | CMU        | 2.18                    | 7.75                   | GFRP | 0.014                  | 0.154                                | 220.0                   | 10500                   | 2.10                              | 11.5                          | Rupture           |
| 21  | Hamilton | ----     | 8.55     | 24                     | CMU        | 2.08                    | 7.75                   | GFRP | 0.014                  | 0.039                                | 220.0                   | 10500                   | 2.10                              | 3.6                           | Debonding-Rupture |
| 22  | Hamilton | ----     | 8.55     | 24                     | CMU        | 1.58                    | 7.75                   | GFRP | 0.014                  | 0.039                                | 220.0                   | 10500                   | 2.10                              | 4.0                           | Debonding-Rupture |
| 23  | Hamilton | ----     | 22.75    | 24                     | CMU        | 1.98                    | 7.75                   | GFRP | 0.014                  | 0.154                                | 220.0                   | 10500                   | 2.10                              | 14.3                          | Debonding-Rupture |
| 24  | Tumialan | COG5R    | 12.3     | 24                     | Concrete   | 1.5                     | 3.75                   | GFRP | 0.014                  | 0.070                                | 220.0                   | 10500                   | 2.1                               | 4.0                           | Shear-Debonding   |
| 25  | Tumialan | CLA5     | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | AFRP | 0.011                  | 0.055                                | 290.0                   | 17000                   | 1.7                               | 3.9                           | Rupture           |
| 26  | Tumialan | CLG3R    | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | GFRP | 0.014                  | 0.042                                | 220.0                   | 10500                   | 2.1                               | 2.9                           | Rupture           |
| 27  | Tumialan | CLG5R    | 12.3     | 24                     | Clay Brick | 2.5                     | 3.75                   | GFRP | 0.014                  | 0.070                                | 220.0                   | 10500                   | 2.1                               | 4.0                           | Rupture           |

Table 2 -- Database for calibration of  $\kappa_m$  – NSM FRP Bars  
(1 in.=25.4 mm, 1 in<sup>2</sup>= 645 mm<sup>2</sup>, 1 ksi = 6.895 MPa, 1 ft-kips=1.35kN-m)

| No. | Source  | Specimen     | Geometry |                        | Masonry    |                         |                        | FRP              |  |                                      |                         |                         |                                   | Experimental Results          |                 |
|-----|---------|--------------|----------|------------------------|------------|-------------------------|------------------------|------------------|--|--------------------------------------|-------------------------|-------------------------|-----------------------------------|-------------------------------|-----------------|
|     |         |              | h/t      | b <sub>m</sub><br>(in) | Type       | f <sub>m</sub><br>(ksi) | t <sub>m</sub><br>(in) | Bar              | A <sub>bar</sub><br>(in <sup>2</sup> ) | A <sub>f</sub><br>(in <sup>2</sup> ) | f <sub>0</sub><br>(ksi) | E <sub>r</sub><br>(ksi) | ε <sub>f<sub>u</sub></sub><br>(%) | M <sub>exp</sub><br>(ft-kips) | Failure Mode    |
| 1   | Gahti   | CO1-GTE1     | 8.0      | 24                     | CMU        | 1.6                     | 5.75                   | GFRP Rectangular | 0.049                                  | 0.049                                | 160.0                   | 6382                    | 2.51                              | 2.47                          | Debonding       |
| 2   | Gahti   | CO1-GTE2     | 8.0      | 24                     | CMU        | 1.6                     | 5.75                   | GFRP Rectangular | 0.049                                  | 0.097                                | 160.0                   | 6382                    | 2.51                              | 5.92                          | Debonding       |
| 3   | Gahti   | CL1-GTE1     | 12.3     | 24                     | Clay Brick | 2.3                     | 3.75                   | GFRP Rectangular | 0.049                                  | 0.049                                | 160.0                   | 6382                    | 2.51                              | 1.59                          | Debonding       |
| 4   | Gahti   | CL1-GTE2     | 12.3     | 24                     | Clay Brick | 2.8                     | 3.75                   | GFRP Rectangular | 0.049                                  | 0.097                                | 160.0                   | 6382                    | 2.51                              | 2.70                          | Debonding       |
| 5   | Gahti   | CO2-GRE21    | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.052                                | 120.0                   | 7276                    | 1.65                              | 1.86                          | Debonding       |
| 6   | Gahti   | CO2-GRE22    | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.103                                | 120.0                   | 7276                    | 1.65                              | 1.95                          | Debonding       |
| 7   | Gahti   | CO2-GRE21-SJ | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.052                                | 120.0                   | 7276                    | 1.65                              | 0.60                          | Debonding       |
| 8   | Gahti   | CO2-GRE22-SJ | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.103                                | 120.0                   | 7276                    | 1.65                              | 2.53                          | Debonding       |
| 9   | Gahti   | CO2-GRE21-S  | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.052                                | 120.0                   | 7276                    | 1.65                              | 1.41                          | Debonding       |
| 10  | Tinazzi | Block1       | 6.0      | 24                     | CMU        | 1.5                     | 7.625                  | GFRP Round       | 0.131                                  | 0.131                                | 110.0                   | 5920                    | 1.86                              | 2.38                          | Debonding       |
| 11  | Tinazzi | Block2       | 6.0      | 24                     | CMU        | 1.5                     | 7.625                  | GFRP Round       | 0.131                                  | 0.261                                | 110.0                   | 5920                    | 1.86                              | 5.24                          | Debonding       |
| 12  | Tinazzi | Brick1       | 8.8      | 5                      | Clay Brick | 2                       | 3.75                   | GFRP Round       | 0.052                                  | 0.052                                | 120.0                   | 7276                    | 1.65                              | 0.83                          | Debonding       |
| 13  | Tinazzi | Brick2       | 11.5     | 5                      | Clay Brick | 2                       | 3.75                   | GFRP Round       | 0.052                                  | 0.052                                | 120.0                   | 7276                    | 1.65                              | 1.20                          | Debonding       |
| 14  | Gahti   | CO2-GRE22-S  | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.103                                | 120.0                   | 7276                    | 1.65                              | 2.66                          | Debonding       |
| 15  | Turco   | W3-1         | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.131                                  | 0.131                                | 110.0                   | 5920                    | 1.86                              | 1.14                          | Debonding       |
| 16  | Turco   | W2-2         | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.103                                | 120.0                   | 7276                    | 1.65                              | 1.23                          | Debonding       |
| 17  | Turco   | W2-3         | 12.7     | 24                     | CMU        | 1.5                     | 3.625                  | GFRP Round       | 0.052                                  | 0.155                                | 120.0                   | 7276                    | 1.65                              | 1.66                          | Shear-Debonding |
| 18  | Bajpai  | 2 // n       | 6.0      | 15.5                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.052                                | 115.0                   | 5520                    | 1.95                              | 5.16                          | Rupture         |
| 19  | Bajpai  | 3 // w       | 6.0      | 31.4                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.155                                | 115.0                   | 5520                    | 1.95                              | 14.26                         | Rupture         |
| 20  | Bajpai  | 4 // w       | 6.0      | 31.4                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.155                                | 115.0                   | 5520                    | 1.95                              | 14.82                         | Rupture         |
| 21  | Bajpai  | 5 perp n     | 6.0      | 15.5                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.052                                | 115.0                   | 5520                    | 1.95                              | 5.69                          | Rupture         |
| 22  | Bajpai  | 6 perp n     | 6.0      | 15.5                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.052                                | 115.0                   | 5520                    | 1.95                              | 5.35                          | Rupture         |
| 23  | Bajpai  | 7 perp w     | 6.0      | 31.4                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.155                                | 115.0                   | 5520                    | 1.95                              | 14.44                         | Rupture         |
| 24  | Bajpai  | 8 perp w     | 6.0      | 31.4                   | CMU        | 2.2                     | 7.625                  | GFRP Round       | 0.052                                  | 0.155                                | 115.0                   | 5520                    | 1.95                              | 14.89                         | Rupture         |

Table 3 -- Database for calibration of  $\kappa_v$  – FRP Laminates(1 in.=25.4 mm, 1 in<sup>2</sup>= 645 mm<sup>2</sup>, 1 ksi = 6.895 MPa, 1 kip=4.448 kN)

| No. | Source        | Specimen    | MASONRY     |        |        |                     |                      | FRP  |                       |                      |                     |                                   | Experimental Results     |                |
|-----|---------------|-------------|-------------|--------|--------|---------------------|----------------------|------|-----------------------|----------------------|---------------------|-----------------------------------|--------------------------|----------------|
|     |               |             | Type        | h (in) | d (in) | t <sub>m</sub> (in) | f <sub>m</sub> (psi) | FRP  | f <sub>fu</sub> (ksi) | E <sub>f</sub> (ksi) | ε <sub>fu</sub> (%) | A <sub>f</sub> (in <sup>2</sup> ) | V <sub>exp.</sub> (kips) | Failure Mode   |
| 1   | Grando        | GL-4        | CMU         | 64     | 64     | 5.625               | 2430                 | GFRP | 220                   | 10000                | 2.20                | 21.0                              | 46.8                     | Diagonal Shear |
| 2   | Grando        | CL-1        | CMU         | 64     | 64     | 5.625               | 2430                 | CFRP | 500                   | 33000                | 1.52                | 14.0                              | 25.4                     | Diagonal Shear |
| 3   | Morbin        | GL-1        | CMU         | 64     | 64     | 5.625               | 2430                 | GFRP | 220                   | 10000                | 2.20                | 16.0                              | 42.0                     | Diagonal Shear |
| 4   | Santa Maria   | FX-01       | Clay Brick  | 80     | 80     | 5.6                 | 1595                 | CFRP | 500                   | 33000                | 1.52                | 24.0                              | 58.3                     | Diagonal Shear |
| 5   | Santa Maria   | FX-02       | Clay Brick  | 80     | 80     | 5.6                 | 1595                 | CFRP | 500                   | 33000                | 1.52                | 16.0                              | 51.6                     | Diagonal Shear |
| 6   | Santa Maria   | FH-02       | Clay Brick  | 80     | 80     | 5.6                 | 1595                 | CFRP | 500                   | 33000                | 1.52                | 36.0                              | 51.0                     | Diagonal Shear |
| 7   | Santa Maria   | FH-04       | Clay Brick  | 80     | 80     | 5.6                 | 1595                 | CFRP | 500                   | 33000                | 1.52                | 24.0                              | 49.5                     | Diagonal Shear |
| 8   | Senescu       | Single W    | Clay Brick  | 30     | 30     | 3.625               | 2906                 | GFRP | 44.1                  | 2270                 | 1.94                | 30.0                              | 56.0                     | Diagonal Shear |
| 9   | Stratford     | Conc2       | Conc. Brick | 48     | 48     | 4                   | 1500                 | GFRP | 143                   | 10633                | 1.34                | 48.0                              | 24.7                     | Diagonal Shear |
| 10  | Stratford     | Conc3       | Conc. Brick | 48     | 48     | 4                   | 1500                 | GFRP | 143                   | 10633                | 1.34                | 48.0                              | 27.0                     | Diagonal Shear |
| 11  | Valuzzi       | PR1Carb2F   | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | CFRP | 500                   | 33000                | 1.52                | 2.8                               | 22.6                     | Diagonal Shear |
| 12  | Valuzzi       | PR2Carb2F   | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | CFRP | 500                   | 33000                | 1.52                | 2.8                               | 25.5                     | Diagonal Shear |
| 13  | Valuzzi       | PR3Carb2F   | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | CFRP | 500                   | 33000                | 1.52                | 2.8                               | 22.6                     | Diagonal Shear |
| 14  | Valuzzi       | PR1Glass2F  | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | GFRP | 240                   | 9400                 | 2.55                | 7.1                               | 24.0                     | Diagonal Shear |
| 15  | Valuzzi       | PR2Glass2F  | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | GFRP | 240                   | 9400                 | 2.55                | 7.1                               | 30.4                     | Diagonal Shear |
| 16  | Valuzzi       | PR3Glass2F  | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | GFRP | 240                   | 9400                 | 2.55                | 7.1                               | 23.2                     | Diagonal Shear |
| 17  | Valuzzi       | PRD1Carb2F  | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | CFRP | 500                   | 33000                | 1.52                | 4.0                               | 32.2                     | Diagonal Shear |
| 18  | Valuzzi       | PRD2Carb2F  | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | CFRP | 500                   | 33000                | 1.52                | 4.0                               | 33.6                     | Diagonal Shear |
| 19  | Valuzzi       | PRD1Glass2F | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | GFRP | 240                   | 9400                 | 2.55                | 6.6                               | 38.3                     | Diagonal Shear |
| 20  | Valuzzi       | PRD2Glass2F | Clay Brick  | 20.4   | 20.4   | 4.8                 | 806                  | GFRP | 240                   | 9400                 | 2.55                | 6.6                               | 40.5                     | Diagonal Shear |
| 21  | Zhao          | Wall2       | Clay Brick  | 39.4   | 55.1   | 9.4                 | 980                  | CFRP | 300                   | 20000                | 1.50                | 11.8                              | 74.6                     | Diagonal Shear |
| 22  | Zhao          | Wall3       | Clay Brick  | 39.4   | 55.1   | 9.4                 | 980                  | CFRP | 300                   | 20000                | 1.50                | 11.8                              | 75.5                     | Diagonal Shear |
| 23  | Zhao          | Wall4       | Clay Brick  | 39.4   | 55.1   | 9.4                 | 980                  | CFRP | 300                   | 20000                | 1.50                | 7.9                               | 64.7                     | Diagonal Shear |
| 24  | Tinazzi       | Wall 5      | Clay Brick  | 24     | 24     | 3.625               | 2050                 | GFRP | 220                   | 10500                | 2.10                | 32.0                              | 26.1                     | Diagonal Shear |
| 25  | Tinazzi       | Wall 6      | Clay Brick  | 24     | 24     | 3.625               | 2500                 | GFRP | 220                   | 10500                | 2.10                | 16.0                              | 28.7                     | Diagonal Shear |
| 26  | Santa Maria 1 | MDF2        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 24.0                              | 44.0647                  | Diagonal Shear |
| 27  | Santa Maria 1 | MDF3        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 24.0                              | 44.0647                  | Diagonal Shear |
| 28  | Santa Maria 1 | CDF4        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 24.0                              | 45.1888                  | Diagonal Shear |
| 29  | Santa Maria 1 | CDF5        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 24.0                              | 45.6385                  | Diagonal Shear |
| 30  | Santa Maria 1 | MHL2        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 406                   | 23200                | 1.75                | 12.0                              | 31.9245                  | Diagonal Shear |
| 31  | Santa Maria 1 | CHL3        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 406                   | 23200                | 1.75                | 12.0                              | 34.6223                  | Diagonal Shear |
| 32  | Santa Maria 1 | CHL4        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 406                   | 23200                | 1.75                | 12.0                              | 32.8237                  | Diagonal Shear |
| 33  | Santa Maria 1 | MHF3        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 12.0                              | 35.2968                  | Diagonal Shear |
| 34  | Santa Maria 1 | CHF4        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 12.0                              | 40.2428                  | Diagonal Shear |
| 35  | Santa Maria 1 | CHF5        | Clay Brick  | 44     | 42.4   | 5.6                 | 1494                 | CFRP | 500                   | 33000                | 1.51515             | 12.0                              | 43.6151                  | Diagonal Shear |

Table 4 -- Database for calibration of  $\kappa_v$  – NSM FRP Bars(1 in.=25.4 mm, 1 in<sup>2</sup>= 645 mm<sup>2</sup>, 1 ksi = 6.895 MPa, 1 kip=4.448 kN)

| No. | Source   | Specimen | MASONRY    |           |           |                        |                          | FRP              |                          |                         |                        |  |                                      |                             | Experimental Results |  |
|-----|----------|----------|------------|-----------|-----------|------------------------|--------------------------|------------------|--------------------------|-------------------------|------------------------|--|--------------------------------------|-----------------------------|----------------------|--|
|     |          |          | Type       | h<br>(in) | d<br>(in) | t <sub>m</sub><br>(in) | f' <sub>m</sub><br>(psi) | FRP              | f <sub>fu</sub><br>(ksi) | E <sub>f</sub><br>(ksi) | g <sub>fu</sub><br>(%) | A <sub>bar</sub><br>(in <sup>2</sup> ) | A <sub>f</sub><br>(in <sup>2</sup> ) | V <sub>exp.</sub><br>(kips) | Failure Mode         |  |
| 1   | Grando   | COW2     | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.350                                | 31.8                        | Diagonal Shear       |  |
| 2   | Grando   | COW3     | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.350                                | 31                          | Diagonal Shear       |  |
| 3   | Grando   | COW8     | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.350                                | 29.3                        | Diagonal Shear       |  |
| 4   | Grando   | CT-3     | CMU        | 64        | 64        | 5.625                  | 2430                     | CFRP Rectangular | 201.9                    | 20702                   | 0.98                   | 0.05                                   | 0.144                                | 30.0                        | Diagonal Shear       |  |
| 5   | Grando   | CT-5     | CMU        | 64        | 64        | 5.625                  | 2430                     | CFRP Rectangular | 201.9                    | 20702                   | 0.98                   | 0.05                                   | 0.240                                | 24.4                        | Diagonal Shear       |  |
| 6   | Morbin   | COW10    | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.350                                | 38.3                        | Diagonal Shear       |  |
| 7   | Morbin   | COW12    | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.150                                | 30.3                        | Diagonal Shear       |  |
| 8   | Secondin | GT-3     | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Rectangular | 160                      | 6382                    | 2.51                   | 0.05                                   | 0.146                                | 35.4                        | Diagonal Shear       |  |
| 9   | Secondin | GT-5     | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Rectangular | 160                      | 6382                    | 2.51                   | 0.05                                   | 0.243                                | 39.4                        | Diagonal Shear       |  |
| 10  | Tinazzi  | Wall2    | Clay Brick | 24        | 24        | 3.625                  | 2500                     | GFRP Round       | 120                      | 5920                    | 2.027                  | 0.05                                   | 0.400                                | 25.2                        | Diagonal Shear       |  |
| 11  | Tinazzi  | Wall3    | Clay Brick | 24        | 24        | 3.625                  | 2500                     | GFRP Round       | 120                      | 5920                    | 2.027                  | 0.05                                   | 0.400                                | 20.8                        | Diagonal Shear       |  |
| 12  | Tinazzi  | Wall4    | Clay Brick | 24        | 24        | 3.625                  | 2500                     | GFRP Round       | 120                      | 5920                    | 2.027                  | 0.05                                   | 0.400                                | 23.3                        | Diagonal Shear       |  |
| 13  | Tinazzi  | Wall7    | Clay Brick | 24        | 24        | 3.625                  | 2050                     | GFRP Round       | 120                      | 5920                    | 2.027                  | 0.05                                   | 0.800                                | 28.0                        | Diagonal Shear       |  |
| 14  | Tinazzi  | Wall10   | Clay Brick | 24        | 24        | 7.25                   | 2050                     | GFRP Round       | 120                      | 5920                    | 2.027                  | 0.05                                   | 0.800                                | 21.5                        | Diagonal Shear       |  |
| 15  | Tumialan | W2       | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.350                                | 51.3                        | Diagonal Shear       |  |
| 16  | Tumialan | W3       | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.500                                | 56.3                        | Diagonal Shear       |  |
| 17  | Tumialan | W4       | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.500                                | 53.8                        | Diagonal Shear       |  |
| 18  | Yu       | W3       | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.150                                | 29.8                        | Diagonal Shear       |  |
| 19  | Yu       | W4       | CMU        | 64        | 64        | 5.625                  | 2430                     | GFRP Round       | 120                      | 7276                    | 1.65                   | 0.05                                   | 0.350                                | 35.6                        | Diagonal Shear       |  |



### Effective strain for flexure-controlled sections

The effective strain and stress used for the design of the flexural strengthening of URM walls due to out-of-plane and in-plane loads is limited to the strain level at which debonding may occur,  $\epsilon_{fd}$ :

$$\epsilon_{fd} = \kappa_m \epsilon_{fu}^* \leq C_E \epsilon_{fu}^* \quad \text{ACI 440.7R Eq. (8-6)}$$

$\epsilon_{fu}^*$  is the ultimate rupture strain of the FRP reinforcement as reported by the manufacturer and  $C_E$  is an environmental reduction factor, which depends on the FRP system and exposure condition (ACI 440.7R Table 8.1)

Where the  $\kappa_m$  coefficients are set as:

$$\kappa_m = \begin{cases} 0.45 & \text{for surface-mounted FRP systems} \\ 0.35 & \text{for NSM FRP systems} \end{cases} \quad \text{ACI 440.7R Eq. (8-8)}$$

It should be noted that surface-mounted FRP systems include wet layup or precured systems (hereafter referred to as laminates). Also, Eq. (8-8) is applicable only when the total force per unit width (per bar for NSM systems) that the FRP system transfers to the masonry substrate satisfies the limitation given in Eq. (8-9).

$$\rho_{fm} = \begin{cases} n t_f f_{fe} \leq 1500 \text{ lb/in.} & \text{for surface-mounted FRP systems} \\ A_{f,bar} \leq 10,000 \text{ lb/bar} & \text{for NSM FRP systems} \end{cases} \quad \text{ACI 440.7R Eq. (8-9)}$$

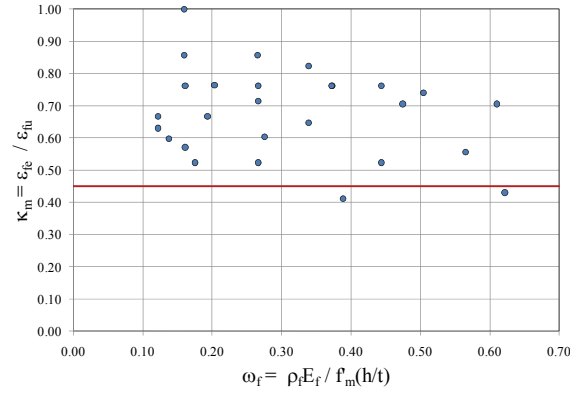
(1 lb/in = 0.175 N/mm, 1 lb = 4.448 N)

Basis for bond-reduction coefficient for flexure ( $\kappa_m$ ) – Previous investigations show that URM walls strengthened in flexure with FRP systems have the following modes of failure: 1) debonding of the FRP laminate or bar from the masonry substrate; 2) flexural failure (i.e. rupture of the FRP laminate in tension or crushing of the masonry in compression); and, 3) shear failure in the masonry. Of these three modes of failure, debonding is the most common mode of failure

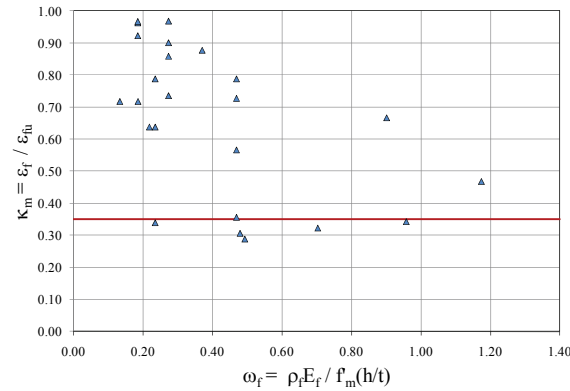
The majority of the test results used in the data base did not report the strain in FRP at failure (experimental effective strain). Thus, the data analysis required back-calculations to estimate the effective strain, using the moment at failure, and strain compatibility and internal force equilibrium principles. Similarly to the analysis of concrete members strengthened with FRP, well-established relationships were used to define the masonry compressive block equivalent to the non-linear stress-strain distribution. In accordance with MSJC recommendations, the maximum usable strain  $\epsilon_{mu}$  was 0.0035 in./in. (mm/mm) for clay masonry, and 0.0025 in./in. (mm/mm) for concrete masonry. The tensile strength of masonry was neglected. For data points reporting experimental strains, the back-calculation procedure showed good agreement between the experimental and analytical strains.



The bond-reduction coefficient,  $\kappa_m$ , is basically an efficiency factor, measured as the ratio between the effective strain in the FRP and the ultimate tensile strain of FRP. Figures 1a and 1b illustrate the relationship between the effective-to-ultimate strain ratio,  $\varepsilon_{fe}/\varepsilon_{fu}$ , and the adjusted reinforcement ratio,  $\omega_f$ , for masonry specimens strengthened with FRP laminates and FRP bars, respectively. The term  $\omega_f$  is expressed as:  $\rho_f E_f / f'_m (h/t)$ , where:  $\rho_f$  is the FRP reinforcement ratio equal to  $A_f/(b t)$  (FRP area over cross-section area),  $E_f$  is the FRP elastic modulus,  $f'_m$  is the masonry compressive strength, and  $h/t$  is the wall height-to-thickness slenderness ratio. The  $\omega_f$  ratio intends to capture the effect of other parameters, in addition to  $\rho_f$ , influencing the wall behavior: 1) the FRP stiffness; 2) the masonry compressive strength that directly affects the out-of-plane flexural capacity; and, 3) the slenderness ratio  $h/t$  that is identified as one of the most influential parameters in the out-of-plane behavior of masonry walls. The slenderness ratio and the out-of-plane capacity are inversely proportional: as the slenderness ratio decreases, the out-of-plane flexural capacity becomes larger.



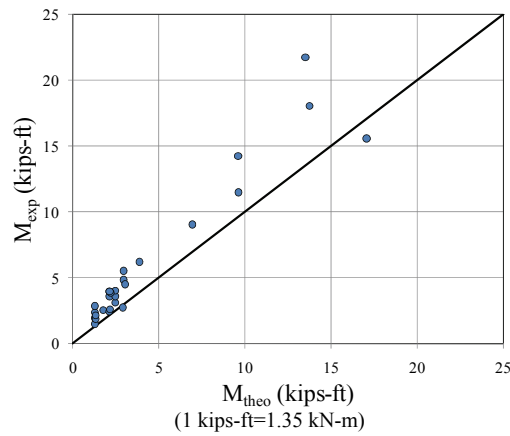
(a) FRP Laminates



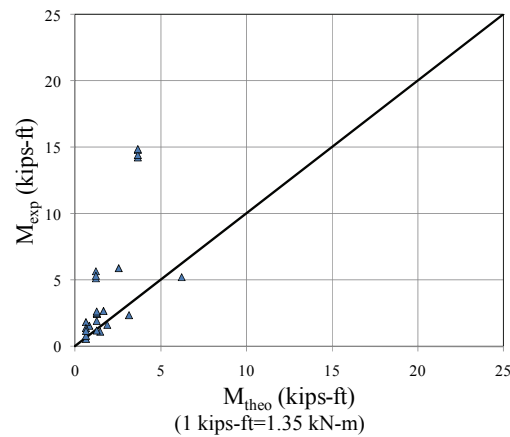
(b) NSM FRP Bars

Figure 1 –  $\kappa_m$  vs.  $\omega_f$  Plots

Figures 1a and 1b do not show a clear trend that can be used to establish an equation or set of equations to compute  $\kappa_m$ . However, the diagrams suggest that the lower limits of  $\kappa_m$  for masonry strengthened with FRP laminates can be taken as 0.45; whereas for masonry strengthened with FRP bars, this value can be taken as 0.35. Figure 2a and 2b show the correlation between the experimental and expected flexural strengths.



(a) FRP Laminates



(b) NSM FRP Bars

Figure 2 – Validation of Design Approach for Flexural Strengthening

It is important to note that the database represents research on a fairly limited range of FRP system types and layouts. The FRP systems tested involve the use of commercially available FRP fabric systems or NSM bars. However most only use one layer of FRP fabric or small diameter (1/2 in. [25 mm] or less) bars. Due to the limited range of FRP systems tested, it is not currently known how the use of much higher

stiffness systems (such as multiple layer systems or large diameter bars) would affect the effective strain. It would be expected that higher stiffness systems would result in lower effective strains. However, the extent to which the strain would be reduced is not known at this time. It is for this reason that the limitations given in Eq. (8-9) are introduced. These criteria limit the type of FRP system used to the range of systems that are in the current database.

#### **Effective strain for shear-controlled sections**

The effective strain and stress used for the design of the shear strengthening of URM walls due to in-plane loads is limited to the strain level at which premature failures may occur,  $\varepsilon_{fd}$ :

$$\varepsilon_{fd} = \kappa_v \varepsilon_{fu}^* \leq C_E \varepsilon_{fu}^* \quad \text{ACI 440.7R Eq. (8-10)}$$

The  $\kappa_v$  coefficient depends on the FRP reinforcement index  $\omega_f$ , as defined in the following equation:

$$\omega_f = \frac{1}{1000} \frac{A_f E_f}{A_n \sqrt{f'_m}} \quad (\text{in-lbs units}) \quad \text{ACI 440.7R Eq. (8-12)}$$

Where the  $\kappa_v$  coefficients are defined as follows:

$$\kappa_v = \begin{cases} 0.40 & \text{for } \omega_f \leq 0.20 \\ 0.64 - 1.2\omega_f & \text{for } 0.20 < \omega_f \leq 0.45 \\ 0.10 & \text{for } \omega_f > 0.45 \end{cases} \quad \text{ACI 440.7R Eq. (8-13)}$$

Similar to flexure-controlled failure modes, Eq. (8-13) is applicable only when the force per unit width (per bar for NSM systems) that the FRP system transfers to the masonry substrate satisfies the limitation given in Eq. (8-14).

$$\rho_{fm} = \begin{cases} n t_f f_{fe} \leq 1500 \text{ lb/in. for surface-mounted FRP systems} \\ A_{f,bar} \leq 10,000 \text{ lb/bar for NSM FRP systems} \end{cases} \quad \text{ACI 440.7R Eq. (8-14)}$$

(1 lb/in = 0.175 N/mm, 1 lb = 4.448 N)

It is recognized that the  $\kappa_m$  and  $\kappa_v$  coefficients in Eq. (8-6) and Eq. (8-10) will always control over the  $C_E$  coefficients. However it should be noted that the bond dependent coefficients were set as a lower bound based on available experimental data. Future investigations may provide in higher  $\kappa_m$  and  $\kappa_v$  coefficients. The upper limitation involving the  $C_E$  factor is included to establish a design philosophy that will remain consistent. Furthermore, ACI 440.7R recommends the use of larger values of  $\kappa_m$  and  $\kappa_v$  for a particular application is available, if these coefficients are properly substantiated by testing.

Basis for bond-reduction coefficient for shear ( $\kappa_v$ ) – In walls strengthened with FRP, shear failure develops from an initial diagonal crack, which is followed by secondary cracks, typically parallel to the first crack. Diagonal cracks run through masonry units (common in brick walls) or can follow the mortar joints – stepped cracking (common in CMU walls). As the cracks in the wall grow and widen, the wall fails when the FRP system debonds from the masonry substrate and/or when the masonry is unable to transfer shear friction through cracked interfaces because of the wide cracks.

The bond-reduction coefficient  $\kappa_v$  accounts for the premature failure of the FRP-strengthened wall caused by these mechanisms. For the data analysis the coefficient  $\kappa_v$  was estimated as the ratio between the experimental shear contribution of FRP,  $V_{f\text{-exp}}$ , and the expected maximum shear contribution of FRP,  $V_{f\text{max}}$ , to the overall wall shear capacity if premature failures do not occur (i.e. FRP rupture governs the wall behavior).  $V_{f\text{exp}}$  was determined by subtracting the ultimate load reported for the control walls (unstrengthened walls) from the ultimate loads of the strengthened walls.  $V_{f\text{theo}}$  was estimated using the following equation:

$$V_{f\text{theo}} = \kappa_v \frac{A_f f_{fu} d_v}{s_f} \cos \alpha \quad \text{Eq. (1)}$$

$A_f$  is the total area of FRP reinforcement,  $f_{fu}$  is the ultimate FRP tensile strength,  $d_v$  is the actual depth of masonry in direction of the shear force,  $s_f$  is the center-to-center spacing between each FRP laminate or bar, and  $\alpha$  represents the fibers inclination.

Figures 3a and 3b illustrate the relationship between ratio of the experimental and theoretical FRP shear contribution and the adjusted reinforcement ratio,  $\omega_{fv}$ , for masonry specimens strengthened with FRP laminates and FRP bars, respectively.  $\omega_{fv}$  intends to recognize the relationship between the FRP stiffness and the masonry shear strength, and it is expressed as:

$$\omega_{fv} = \frac{A_f E_f}{A_m \sqrt{f'_m}} \quad (\text{in-lbs units}) \quad \text{Eq. (2)}$$

Where:  $E_f$  is the FRP elastic modulus,  $A_m$  is the net shear area, and  $f'_m$  is the masonry compressive strength.

Although, the diagrams do not show a clear trend, two zones for  $\kappa_v$  can be distinguished. This suggests that  $\kappa_v$  can be defined based on the magnitude of the reinforcement ratio  $\omega_{fv}$ . Basically, larger  $\kappa_v$  coefficients are observed when  $\omega_{fv}$  are about or smaller than 0.20. The  $\kappa_v$  coefficients decrease to about 0.10 when  $\omega_{fv}$  are larger than 0.45. Figures 4a and 4b show the correlation between the experimental and expected shear strengths.

Similar to Eq. (8-9) for flexure-controlled sections, Eq. (8-14) provides criteria that limit the type of FRP systems used to the range of systems that are in the current database.

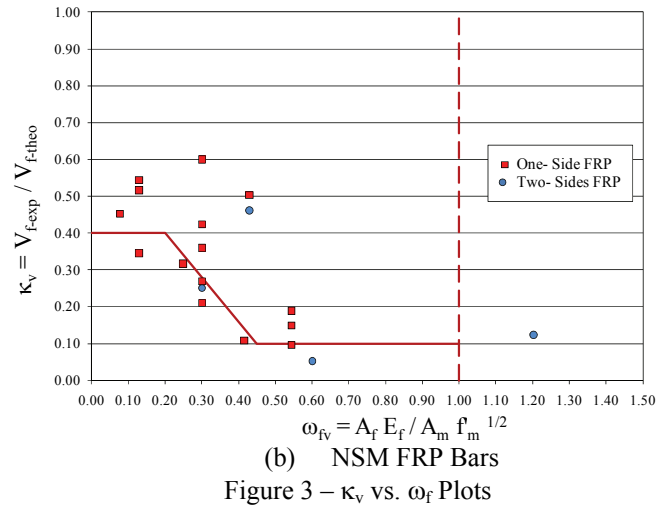
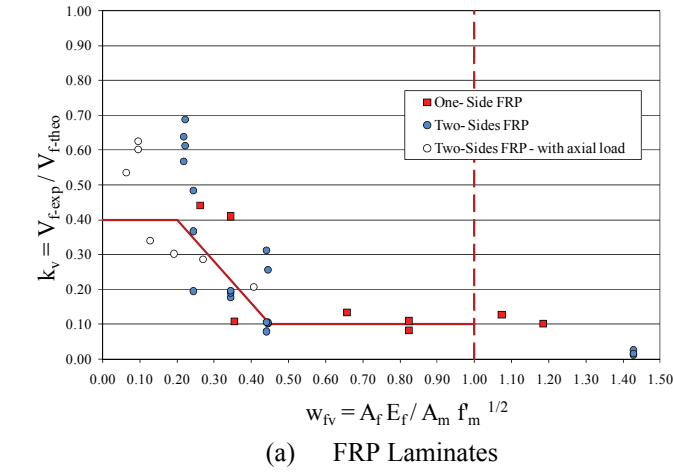


Figure 3 –  $\kappa_v$  vs.  $\omega_f$  Plots

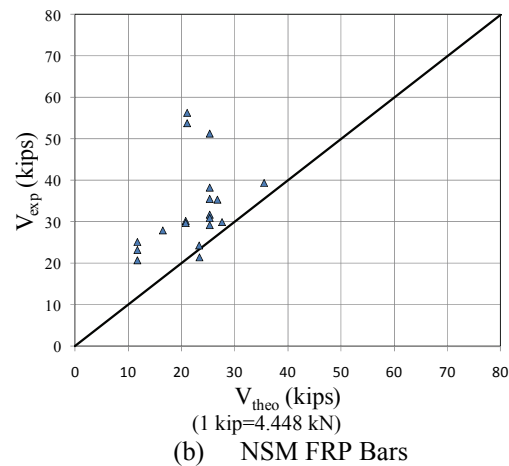
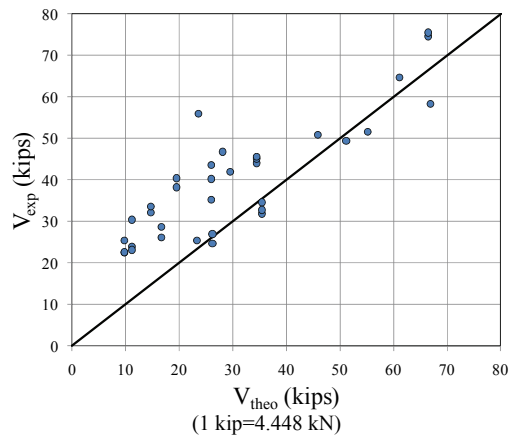


Figure 4 – Validation of Design Approach for Shear Strengthening

## DESIGN PROTOCOLS FOR FRP STRENGTHENING OF URM WALLS

### FRP Flexural strengthening for out-of-plane loads

**Nominal Flexural Strength** – The ultimate strength design method requires that the design flexural strength of the strengthened wall must exceed the flexural demand:

$$\phi M_n \geq M_u \quad \text{ACI 440.7R Eq. (9-1)}$$

The nominal flexural capacity is computed considering a reduction factor,  $\phi$ , equal to 0.60, which is similar to the  $\phi$ -factor specified by the Building Code Requirements and Specification for Masonry Structures (MSJC 2008) for URM walls subjected to flexural loads, axial loads or combination of both. The use of this  $\phi$ -factor is

justified by the need to compensate a section with low ductility with a higher reserve of strength. The approach for the reduction factor is similar to that of the ACI-318, where a section with low ductility must be compensated with a higher reserve of strength. The higher reserve of strength can be attained by applying a strength reduction factor of 0.60 to sections prone to have brittle or premature failures such as debonding of the FRP laminate.

The nominal flexural strength  $M_n$  of an FRP-strengthened URM wall is expressed as shown in the equation below. In this equation the factored axial load,  $P_u$ , is assumed to be acting at the wall section centroid. The equation can be modified to include the effect of the eccentric loads, typically found in load-bearing masonry construction.

$$M_n = A_f f_{fe} \left( d_f - \frac{\beta_1 c}{2} \right) + P_u \left( \frac{t}{2} - \frac{\beta_1 c}{2} \right) \quad \text{ACI 440.7R Eq. (9-2)}$$

The maximum strain level that can be achieved in the FRP reinforcement will be governed by either the strain level developed in the FRP at the point at which masonry crushes, or the point at which the FRP debonds from the substrate. The effective strain level in the FRP reinforcement at ultimate limit can be calculated from the following relationship.

$$\varepsilon_{fe} = \varepsilon_{mu} \left( \frac{t - c}{c} \right) \leq \min(\kappa_m \varepsilon_{fu}^*, C_E \varepsilon_{fu}^*) \quad \text{ACI 440.7R Eq. (9-3)}$$

The flexural strength is calculated by solving Eq. 9-2 and Eq. 9-3, including the parameters defining the well-known rectangular stress block in the masonry equivalent the nonlinear distribution of stress, and considering the following assumptions:

- The strains in the FRP reinforcement and masonry are directly proportional to their distance from the neutral axis
- The maximum usable compressive strain in concrete masonry is 0.0025, and 0.0035 for clay and natural stone masonry
- FRP reinforcement is linear elastic up to failure
- The contributions of masonry in tension and FRP reinforcement in compression are neglected
- There is no relative slip between the FRP reinforcement and masonry until debonding failure occurs; and
- The wall behaves as a simply supported element or very nearly so (i.e. arching mechanism does not develop)

Limitations for FRP Flexural Strengthening – There are two primary limitations for strengthening of URM walls with FRP, related to the slenderness ratio  $h/t$  of the wall.

- Walls with  $h/t$  larger than 20 should not be strengthened with FRP systems unless the efficiency of FRP has been properly substantiated by testing. This limitation is based on the  $h/t$  ratios included limitation in the database used to calibrate the bond-dependent coefficient, and in the risk of strengthening very slender walls which



could potentially be unstable due to out-of-plane load and secondary bending moments caused by axial loads (including self-weight) when deforming due to the out-of-plane loading.

- Walls with  $h/t$  smaller than 8 and built within stiff supports most likely will not require to be strengthened because the wall can develop arching mechanism. Galati et al. (2007) presents a protocol for FRP flexural strengthening of URM walls in the event that the analysis considering arching shows that strengthening is required. It should be noted that the contribution of FRP to the URM flexural strength is not as pronounced as in the cases of slender and/or simply-supported walls, being many times just a marginal increase.

**FRP Spacing Limits in Flexural Strengthening** – ACI 440.7R recommends that the maximum center-to-center spacing of FRP systems in walls strengthened in flexure should meet the following spacing requirements.

FRP laminates:  $s_{f,max} \leq 3t + w_f$

NSM FRP bars:  $s_{f,max} \leq 3t$

Where  $w_f$  is the width of the FRP laminate

These reduced limits are conservative design considerations, which are justified by the difference in behavior between an FRP-strengthened URM wall and a reinforced wall with steel reinforcement in grouted cells. In a new reinforced masonry wall, in addition to span between supports, masonry also spans between the grouted cells, which essentially behave as pilasters. For this reason the steel reinforcement can be spaced up to  $6t$ . Contrarily, in an FRP-strengthened URM wall, the FRP reinforcement is not grouted and the FRP sections are not stiff enough to cause horizontal bending.

### **FRP shear strengthening for in-plane loads**

**Nominal Shear Strength** – The ultimate strength design method requires that the design shear strength of the strengthened wall must exceed the shear demand:

$$\phi V_n \geq V_u \quad \text{ACI 440.7R Eq. (10-2)}$$

The nominal shear capacity is computed considering a reduction factor,  $\phi$ , equal to 0.80, which is similar to the  $\phi$ -factor specified by MSJC (2008) for URM walls subjected to shear loads.

The nominal shear strength  $V_n$  of the FRP-strengthened wall can be estimated as the summation of the contributions of masonry and FRP.

$$V_n = V_n^{URM} + V_f \quad \text{ACI 440.7R Eq. (10-3)}$$

$V_n^{URM}$  is the nominal shear strength given of the unreinforced wall, which can be estimated following recommendations provided by MSJC or ASCE-41 (2006). The FRP contribution to the shear strength  $V_f$  can be estimated as:

$$V_f = \begin{cases} p_{fv} w_f \frac{d_v}{s_f} & \text{for surface-mounted FRP systems} \\ p_{fv} \frac{d_v}{s_f} & \text{for NSM FRP systems} \end{cases} \quad \text{ACI 440.7R Eq. (10-4)}$$

Where  $p_{fv}$  is computed according to Eq. 8-14,  $w_f$  is the width of the FRP laminates,  $s_f$  is the center-to-center spacing between strips or bars, and  $d_v$  is the effective masonry depth for shear calculations, calculated as the minimum of the wall height  $H$ , and the wall length  $L$ .

Limitations for FRP Shear Strengthening – The in-plane shear performance of FRP-strengthened walls depends on the type of masonry construction and the FRP strengthening layout. Test results have shown that FRP systems can significantly increase the shear capacity of URM walls when the existing shear strength of the wall is not large such as the case of single-wythe or ungrouted walls). Contrarily, when the existing shear strength of the URM wall is large (multi-wythe or grouted walls), the contribution of FRP has been marginal in some situations. Test results also indicate that the FRP layout influences the structural performance of the wall. For instance, in thick walls, FRP placed on the two wall sides has been shown to be more effective than FRP placed on one side. In the absence of project specific experimental evidence, ACI 440.7R-10 recommends adopting the limitations shown on Table 5.

Table 5 -- FRP limitations for shear strengthening (ACI 440.7R Table 10.1)

| Masonry Type             | Wall Construction   | FRP Strengthening Layout              |
|--------------------------|---|---------------------------------------|
| Hollow unit masonry wall | $t = 8$ in. (200 mm) or less<br>UngROUTED or partially grouted walls<br>with grouted cells spaced greater than 48 in. (1.20 m)    | FRP on one face of wall is acceptable |
|                          | $t = 8$ in. (200 mm) or less<br>Fully or partially grouted walls with grouted cells spaced at 48 in. (1.20 m) or less             | FRP on two faces of wall is required  |
|                          | $t = 10$ to 12 in. (250 to 300 mm)<br>UngROUTED or partially grouted walls with grouted cells spaced greater than 60 in. (1.50 m) | FRP on two faces of wall is required  |
|                          | $t = 10$ to 12 in. (250 to 300 mm)<br>Fully or partially grouted walls with grouted cells spaced at 60 in. (1.50 m) or less       | Use of FRP is not recommended         |
|                          | $t$ greater than 12 in. (300 mm)<br>UngROUTED or grouted  | Use of FRP is not recommended         |
| Solid unit masonry wall  | Single-wythe walls with<br>$t = 4$ in. (100 mm) or less   | FRP on one face of wall is acceptable |
|                          | Double-wythe walls with<br>$t = 8$ in. (200 mm) or less   | FRP on two faces of wall is required  |
|                          | Multi-wythe walls with<br>$t > 8$ in. (200 mm)  | Use of FRP is not recommended         |

FRP Spacing Limits in Shear Strengthening – ACI 440.7R recommends that the maximum center-to-center spacing of FRP systems in walls strengthened in shear should meet the following requirements.

FRP laminates:  $s_{f,max} \leq 16 \text{ in. (400 mm)} + w_f$

NSM FRP bars:  $s_{f,max} \leq 16 \text{ in. (400 mm)}$

The spacing limitation of 16 in. (400 mm) is based on MSJC provisions for spacing of horizontal reinforcement when the reinforcement is placed in the bed joints.

### FINAL REMARKS

The retrofitting of existing masonry with FRP systems is of particular relevance for the case of URM walls to improve capacity under out-of-plane and in-plane loads. It is expected that the use of FRP systems in masonry applications will become a more common staple for design professionals and contractors with the availability of ACI guides for design and construction procedures of masonry strengthening with FRP systems.

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