

Tabla de derivadas

1. $D_x(u^n) = nu^{n-1}D_x u$
2. $D_x(u + v) = D_x u + D_x v$
3. $D_x(uv) = uD_x v + vD_x u$
4. $D_x\left(\frac{u}{v}\right) = \frac{vD_x u - uD_x v}{v^2}$
5. $D_x(e^u) = e^u D_x u$
6. $D_x(a^u) = a^u \ln a D_x u$
7. $D_x(\ln u) = \frac{1}{u} D_x u$
8. $D_x(\operatorname{sen} u) = \cos u D_x u$
9. $D_x(\cos u) = -\operatorname{sen} u D_x u$
10. $D_x(\tan u) = \sec^2 u D_x u$
11. $D_x(\cot u) = -\csc^2 u D_x u$
12. $D_x(\sec u) = \sec u \tan u D_x u$
13. $D_x(\csc u) = -\csc u \cot u D_x u$
14. $D_x(\operatorname{arcsen} u) = \frac{1}{\sqrt{1-u^2}} D_x u$

*Tabla de integrales**Formas elementales*

1. $\int du = u + c$
2. $\int a du = au + c$
3. $\int [f(u) + g(u)]du = \int f(u)du + \int g(u)du$
4. $\int u^n du = \frac{u^{n+1}}{n+1} + c \quad (n \neq 1)$
5. $\int \frac{du}{u} = \ln|u| + c$

Formas que contienen $a^2 \pm u^2$

$$6. \int \frac{du}{a^2 + u^2} = \frac{1}{a} \arctan \frac{u}{a} + c$$

$$7. \int \frac{du}{a^2 - u^2} = \frac{1}{2a} \ln \left| \frac{u+a}{u-a} \right| + c = \begin{cases} \frac{1}{a} \operatorname{arctanh} \frac{u}{a} + c & \text{si } |u| < a \\ \frac{1}{a} \operatorname{arccoth} \frac{u}{a} + c & \text{si } |u| > a \end{cases}$$

$$8. \int \frac{du}{u^2 - a^2} = \frac{1}{2a} \ln \left| \frac{u-a}{u+a} \right| + c = \begin{cases} -\frac{1}{a} \operatorname{arctanh} \frac{u}{a} + c & \text{si } |u| < a \\ -\frac{1}{a} \operatorname{arccoth} \frac{u}{a} + c & \text{si } |u| > a \end{cases}$$

$$9. \int \frac{du}{\sqrt{u^2 \pm a^2}} = \ln \left| u + \sqrt{u^2 \pm a^2} \right| + c$$

$$10. \int \sqrt{u^2 \pm a^2} \, du = \frac{u}{2} \sqrt{u^2 \pm a^2} \pm \frac{a^2}{2} \ln \left| u + \sqrt{u^2 \pm a^2} \right| + c$$

$$11. \int u^2 \sqrt{u^2 \pm a^2} \, du = \frac{u}{8} \cancel{(u^2 \pm a^2)} \sqrt{u^2 \pm a^2} - \frac{a^4}{8} \ln \left| u + \sqrt{u^2 \pm a^2} \right| + c$$

$$12. \int \frac{\sqrt{u^2 + a^2} \, du}{u} = \sqrt{u^2 + a^2} - a \ln \left| \frac{a + \sqrt{u^2 + a^2}}{u} \right| + c$$

$$13. \int \frac{\sqrt{u^2 - a^2} \, du}{u} = \sqrt{u^2 - a^2} - a \operatorname{arcsec} \frac{u}{a} + c$$

$$14. \int \frac{\sqrt{u^2 \pm a^2} \, du}{u^2} = -\frac{\sqrt{u^2 \pm a^2}}{u} + \ln \left| u + \sqrt{u^2 \pm a^2} \right| + c$$

Formas que contienen $\sqrt{a^2 - u^2}$

$$15. \int \frac{du}{\sqrt{a^2 - u^2}} = \operatorname{arcsen} \frac{u}{a} + c$$

$$16. \int \sqrt{a^2 - u^2} \, du = \frac{u}{2} \sqrt{a^2 - u^2} + \frac{a^2}{2} \operatorname{arcsen} \frac{u}{a} + c$$

$$17. \int u^2 \sqrt{a^2 - u^2} \, du = \frac{u}{8} \cancel{(u^2 - a^2)} \sqrt{a^2 - u^2} + \frac{a^4}{8} \operatorname{arcsen} \frac{u}{a} + c$$

Formas que contienen funciones trigonométricas

18. $\int \operatorname{sen} u \, du = -\cos u + c$
19. $\int \cos u \, du = \operatorname{sen} u + c$
20. $\int \tan u \, du = \ln|\sec u| + c$
21. $\int \cot u \, du = \ln|\operatorname{sen} u| + c$
22. $\int \sec u \, du = \ln|\sec u + \tan u| + c = \ln|\tan(\frac{\pi}{2} + \frac{1}{2}u)| + c$
23. $\int \csc u \, du = \ln|\csc u - \cot u| + c = \ln|\tan(\frac{1}{2}u)| + c$
24. $\int \sec^2 u \, du = \tan u + c$
25. $\int \csc^2 u \, du = -\cot u + c$
26. $\int \sec u \tan u \, du = \sec u + c$
27. $\int \csc u \cot u \, du = -\csc u + c$
28. $\int \operatorname{sen}^2 u \, du = \frac{1}{2}u - \frac{1}{4}\operatorname{sen}2u + c$
29. $\int \cos^2 u \, du = \frac{1}{2}u + \frac{1}{4}\operatorname{sen}2u + c$
30. $\int \tan^2 u \, du = \tan u - u + c$
31. $\int \cot^2 u \, du = -\cot u - u + c$
32. $\int \operatorname{sen}^n u \, du = -\frac{1}{n}\operatorname{sen}^{n-1} u \cos u + \frac{n-1}{n} \int \operatorname{sen}^{n-2} u \, du$
33. $\int \cos^n u \, du = \frac{1}{n}\cos^{n-1} u \operatorname{sen} u + \frac{n-1}{n} \int \cos^{n-2} u \, du$
34. $\int \tan^n u \, du = \frac{1}{n-1}\tan^{n-1} u - \int \tan^{n-2} u \, du$
35. $\int \cot^n u \, du = -\frac{1}{n-1}\cot^{n-1} u - \int \cot^{n-2} u \, du$
36. $\int \sec^n u \, du = \frac{1}{n-1}\sec^{n-2} u \tan u + \frac{n-2}{n-1} \int \sec^{n-2} u \, du$
37. $\int \csc^n u \, du = -\frac{1}{n-1}\csc^{n-2} u \cot u + \frac{n-2}{n-1} \int \csc^{n-2} u \, du$

Formas que contienen funciones exponenciales y logarítmicas

38. $\int e^u \, du = e^u + c$
39. $\int a^u \, du = \frac{a^u}{\ln a} + c$

$$40. \int \ln u \, du = u \ln u - u + c$$

Relaciones entre las razones trigonométricas

$$\operatorname{Sen} \alpha = \frac{1}{\operatorname{Csc} \alpha} \quad \operatorname{Csc} \alpha = \frac{1}{\operatorname{Sen} \alpha} \quad \operatorname{Sec} \alpha = \frac{1}{\operatorname{Cos} \alpha}$$

$$\operatorname{Cos} \alpha = \frac{1}{\operatorname{Sec} \alpha} \quad \operatorname{Tg} \alpha = \frac{1}{\operatorname{Ctg} \alpha} \quad \operatorname{Ctg} \alpha = \frac{1}{\operatorname{Tg} \alpha}$$

Identidades fundamentales:

$$\operatorname{Sen}^2 \alpha + \operatorname{Cos}^2 \alpha = 1 \quad \operatorname{Sen}^2 \alpha = 1 - \operatorname{Cos}^2 \alpha \quad \operatorname{Cos}^2 \alpha = 1 - \operatorname{Sen}^2 \alpha$$

$$\operatorname{Tg}^2 \alpha + 1 = \operatorname{Sec}^2 \alpha \quad \operatorname{Tg}^2 \alpha = \operatorname{Sec}^2 \alpha - 1 \quad \operatorname{Tg} \alpha = \frac{\operatorname{Sen} \alpha}{\operatorname{Cos} \alpha} \quad \operatorname{Sen} \alpha = \operatorname{Cos} \alpha \cdot \operatorname{Tg} \alpha$$

$$\operatorname{Ctg}^2 \alpha + 1 = \operatorname{Csc}^2 \alpha \quad \operatorname{Ctg}^2 \alpha = \operatorname{Csc}^2 \alpha - 1 \quad \operatorname{Ctg} \alpha = \frac{\operatorname{Cos} \alpha}{\operatorname{Sen} \alpha} \quad \operatorname{Cos} \alpha = \operatorname{Sen} \alpha \cdot \operatorname{Ctg} \alpha$$

Razones trigonométricas del ángulo doble:

$$\operatorname{Sen} 2\alpha = 2 \operatorname{Sen} \alpha \cdot \operatorname{Cos} \alpha \quad \operatorname{Tg} 2\alpha = \frac{2\operatorname{Tg} \alpha}{1 - \operatorname{Tg}^2 \alpha}$$

$$\operatorname{Cos} 2\alpha = 2\operatorname{Cos}^2 \alpha - 1 = 1 - 2\operatorname{Sen}^2 \alpha = \operatorname{Cos}^2 \alpha - \operatorname{Sen}^2 \alpha$$