

► CONFERENCIA

Equivalent frame modelling of URM buildings: validation examples on monitored structures and TRICKY issues

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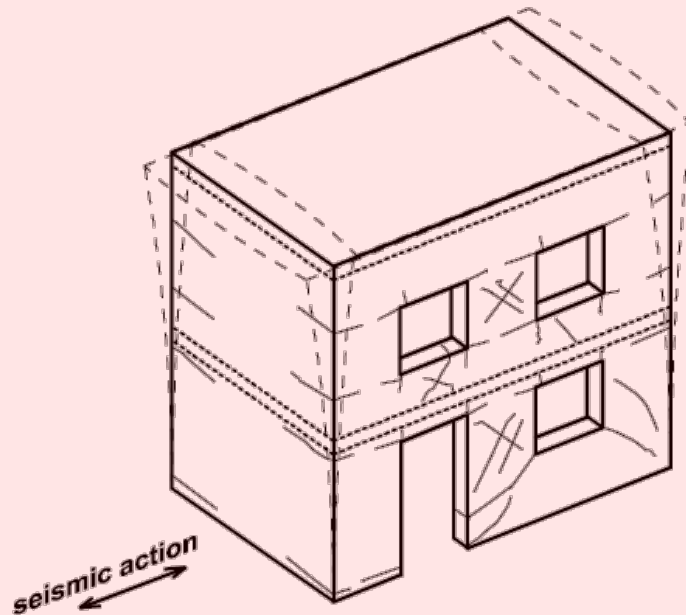


**Università
di Genova**

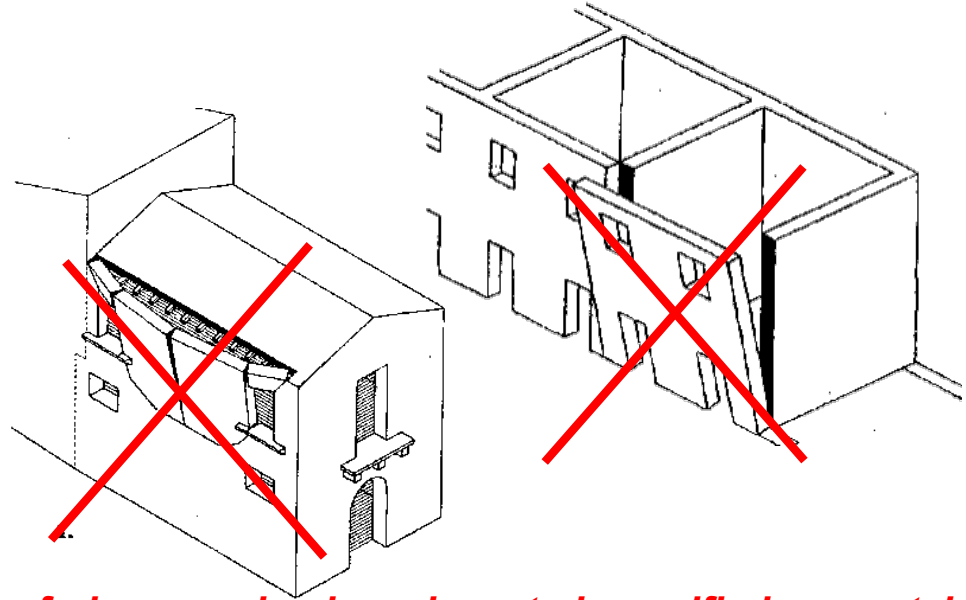
**DICCA – Department of Civil, Chemical and
Environmental Engineering**

INTRODUCTION - CONTEXT

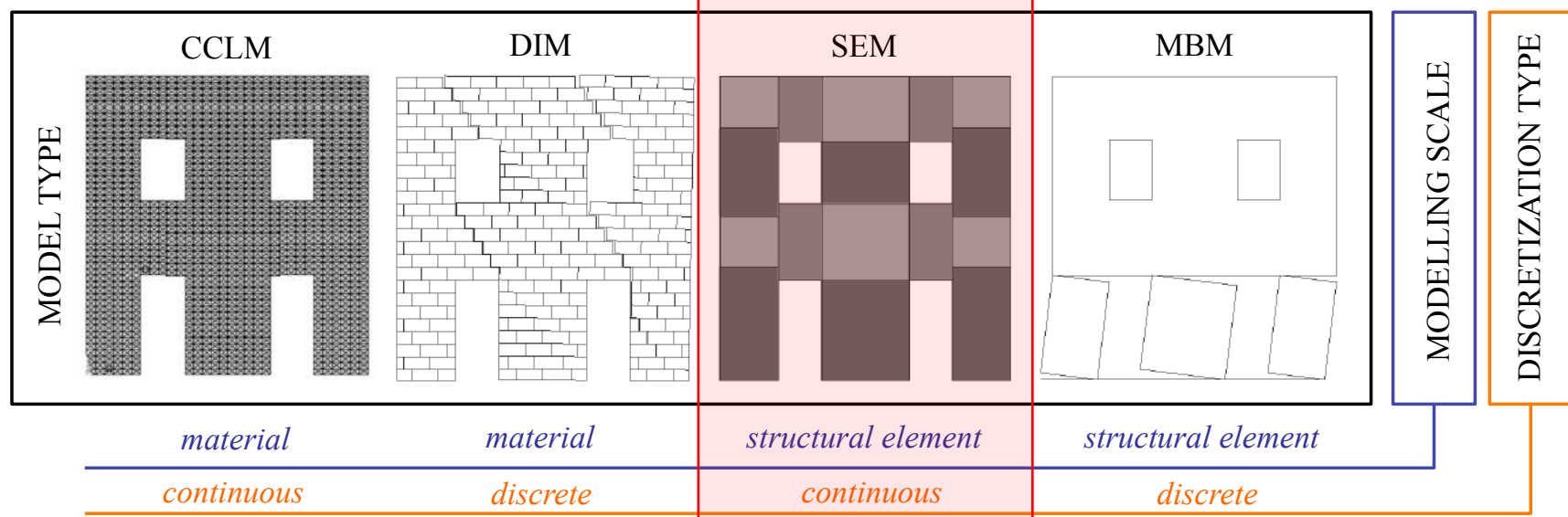
**In-plane failure mode:
Global behaviour of the building**



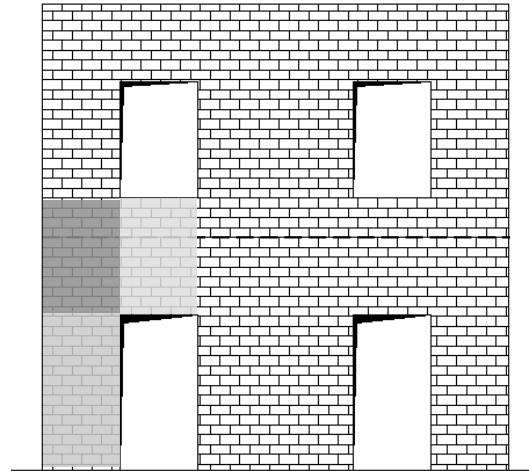
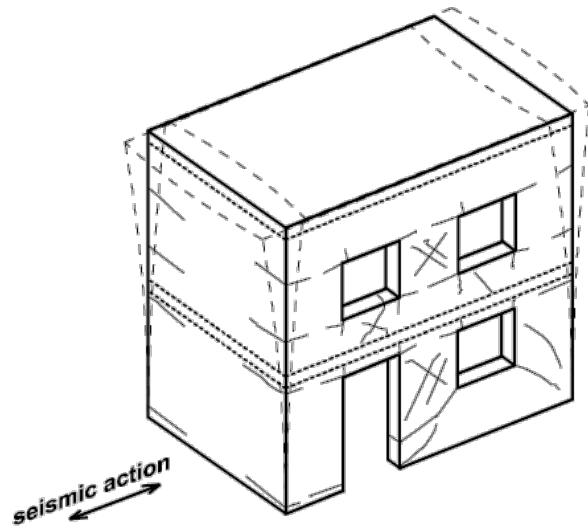
Out-of- plane mechanisms



**Out-of-plane mechanisms have to be verified separately
through suitable analytical methods**



Structural Element Model – *Basics*



MASONRY PANEL TYPE:

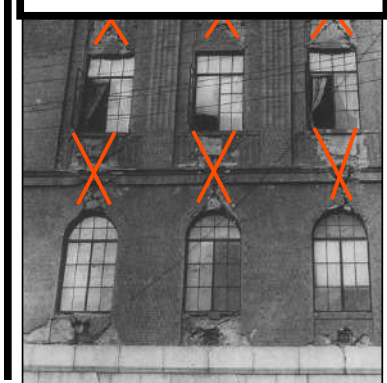
-  Joint panel
-  Spandrel
-  Pier



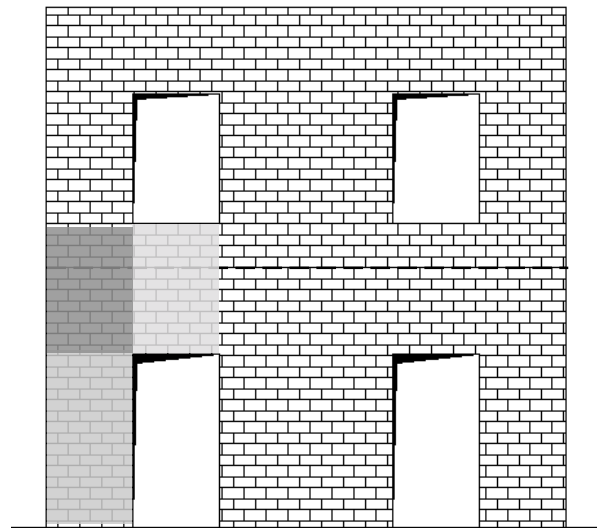
PIERS



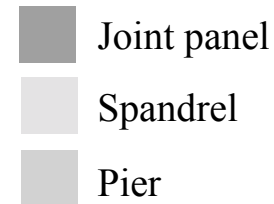
SPANDRELS



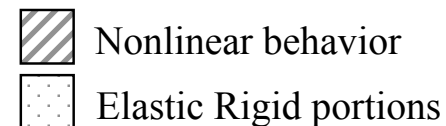
Structural Element Model – *Basics*



MASONRY PANEL TYPE:



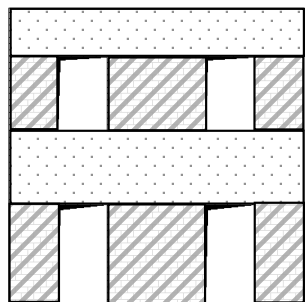
MODELLING ASSUMPTION:



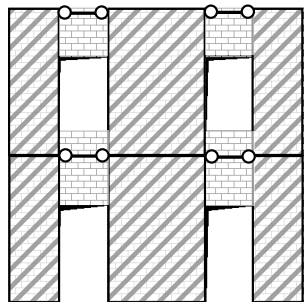
SIMPLIFIED MODELS

	<i>Joint</i>	<i>Pier</i>	<i>Spandrel</i>
<i>Stiffness</i>	☐	☒	☐
<i>Non linearity</i>	☐	☒	☐

SSWP

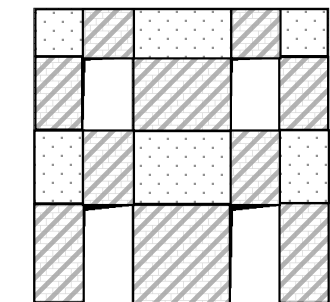


WSSP



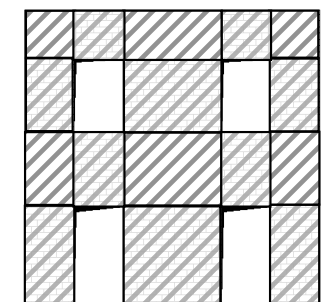
EQUIVALENT FRAME MODELS

	<i>Joint</i>	<i>Pier</i>	<i>Spandrel</i>
<i>Stiffness</i>	☐	☒	☒
<i>Non linearity</i>	☐	☒	☒



HYBRID MODELS

	<i>Joint</i>	<i>Pier</i>	<i>Spandrel</i>
<i>Stiffness</i>	☒	☒	☒
<i>Non linearity</i>	☒	☒	☒



STRONG SPANDREL- WEAK PIER /
WEAK SPANDREL-STRONG PIER

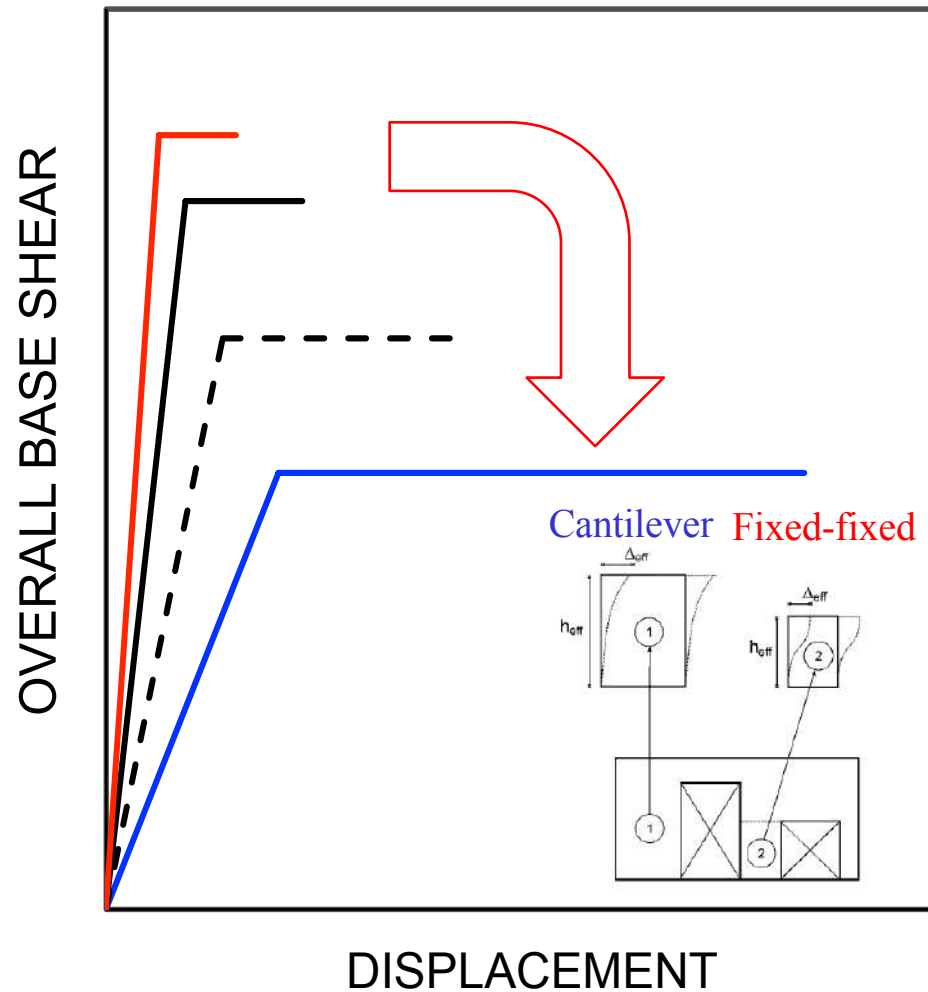
FEMA 306 – ASCE 41/13 – POR
METHOD (Tomazevic 1978)

e.g. Tremuri (Lagomarsino et al. 2013) ,
SAM (Magenes and Della Fontana
1998),easily implementable in purposes
software packages

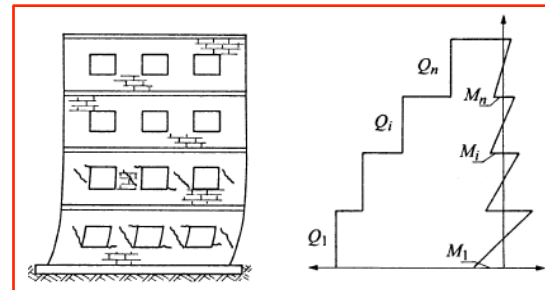
e.g. 3D Macro (Caliò et al. 2012),
D'Asdia and Viskovic (1995), Vanin and
Foraboschi (2009), Braga et al. (1998)

Equivalent Frame Model – *Basics*

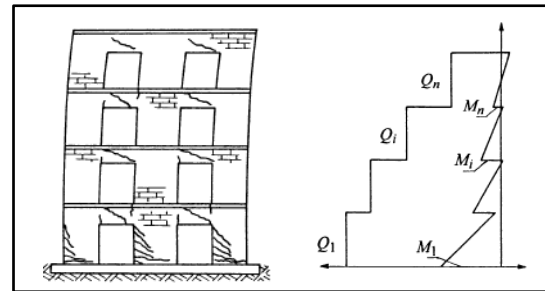
Equivalent frame model *versus* simplified analytical mechanical-based models



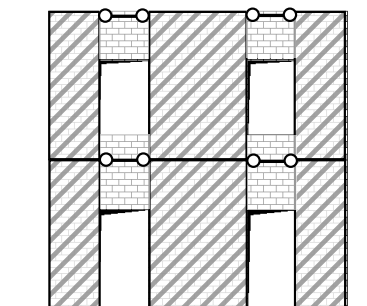
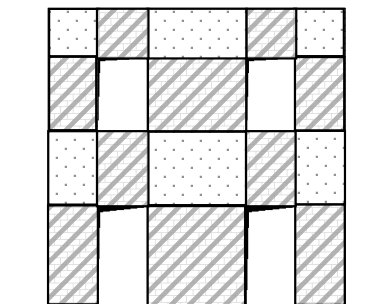
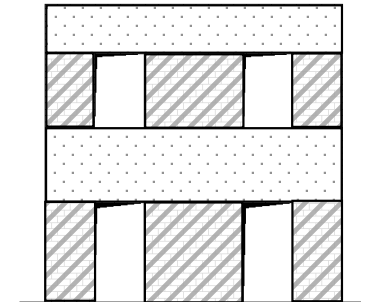
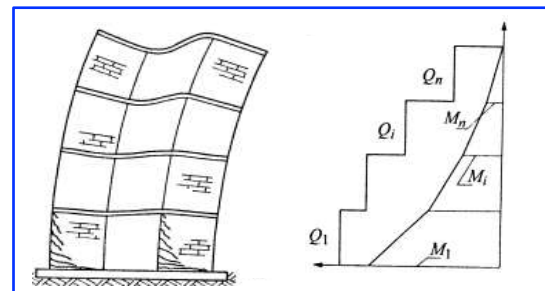
SSWP



EF

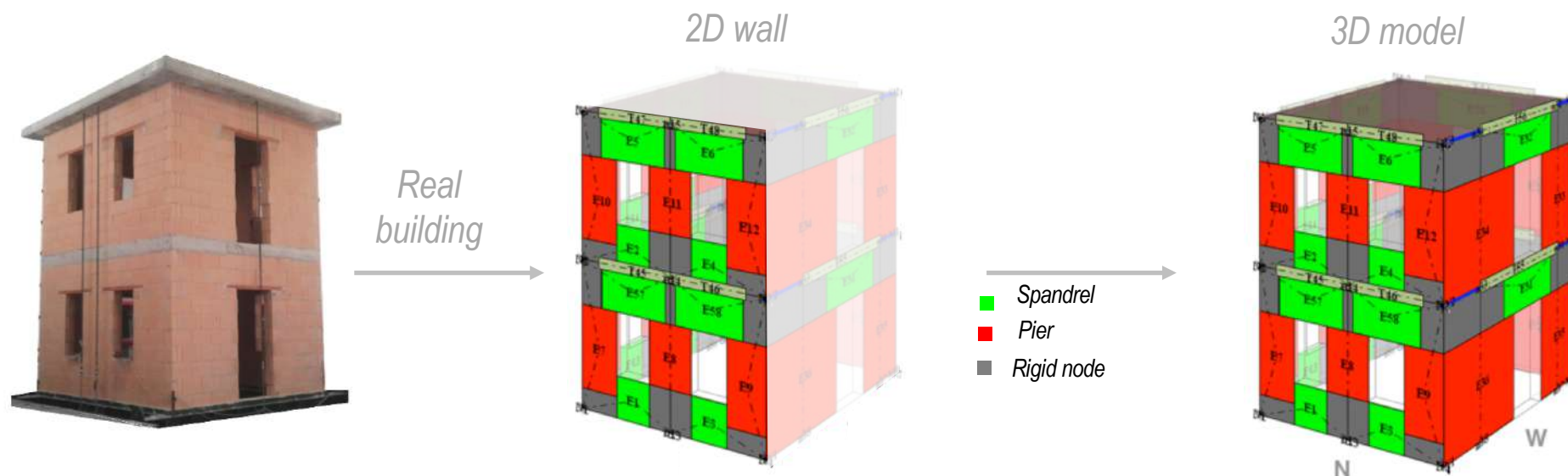


WSSP



Equivalent Frame Model – *Basics*

From the **2D modelling of walls** to the **3D modelling of buildings**



The walls are the bearing elements, while diaphragms are the elements governing the sharing of horizontal actions among the walls.

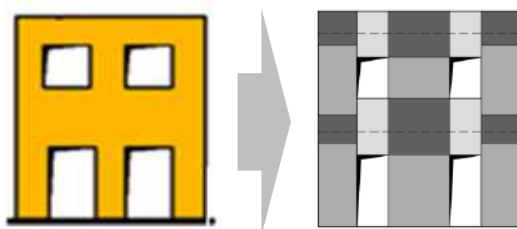
In **MOST** cases the flexural behaviour of the diaphragms and **OFTEN** the wall out-of-plane response are not computed because they are considered negligible with respect to the global building response, which is governed by their in-plane behaviour.

The **MAIN ROLE of diaphragms** is to redistribute and transfer the horizontal force among the walls, both in linear and nonlinear phases

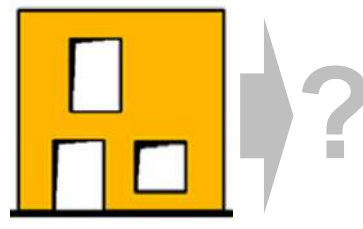
Equivalent Frame Model – *Tricky issues*

2D

Equivalent frame idealization of walls



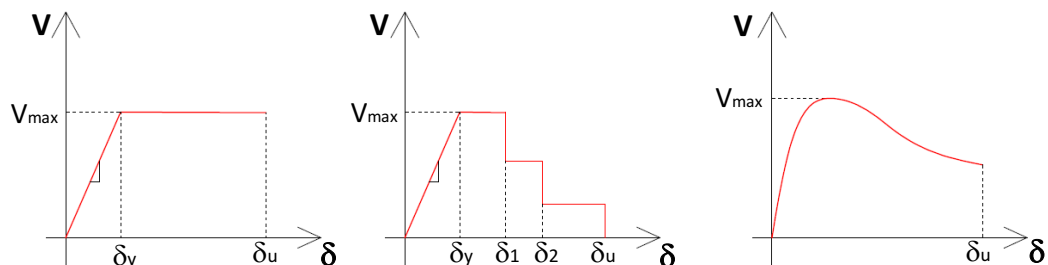
Regular wall



Irregular wall

Constitutive models adopted for masonry panels

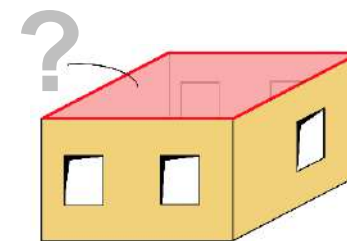
- Strength criteria to simulate failure criteria
- Backbone curve
- Flexibility in differentiating the behavior of spandrels and piers



Possibility of modelling other NON linear elements

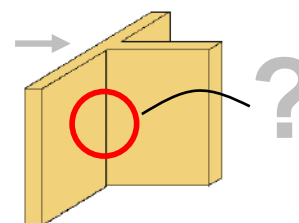
3D

Modelling of diaphragms



- Rigid / Stiff / flexible
- Equivalent stiffness

Connection between orthogonal walls

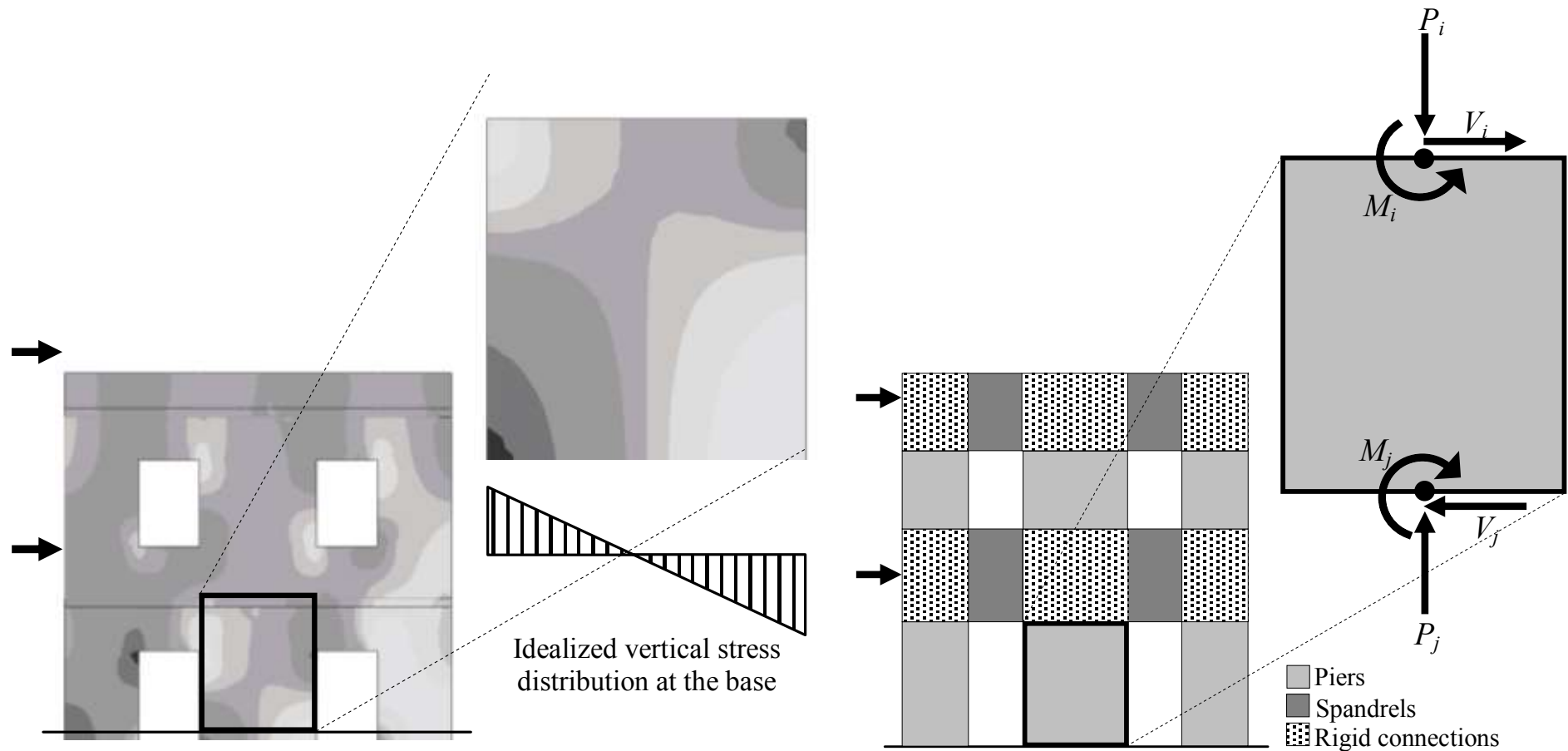


Flange effect

It consists in properly simulating both:

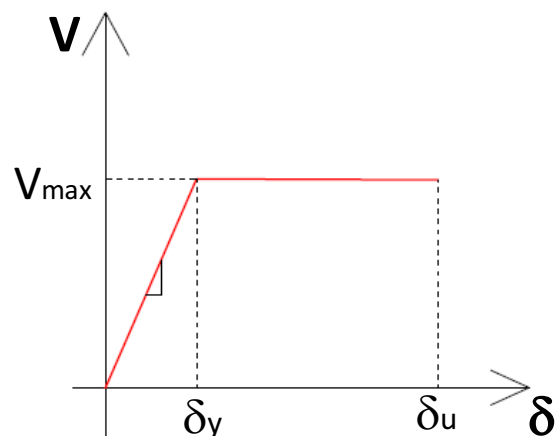
- the wall-to-wall connection quality
- the actual length of the orthogonal pier where it can occur a redistribution of the stress

2D Issues: Constitutive models adopted for URM panels

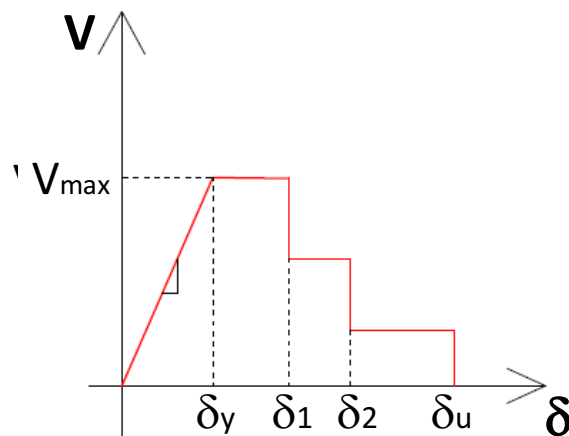


REF: Calderini C., Cattari S., Lagomarsino S. (2009) In-plane strength of unreinforced masonry piers, *Earthquake Engineering and Structural Dynamics*, 38(2), pp. 243-267

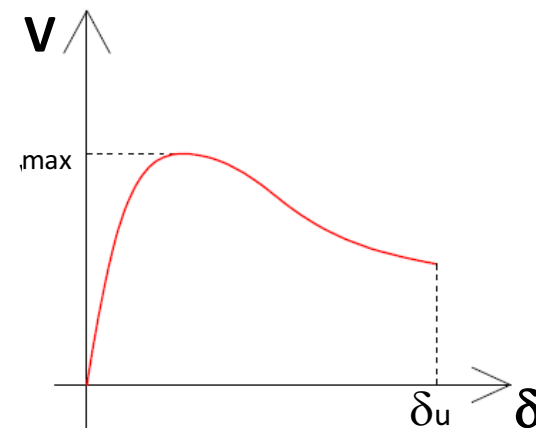
2D Issues: Constitutive models adopted for URM panels



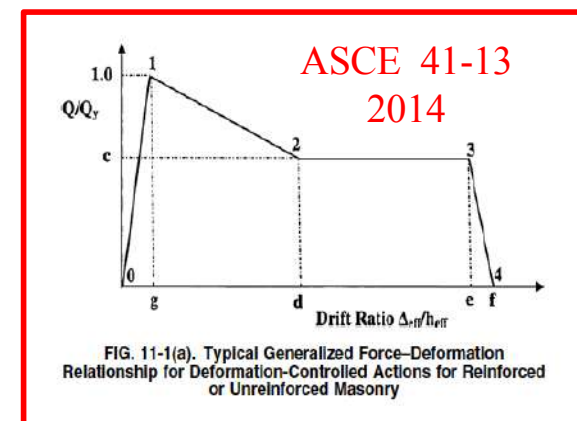
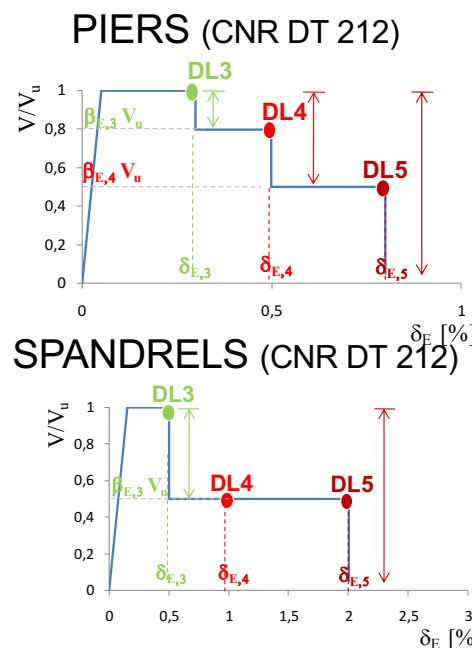
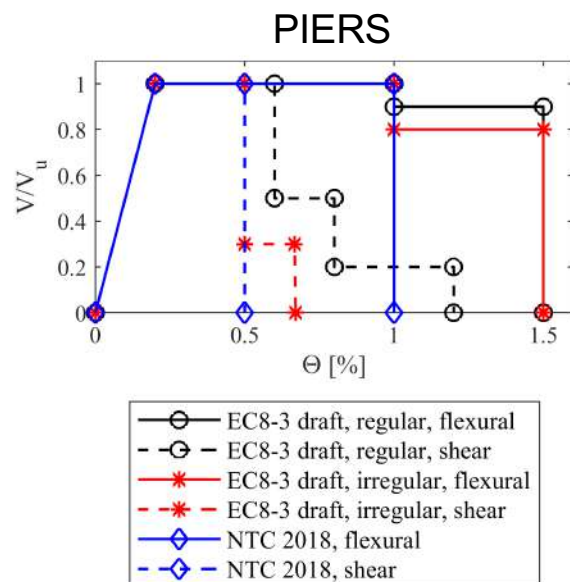
- Italian Structural Code (NTC 2018; MIT 2019)
- Eurocode 8-3



- CNR DT 212 (2013)
- Eurocode 8-3 (updating under review)



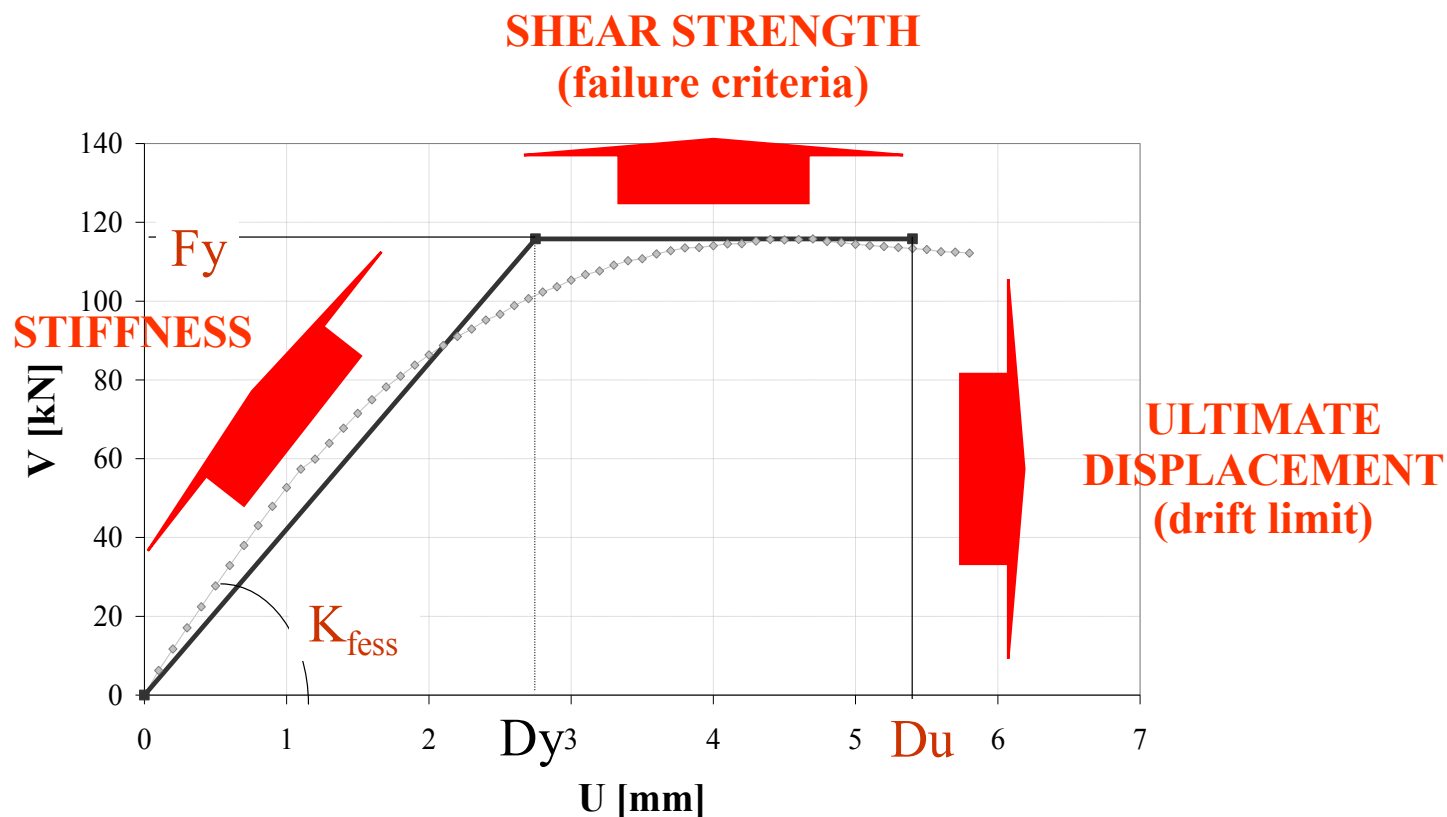
- More accurate macroelements



2D Issues: Constitutive models adopted for URM panels

Bilinear relationship

- The force-displacement curve in shear is modelled by a bilinear model, defined by three parameters.
- Different failure modes can occur: *Rocking* and *Crushing* (flexural behaviour); *Sliding* and *Diagonal Cracking* (shear behaviour).
- After collapse, the element contribution to the equivalent frame is only related to its capacity of bearing axial loads.



2D Issues: Constitutive models adopted for URM panels

■ Shear strength for masonry piers

Failure criteria for masonry piers are based on the approximate evaluation of the local (or mean) stress state induced by the applied forces on predefined points (or sections) of the panel, to be compared with proper limit strength domain for the constituent material (and the panel itself)

■ FLEXURAL BEHAVIOUR

Failure modes: *Rocking* and/or *Crushing*

$$M_u = \frac{Nl}{0.425f_m} \left(1 - \frac{N}{lt} \right)$$

■ SHEAR BEHAVIOUR – PRINCIPAL STRESS MODELS

Failure modes: *Diagonal Cracking*

$$(Turnsek \text{ and } Cacovic, 1971) \quad T_u = lt \frac{f_t}{b} \sqrt{1 + \frac{N}{f_t lt}}$$

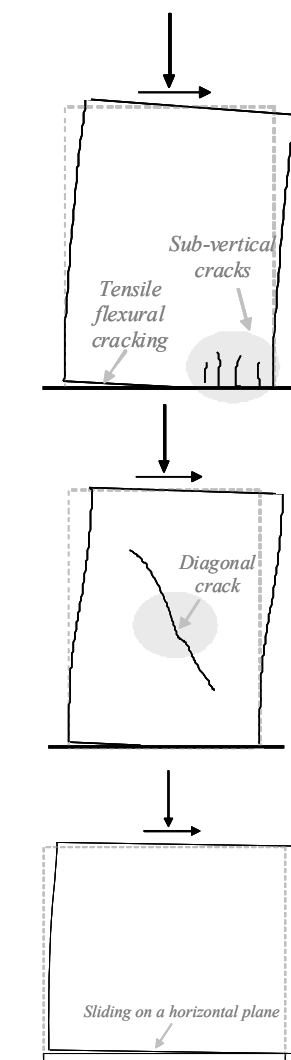
$b = f$ (slenderness of the panel)

■ SHEAR BEHAVIOUR – COULOMB TYPE MODELS

Failure modes: *Bed Joint Sliding* – *Diagonal Cracking through Joints*

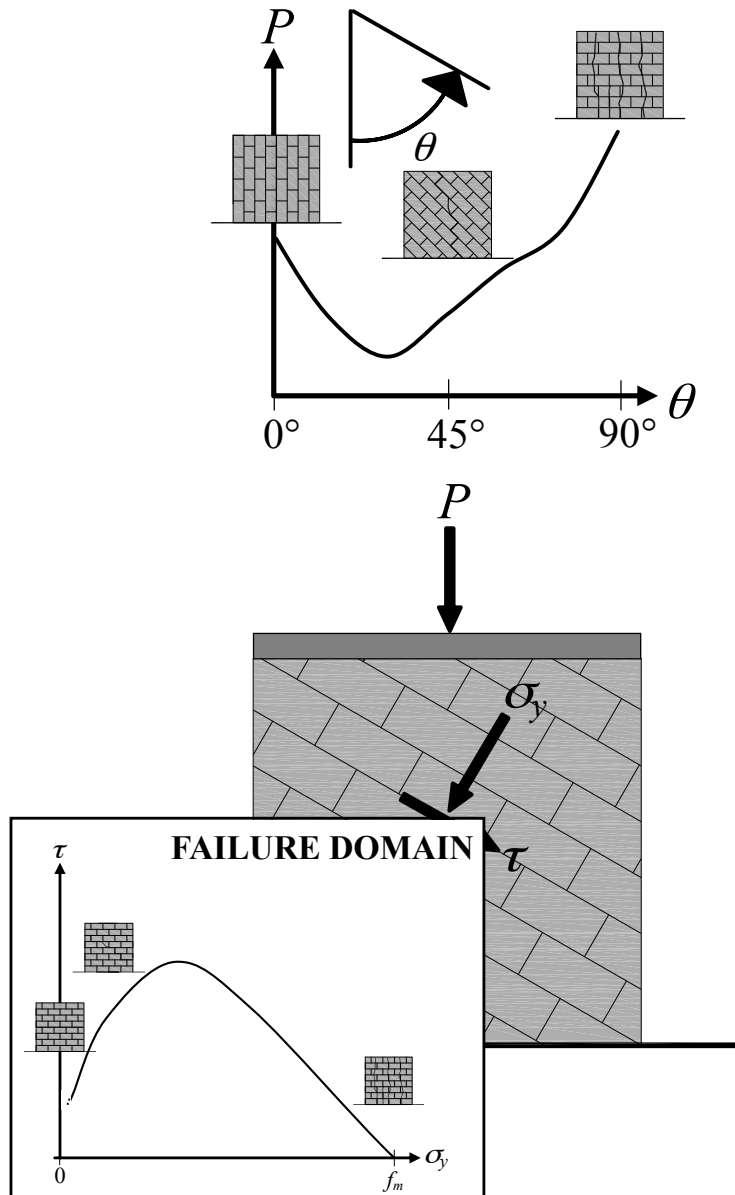
$$T_u = l'tc + \mu N$$

$$T_u = \frac{lt}{b} (\tilde{c} + \tilde{\mu} N)$$

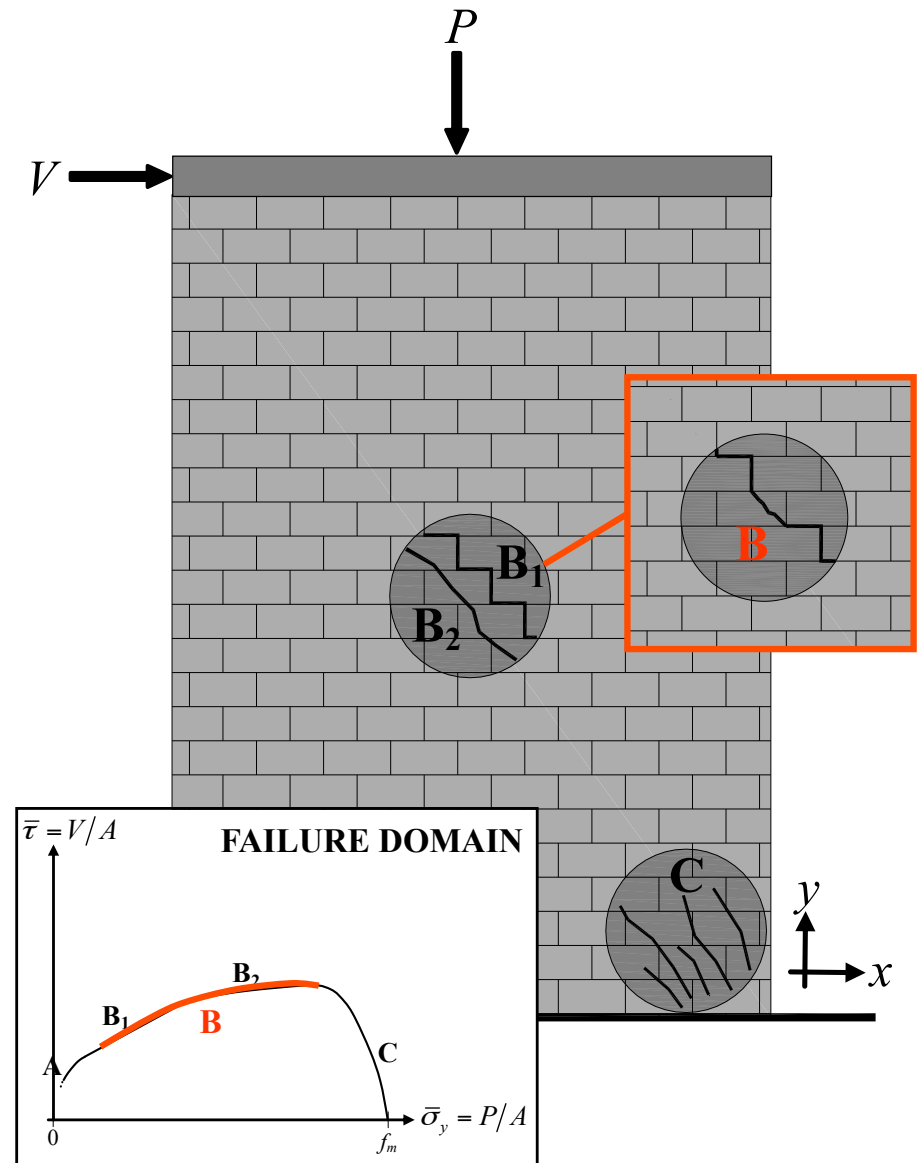


2D Issues: Constitutive models adopted for URM panels

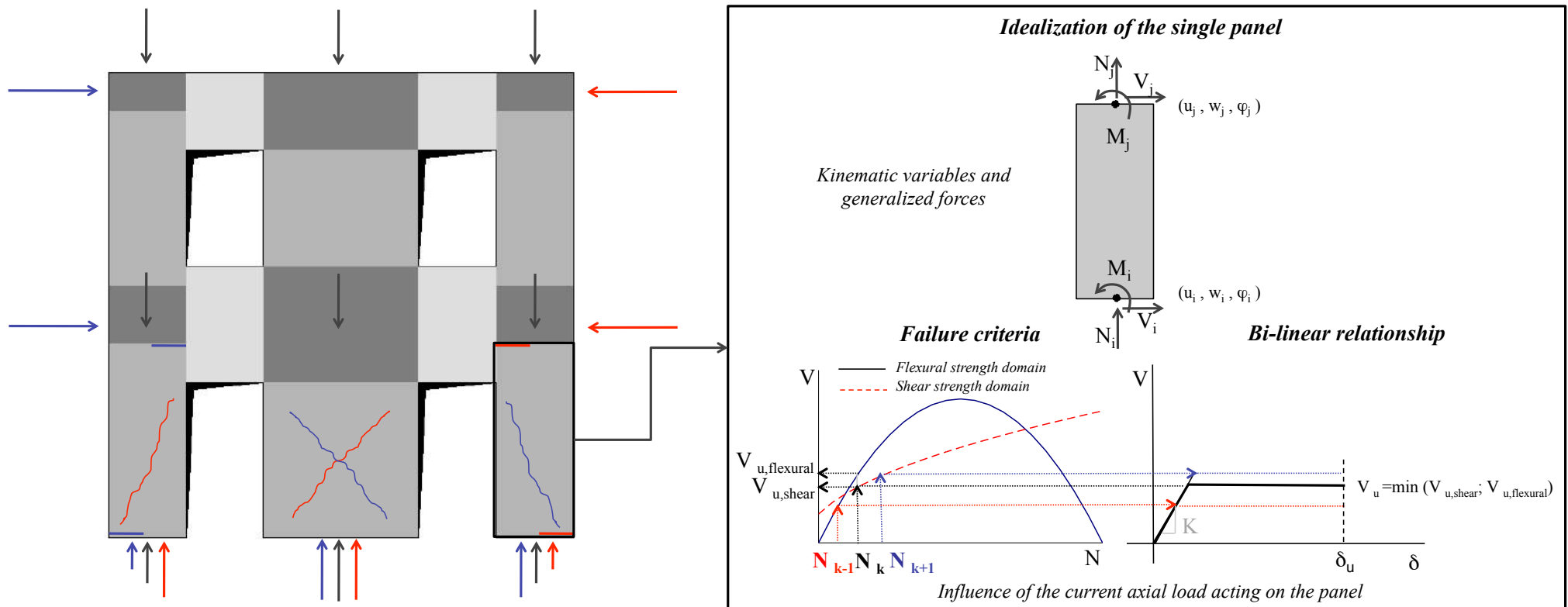
HOMOGENEOUS STRESS STATES



NON-HOMOGENEOUS STRESS STATES



2D Issues: Constitutive models adopted for URM panels



REF:Lagomarsino S, Penna A, Galasco A, Cattari S. (2013) TREMURI program: an equivalent frame model for the nonlinear seismic analysis of masonry buildings, *Engineering Structures*, 56, pp. 1787-1799, Elsevier, ISSN: 0141-0296

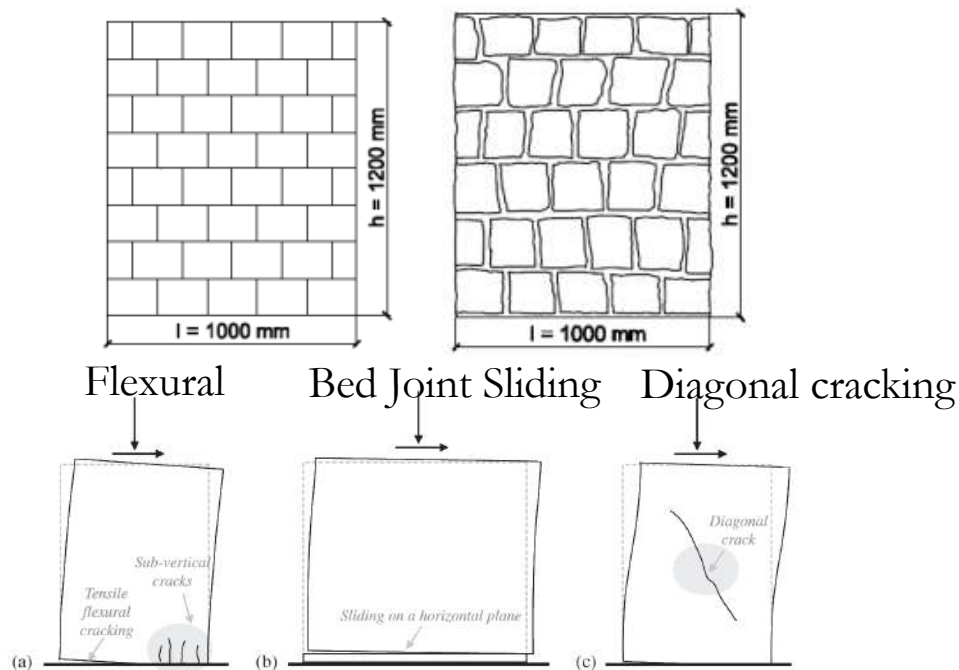
2D Issues: Constitutive models adopted for URM panels

Strength criteria for piers – Trends of recent codes

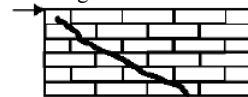
Distinction between REGULAR and IRREGULAR masonry

REGULAR masonry

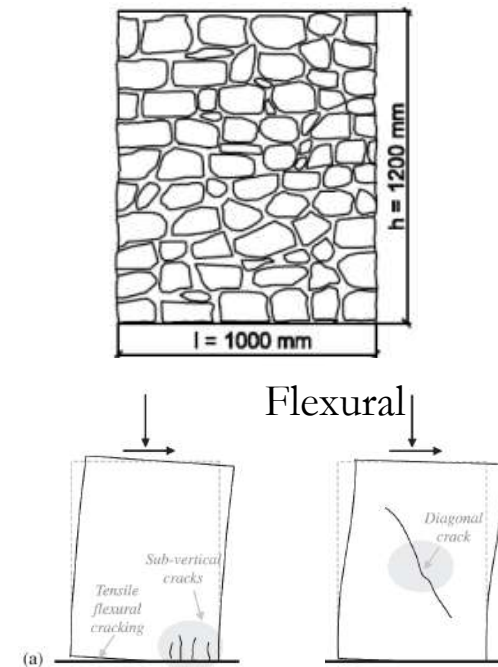
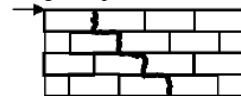
IRREGULAR masonry



1) Lesione passante tra giunti e blocchi



2) Lesione a scaletta sui giunti princ. e second.



Masonry assumed as isotropic material

2D Issues: Constitutive models adopted for URM panels

Strength criteria for piers

	NTC 2018	Eurocode 8 (draft)
	Rocking	
Regular and irregular masonry	$M_u = \frac{l^2 t \sigma_0}{2} \left(1 - \frac{\sigma_0}{0.85 f_d} \right)$	$V_f = \frac{l N}{2 h_0} (1 - 1.15 \nu)$
	Diagonal shear ⁽¹⁾	
<u>Regular masonry</u> (Mann & Müller)	$V_d = \frac{lt}{b} \left(\frac{f_{v0}}{1 + \mu_j \phi} + \frac{\mu_j}{1 + \mu_j \phi} \sigma_0 \right) \leq V_{d,lim}$ $V_{d,lim} = \frac{lt}{b} \frac{f_{bt}}{2.3} \sqrt{1 + \frac{\sigma_0}{f_{bt}}}$	
<u>Irregular masonry</u> (Turnšek & Čaćović)	$V_d = \frac{lt}{b} f_t \sqrt{1 + \frac{\sigma_0}{f_t}}$	
	Shear sliding	
Regular masonry	$V_s = l' t f_{vd} = l' t (f_{v0d} + \mu \sigma_0)$	$V_s = l' t \left(f_{v0} + \frac{\mu N}{l' t} \right) \leq V_{s,units}$

⁽¹⁾ for the Eurocode 8, the Italian code uses the design parameters f_{btd} , f_{td} , f_{v0d} rather than f_{bt} , f_t , f_{v0} .

2D Issues: Constitutive models adopted for URM panels

Strength criteria for spandrels

	NTC 2018	Eurocode 8 (draft)
	Flexural mechanism ⁽¹⁾	
Regular and irregular masonry	$M_u = N_{sd} \frac{h}{2} \left[1 - \frac{N_{sd}}{0.85 f_{hd} h t} \right]$ $V_f = \frac{2M_u}{l}$	$V_{f,u} = 1.15 \frac{h^2 t}{6 h_0} f_{ht}$ $V_{f,s} = \frac{h^2 t}{2 h_0 (1 + f_{ht}/f_h)} f_{ht}$ $V_{f,d} = \frac{h N_s}{h} \left(1 - 1.15 \frac{N_s}{l t f_h} \right)$
	Shear mechanism ⁽²⁾	
Regular masonry	$V_d = \frac{h t}{b} \left(\frac{f_{v0}}{1 + \mu_j \phi} + \frac{\mu_j}{1 + \mu_j \phi} \sigma_0 \right) \leq V_{d,lim}$ $V_{d,lim} = \frac{h t}{b} \frac{f_{bt}}{2.3} \sqrt{1 + \frac{\sigma_0}{f_{bt}}}$	
Irregular masonry	$V_d = \frac{h t}{b} f_t \sqrt{1 + \frac{\sigma_0}{f_t}}$	

⁽¹⁾ also Comm (2019) allows to take into account the horizontal tensile strength of masonry, however no close form equation to evaluate the strength are provided;

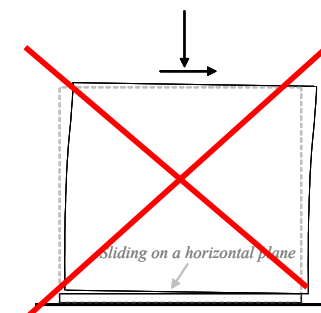
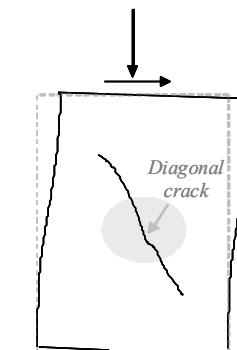
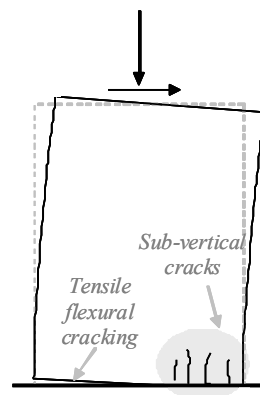
⁽²⁾ for the Eurocode 8, the Italian code uses the design parameters f_{btd} , f_{td} , f_{v0d} rather than f_{bt} , f_t , f_{v0} .

2D Issues: Constitutive models adopted for URM panels

■ Shear strength for masonry spandrels

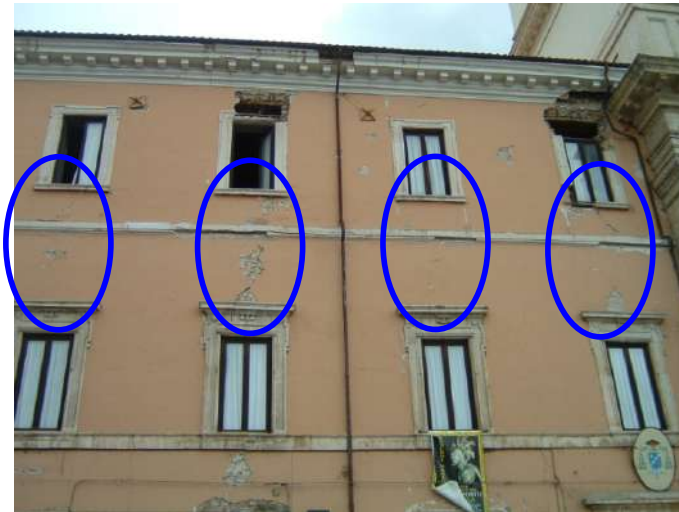


- ❑ DIFFERENT ORIENTATION OF MAIN JOINTS ACTIVATED
- ❑ INTERLOCKING AT THE END SECTION WITH ADJACENT MASONRY PORTIONS
- ❑ LOW AXIAL FORCES
- ❑ INTERACTION WITH LINTEL/ARCHITRAVE TYPE (STEEL/TIMBER BEAMS – FLAT ARCH)



2D Issues: Constitutive models adopted for URM panels

— *Diagonal cracking failure mode*



L'Aquila Earthquake – 6/04/2009

Existing buildings: Due to the moderate value of axial load acting on spandrels or to the lack of tie-rods, if the same criterion proposed for piers for the flexural response is used, **Rocking** tends to prevail on **Diagonal Cracking** much more frequently than that observed in existing buildings after an earthquake



This means that masonry spandrels have a higher flexural strength

2D Issues: Constitutive models adopted for URM panels

✓ **Experimental campaign carried out at the University of Trieste – Gattesco et al. 2008**

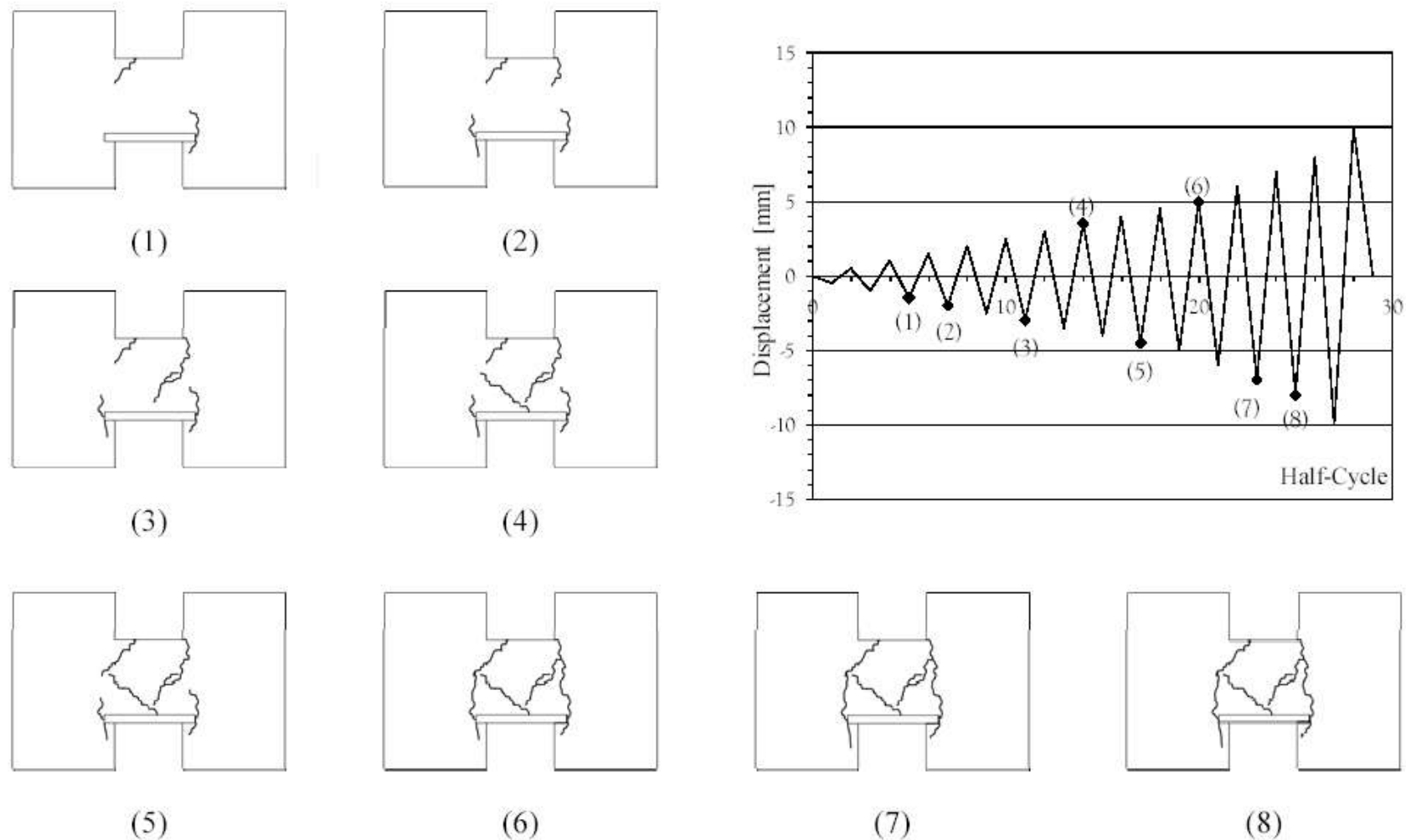
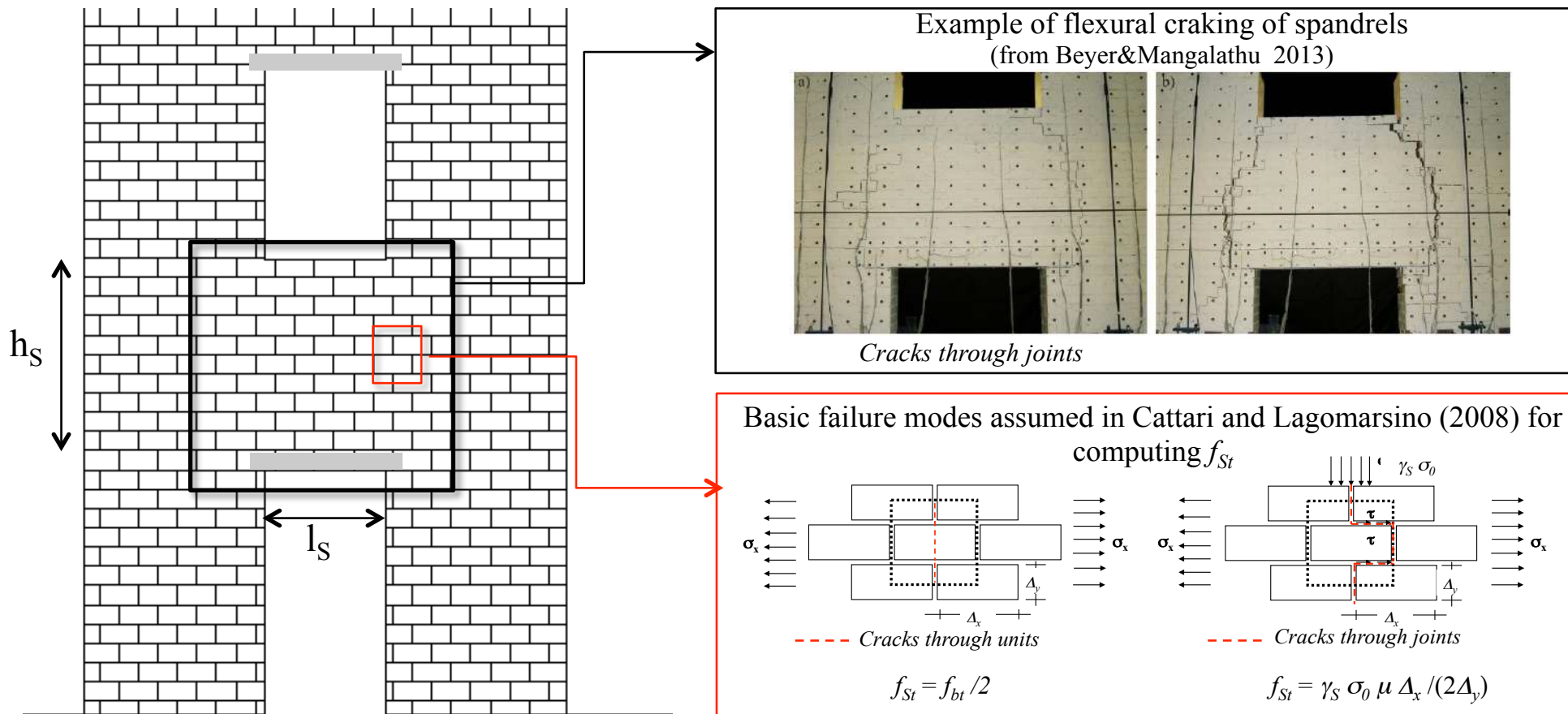


Figure. 7. Sequence of cracks in the spandrel's back face of the specimen MS1.

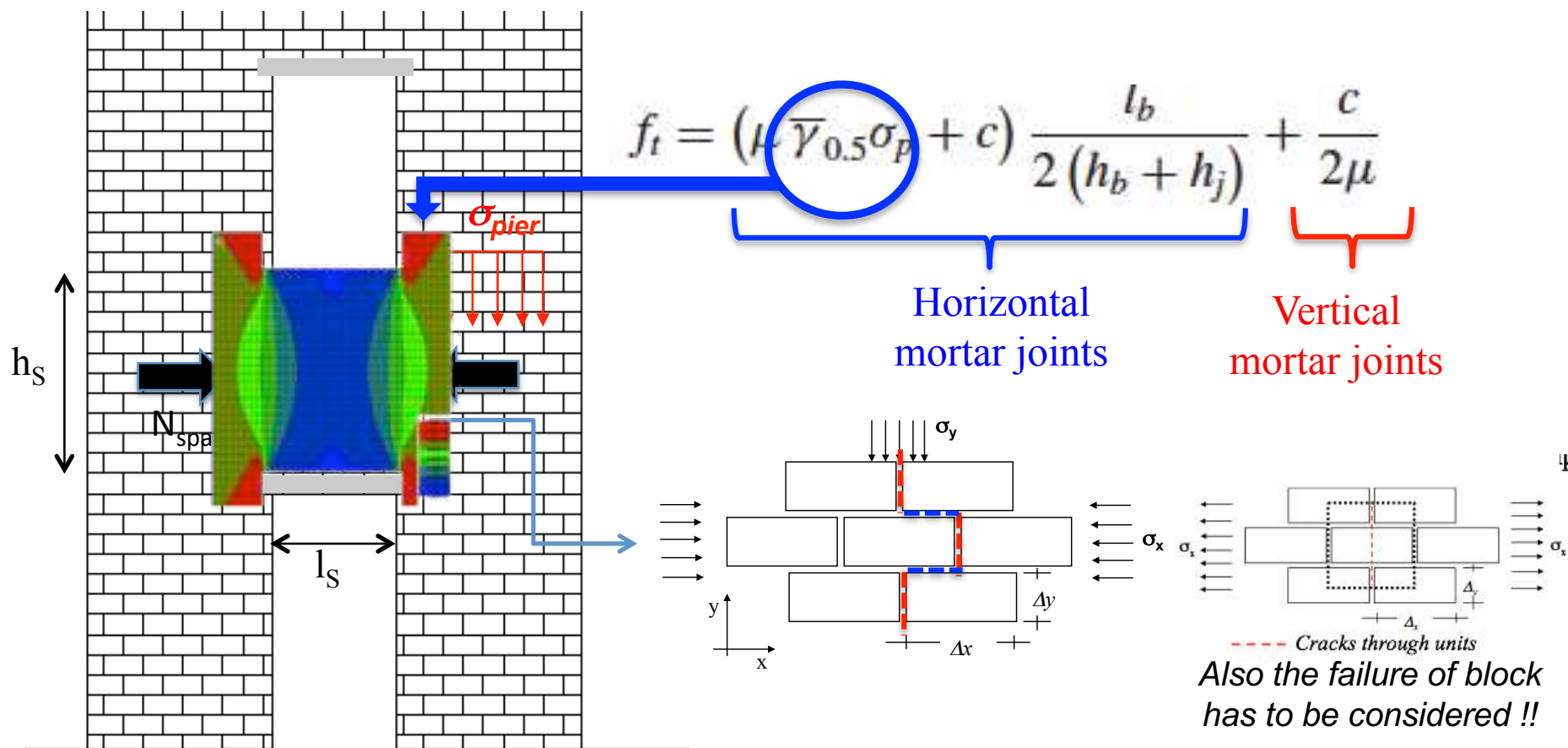
2D Issues: Constitutive models adopted for URM panels

$$f_{ftd} = \min \left(\frac{f_{btd}}{2}; f_{v0d} + \frac{\mu \sigma_y}{\Phi} \right)$$



2D Issues: Constitutive models adopted for URM panels

Thanks to the interlocking phenomena, spandrels may rely on the contribution of an
 “equivalent tensile strength” $f_{t,spandrel}$



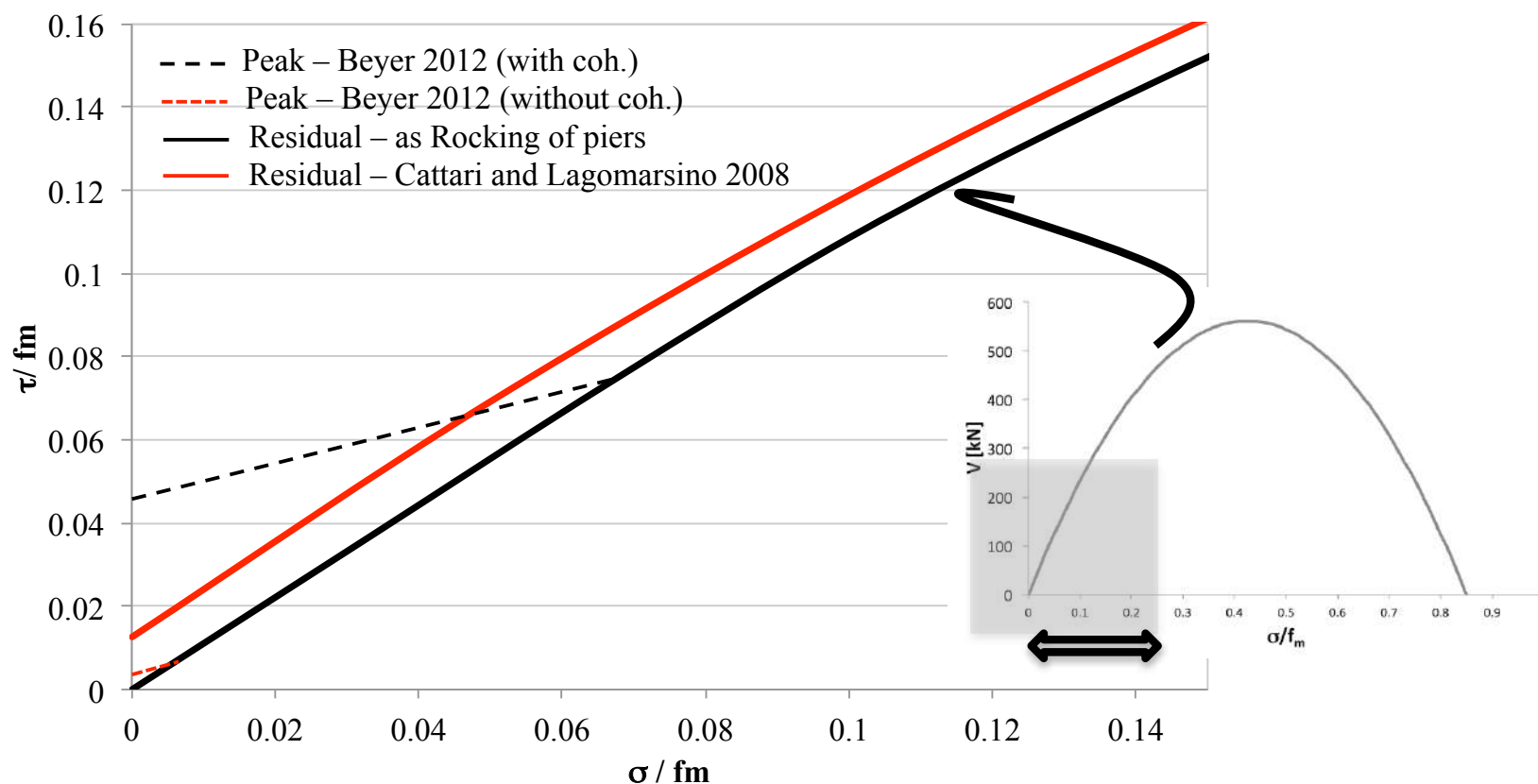
REF : Beyer K., Mangalathu S. 2013. Review of strength models for masonry spandrels. *Bull Earth Eng*, 11. 521–542.

REF. Cattari S., Beyer K. (2015) Influence of spandrel modelling on the seismic assessment of existing masonry buildings, in: Proc. of Tenth Pacific Conference on Earthquake Engineering: Building an Earthquake-Resilient Pacific, 6-8 November 2015, Sydney, Australia, 10 pages.

2D Issues: Constitutive models adopted for URM panels

Different proposals in literature: FEMA 306 1998, Cattari and Lagomarsino 2009, Beyer 2012.

	FEMA 306	Cattari and Lagomarsino 2009	Beyer 2012
$f_{t,sp}$	$f_{p,sj} = 0,5 (0,75c)$ $f_{p,bj} = 0,5(0,75c + \gamma_{sp}\sigma_p)$	f_{tu} $= \min \left(\mu \gamma_{sp} \sigma_p \frac{l_b}{2(h_j + h_b)}; \frac{f_{bt}}{2} \right)$	$f_{bj} = (\mu \gamma_{sp} \sigma_p + c) \frac{l_b}{2(h_b + h_j)}$ $f_{hj} = \frac{c}{2\mu}; f_{t,sp} = f_{bj} + f_{hj}$

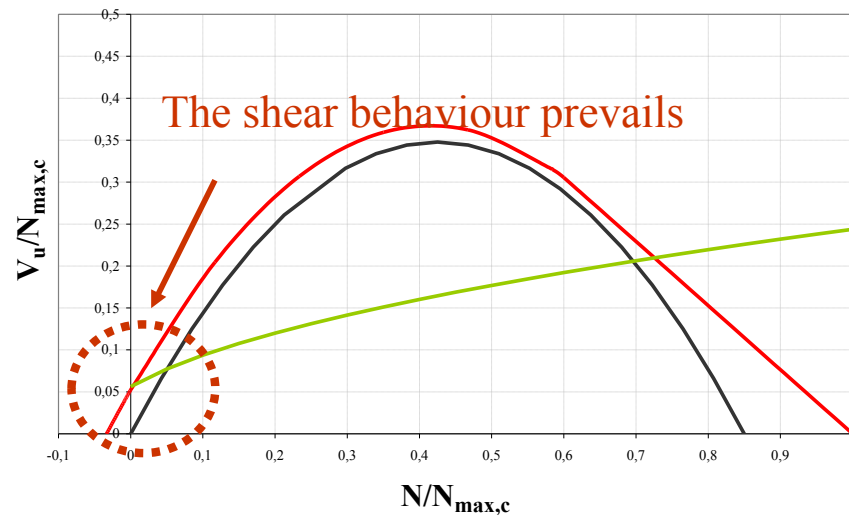


NOW INTRODUCED IN THE ITALIAN STRUCTURAL CODE 2018 & MIT 2019 AND IN EUROCODE 8- PART (DRAFT UNDER REVIEW)

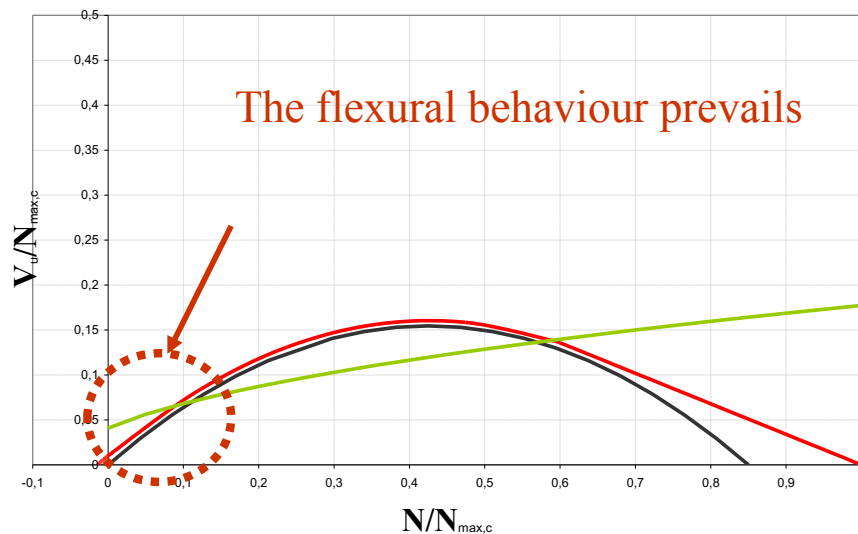
2D Issues: Constitutive models adopted for URM panels

(Cattari and Lagomarsino 2008, in proceeding of 14th WCEE, Beijing).

SPANDREL – INTERMEDIATE FLOOR

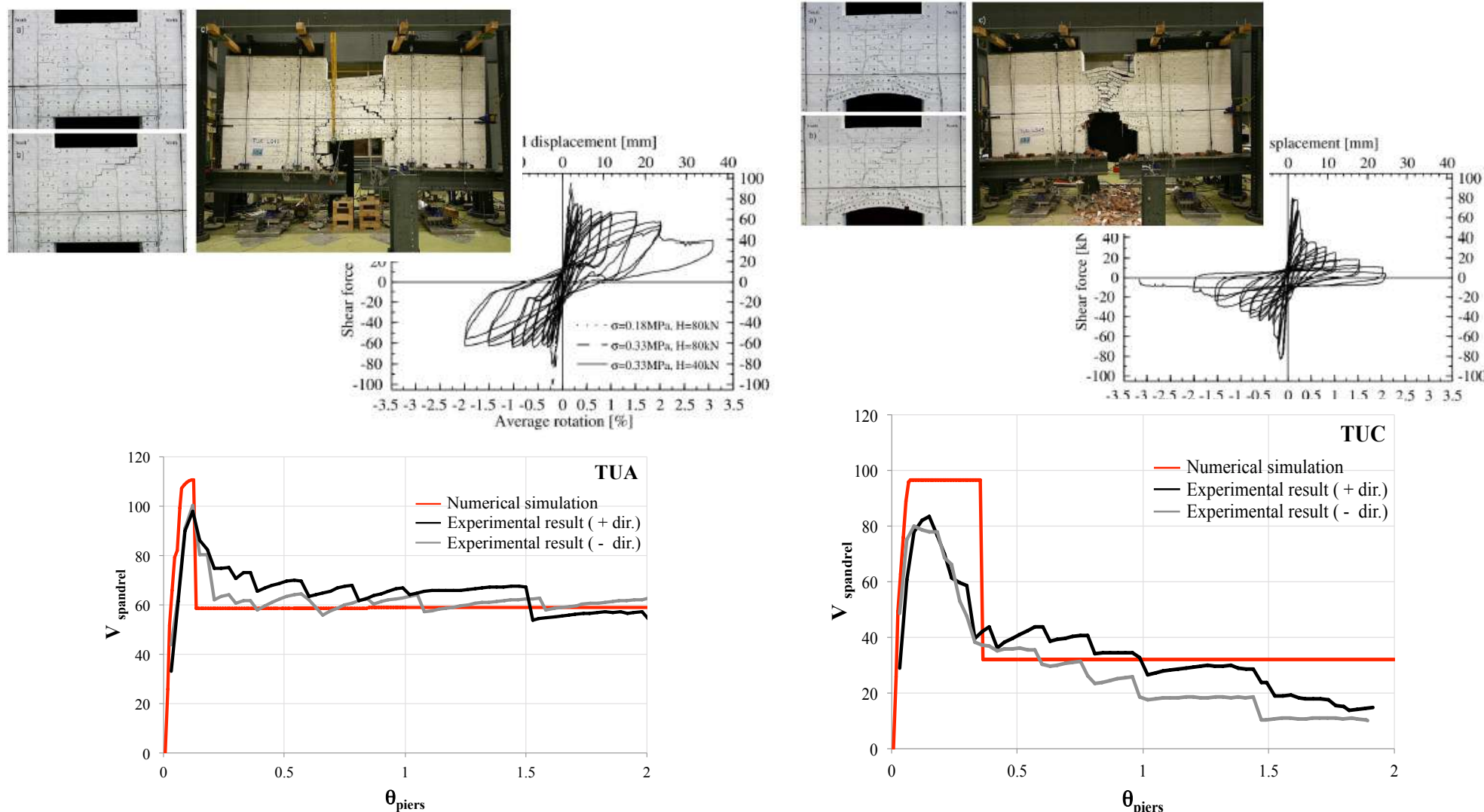


SPANDREL – TOP FLOOR



2D Issues: Constitutive models adopted for URM panels

RESIDUAL STRENGTH OF SPANDREL AS A FUNCTION ALSO OF THE ARCHITRAVE TYPE EXPERIMENTAL RESULTS FROM BEYER&DAZIO 2012 & STRENGTH CRITERIA PROPOSED IN BEYER 2012 (Engineering Structures)

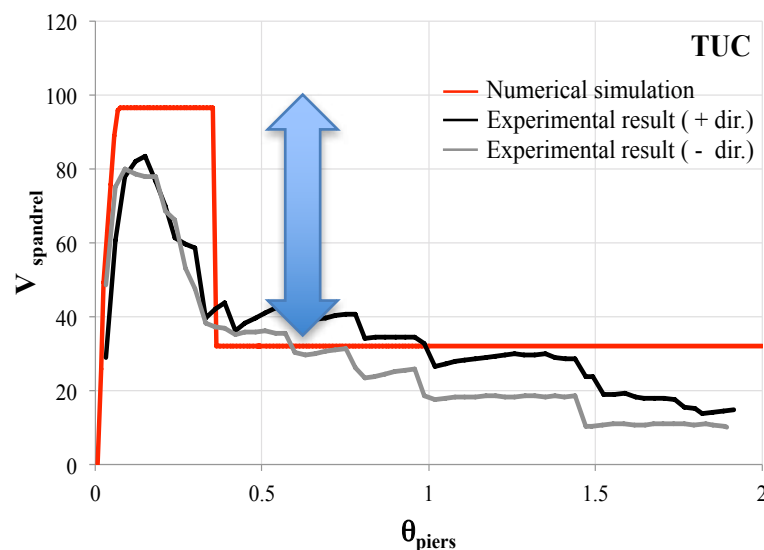
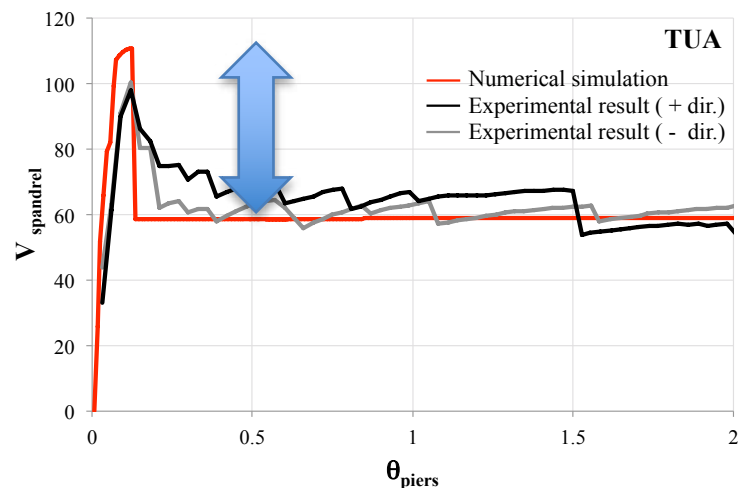


NUMERICAL SIMULATION PROVIDED BY MULTILINEAR BEAM IMPLEMENTED IN TREMURI (Cattari and Beyer 2015, PCEE conference)

2D Issues: Constitutive models adopted for URM panels

SPANDRELS

ITALIAN STRUCTURAL CODE – NTC 2018 & INSTRUCTIONS ISSUED IN 2019



RESIDUAL STRENGTH AS A FUNCTION OF THE LINTEL TYPE

60% when the spandrel is coupled to a r.c.
beam or steel lintel

40% when the spandrel is coupled to a
timber lintel

10% in presence of a flat arch as lintel

HIGHER DRIFT LIMITS THAN PIERS

Ultimate drift equal to 0.015 (increased until
to 0.02 when a tensile resistant element is
coupled to the spandrel)

2D Issues: Constitutive models adopted for URM panels

DEFINITION OF DRIFT THRESHOLDS

REF: CNR DT 212 (2013)

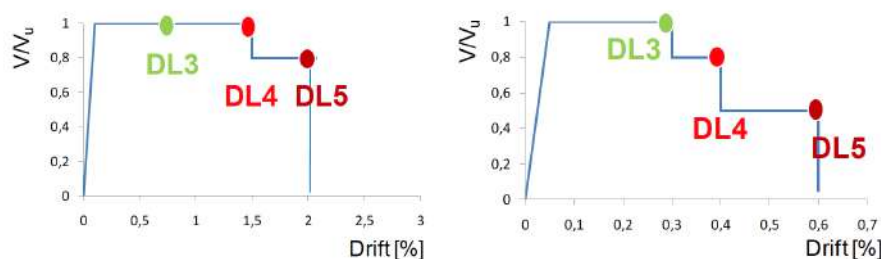


Table 3.2. Indicative intervals for drift values and for the residual resistance for the different states of damage.

	Drift (%)			Residual resistance	
damage	3	4	5	3→4	4→5
normal force and bending	0.4 ÷ 0.8	0.8 ÷ 1.2	1.2 ÷ 1.8	1.0	0.8 ÷ 0.9
shear	0.25 ÷ 0.4	0.4 ÷ 0.6	0.6 ÷ 0.9	0.6 ÷ 0.8	0.25 ÷ 0.6

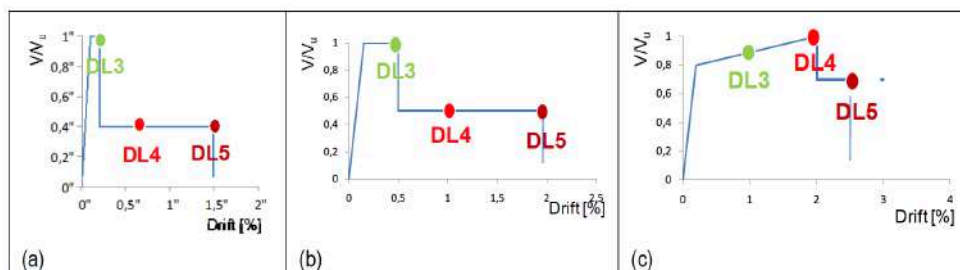


Fig. 3-4. Constitutive drift-shear laws for spandrels supported by: a) a masonry arch; b) a lintel in timber, steel or reinforced concrete; c) a lintel coupled to a tensile-resistant element.

damage	Drift (%)			Residual resistance	
	3	4	5	3→4	4→5
Lintel without tie rod or tie beam	0.40 ÷ 0.60	0.80 ÷ 1.20	1.80 ÷ 2.20	0.40 ÷ 0.60	
Lintel with tie rod or tie beam	0.80 ÷ 1.20	1.60 ÷ 2.00	2.40 ÷ 2.60	1.00	0.60 ÷ 0.80
Arch	0.15 ÷ 0.25	0.45 ÷ 0.75	1.20 ÷ 2.00	0.30 ÷ 0.50	
Arch with Tie rod	0.20 ÷ 0.40	0.50 ÷ 0.80	1.40 ÷ 2.40	1.00	0.40 ÷ 0.60

DATABASE OF EXPERIMENTAL TESTS ONLY FOR PIERS

REF: Vanin et al. (2017, *Bulletin of Earthquake Engineering*)

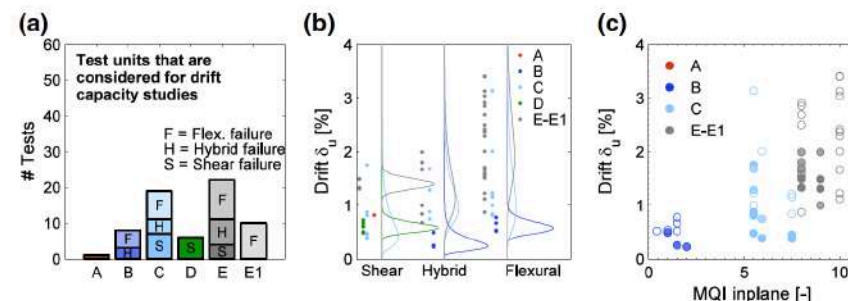


Fig. 15 Distribution of test units considered for drift capacity studies (a). Ultimate drift capacity δ_u as a function of the failure mode (b), and the Masonry Quality Index for in-plane loading (c). Solid markers represent walls failing in shear of a hybrid mode; empty markers walls failing in flexure

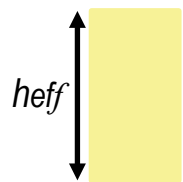
Table 15 Summary of proposed median values and coefficients of variations for stone masonry assessment

MASONRY TYPOLOGIES					
A	B	C	D	E	E1
DISPLACEMENT CAPACITY					
Drift at cracking: $\delta_{cr} = 0.20\%$		Drift at SD limit state: $\delta_{SD} = 0.50 \cdot \delta_u$			
Yielding drift:		Drift at max. force: $\delta_{max} = 0.70 \cdot \delta_u$			
- shear: $\delta_y = 1/4 \cdot \delta_u$		Drift at collapse: $\delta_c = 1.15 \cdot \delta_u$			
- flexure: $\delta_y = 1/6.5 \cdot \delta_u$					
Ultimate drift:		reference values from table			
- Model 1:					
- Model 2:					

ALEATORIC VARIABILITY		Suggested coefficients of variation							
		K_{eff}	V_a	δ_{cr}	δ_y	δ_{SD}	δ_{max}	δ_u	δ_c
A-E1		0.20	0.10	0.10	0.20	0.30	0.30	0.30	-

2D Issues: Equivalent frame idealization of URM walls

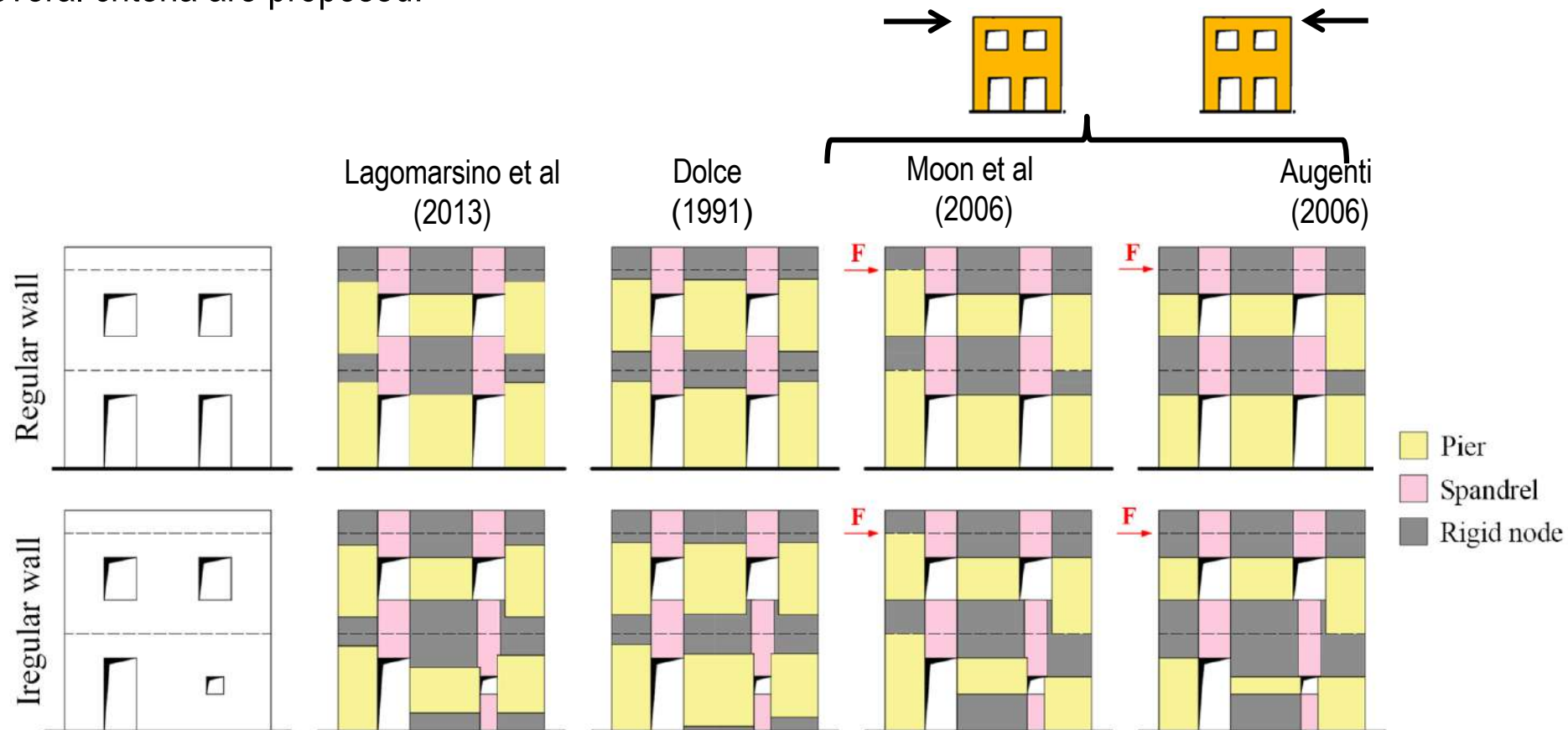
Rules for the identification of the structural elements



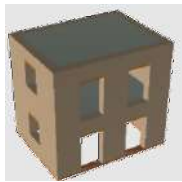
PIERS – Effective height

Several criteria are proposed:

- empirical
- based on limited experimentations
- based on few numerical simulations
- mainly developed for almost regular walls

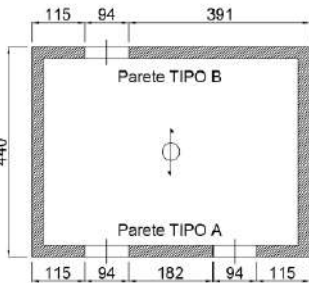
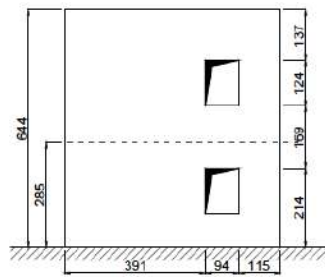


2D Issues: Equivalent frame idealization of URM walls

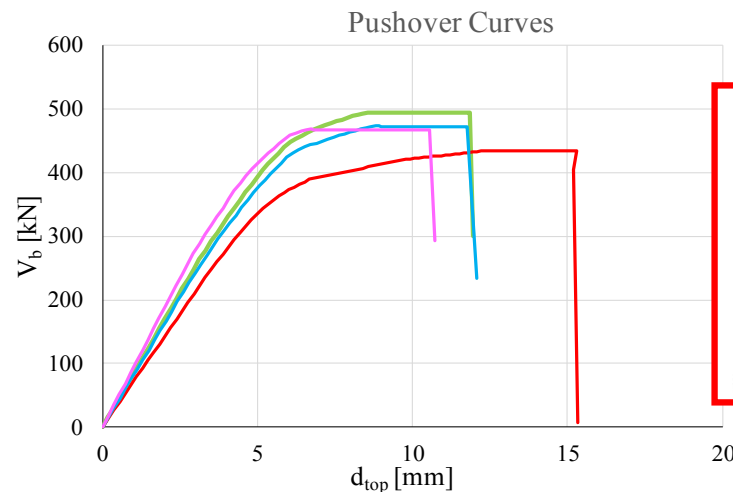
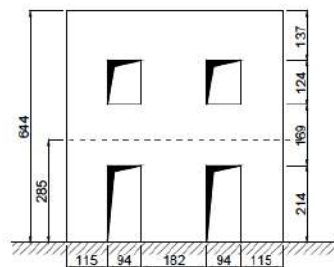


2-STOREY SIMPLE
MASONRY BUILDING

Parete TIPO B

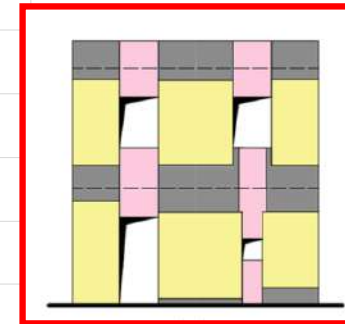


Parete TIPO A

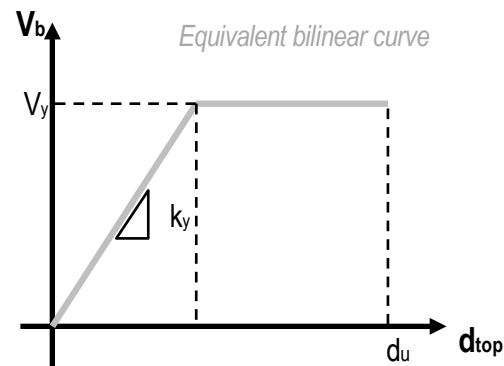
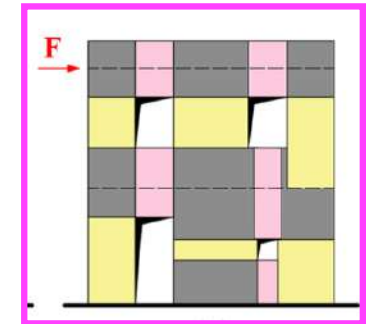


— Augenti (2006) — Moon et al (2006)
— Lagomarsino et al (2013) — Dolce (1991)

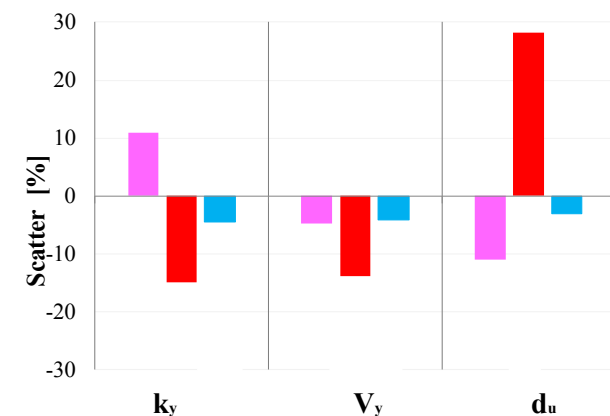
Dolce 1991



Augenti 2006

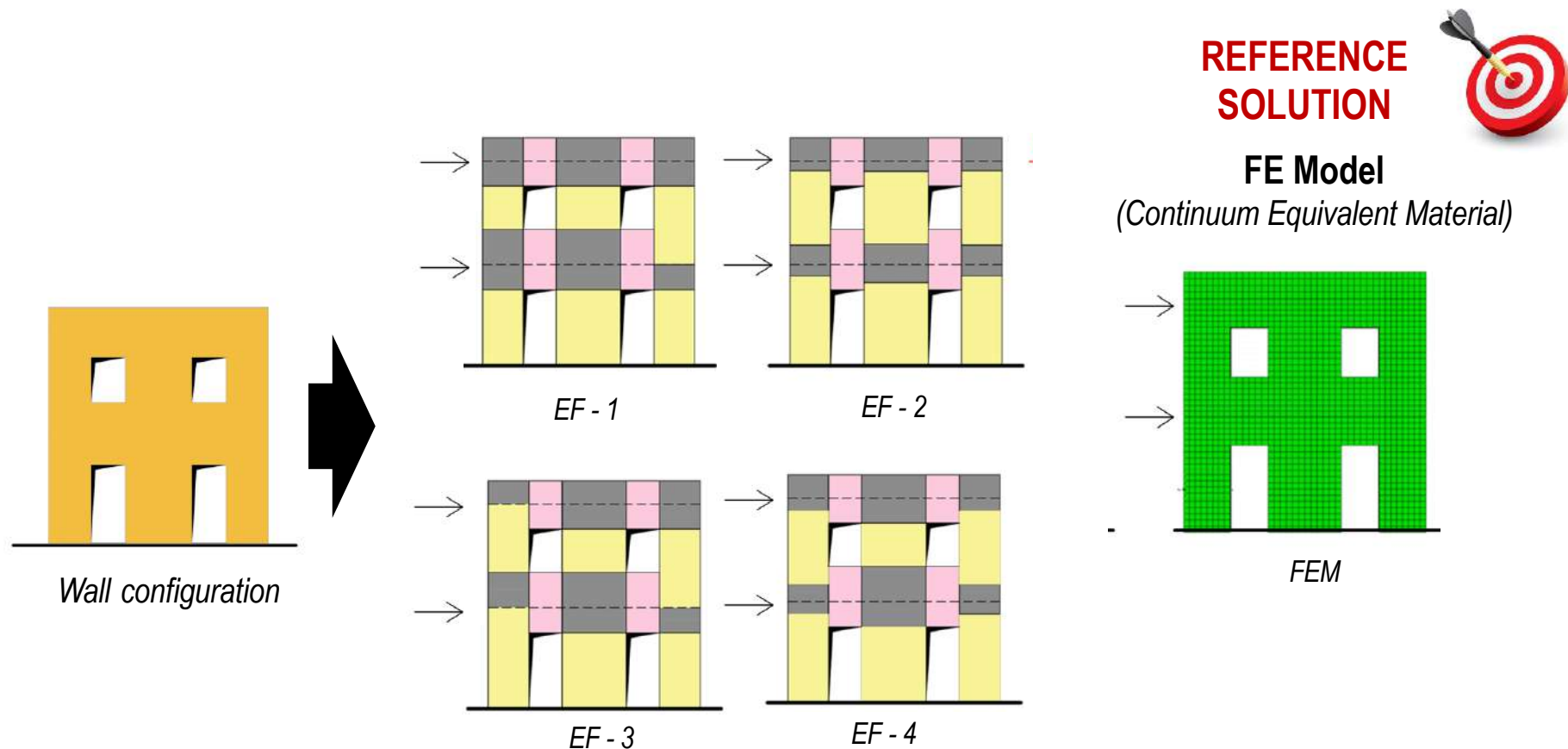


Scatter on V_y , d_u , k_y
(same software, different mesh)



■ Augenti (2006) ■ Dolce (1991) ■ Moon et al (2006)

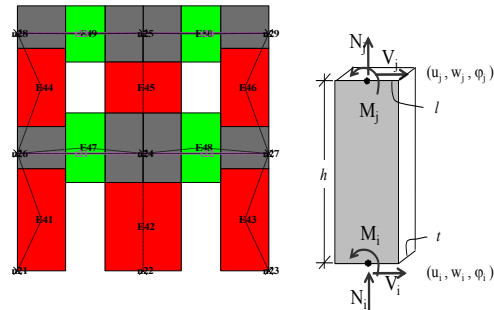
2D Issues: Equivalent frame idealization of URM walls



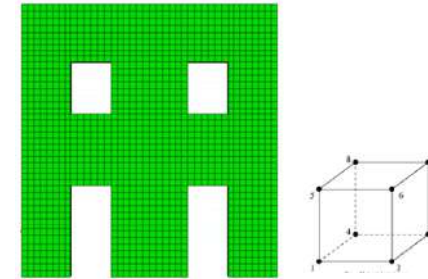
- ❑ PROPER CALIBRATION OF MECHANICAL PARAMETER TO GUARANTEE THE CONSISTENCY
- ❑ COMPARISON OF RESULTS OF STRUCTURAL RESPONSE PARAMETERS AT GLOBAL and LOCAL SCALE

2D Issues: Equivalent frame idealization of URM walls

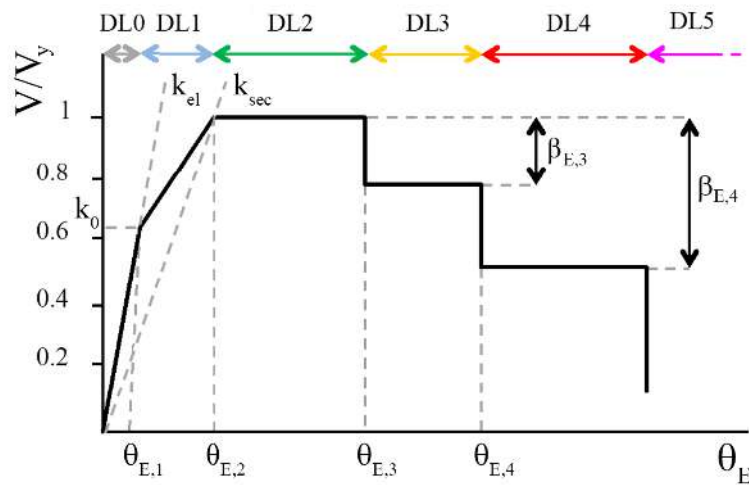
EF Model: Tremuri Research Version



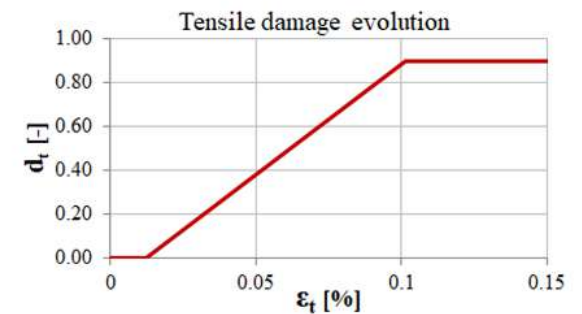
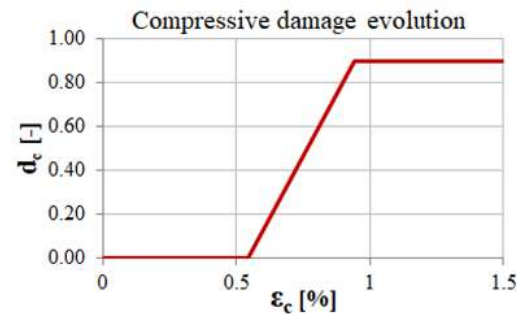
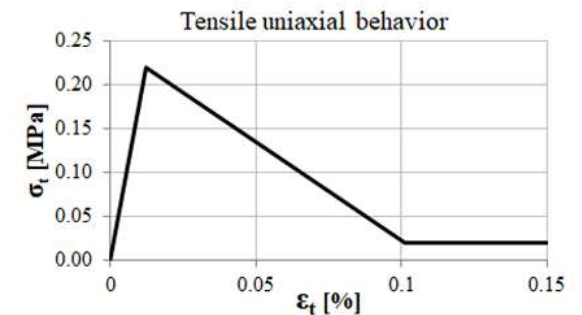
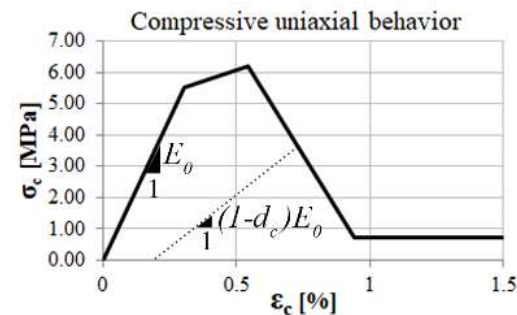
FE Model: Abaqus v.6.14



CONCRETE DAMAGED PLASTICITY Model
(Lubliner et al 1989, Lee and Fenves 1998)

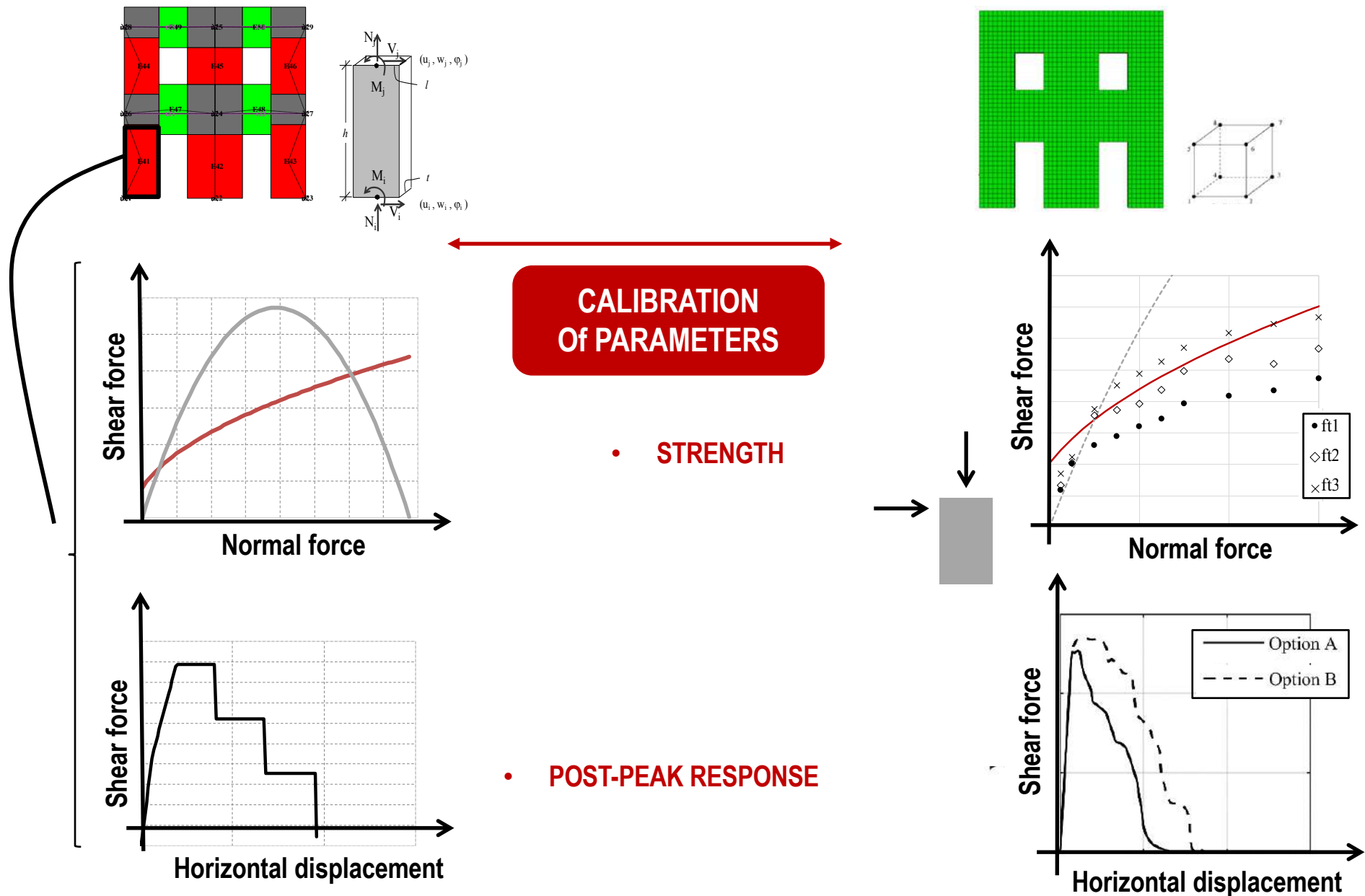


(Cattari and Lagomarsino 2013)

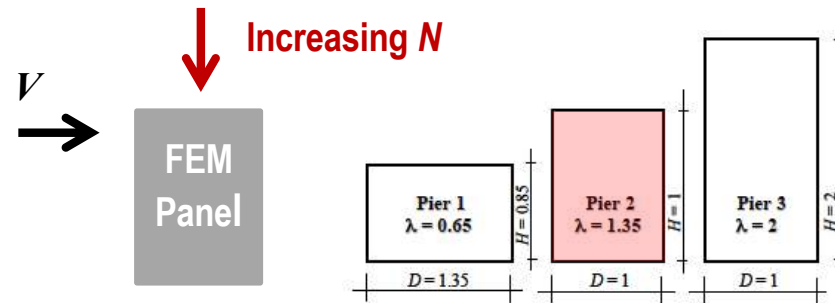


Reference: Camilletti 2019 PhD thesis, University of Genoa

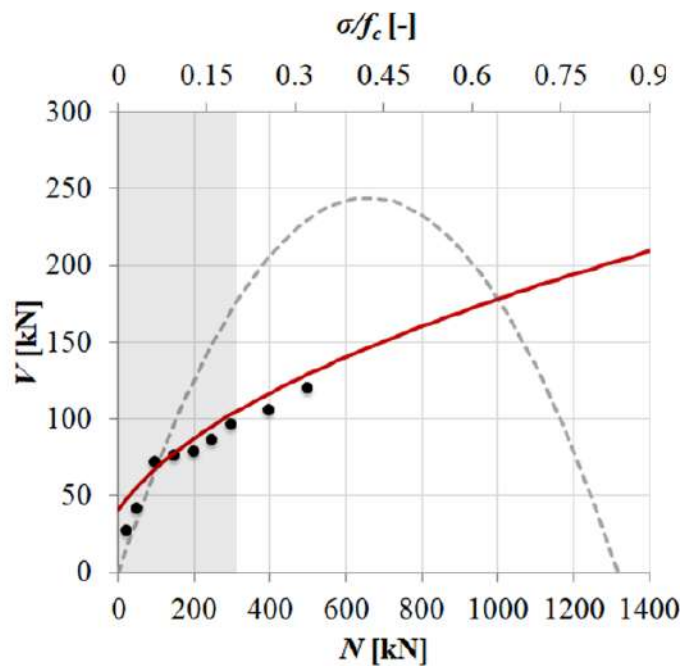
2D Issues: Equivalent frame idealization of URM walls



2D Issues: Equivalent frame idealization of URM walls

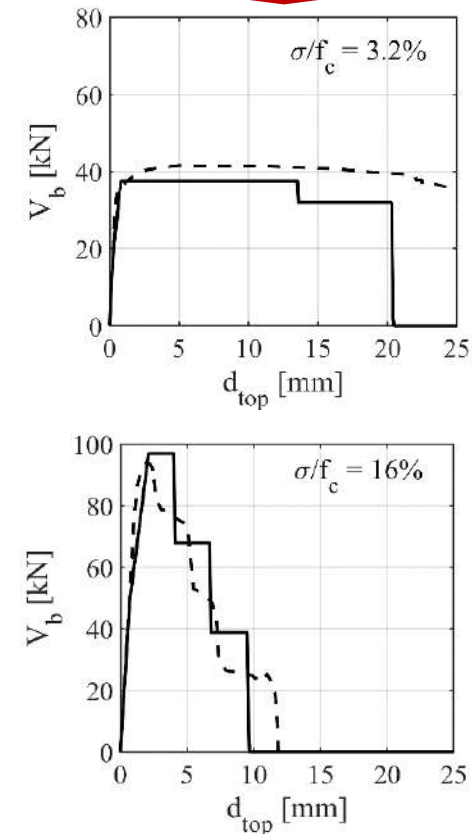


STRENGTH



- V_{u_Shear} failure
- $V_{u_Flexural}$ failure
- $V_{\max}$ ABAQUS

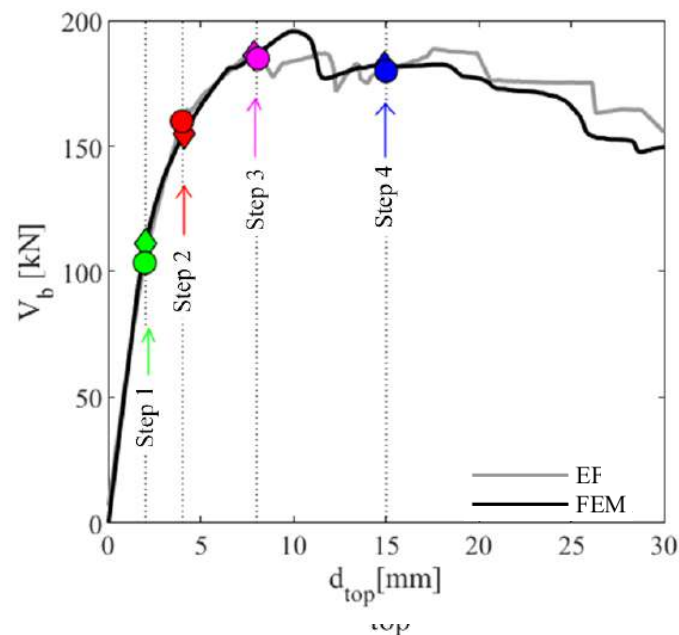
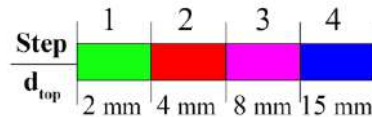
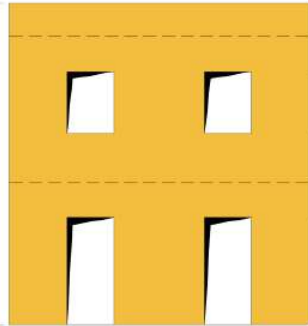
POST-PEAK RESPONSE



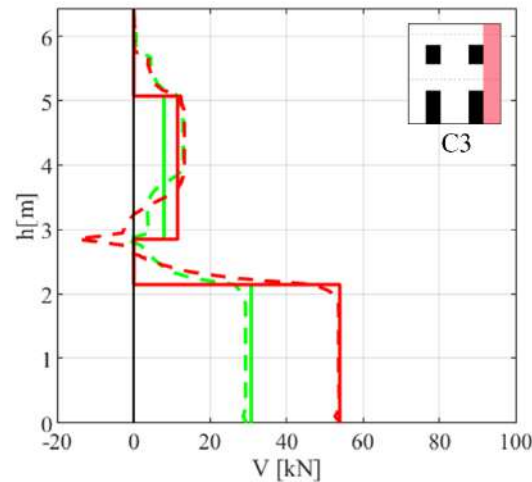
2D Issues: Equivalent frame idealization of URM walls

LOCAL RESPONSE

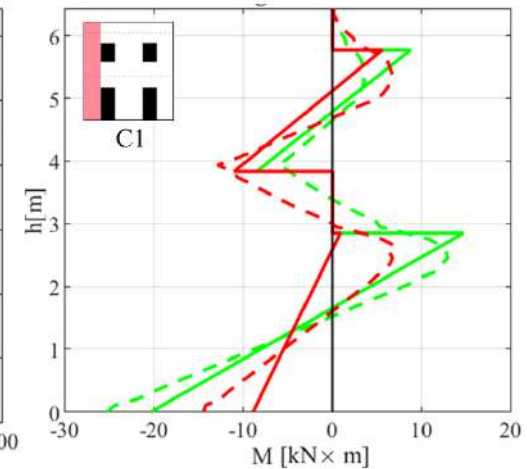
Regular wall



Shear force - C3

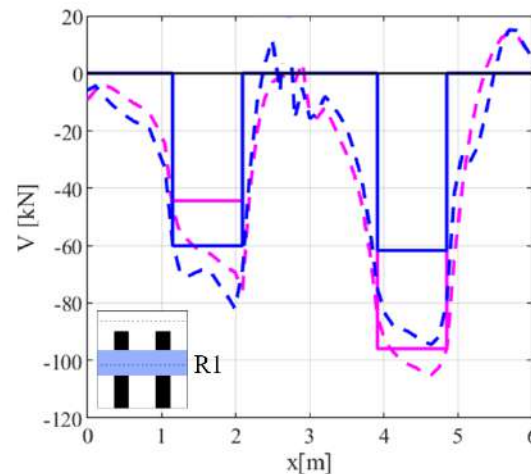


Bending Moment - C1

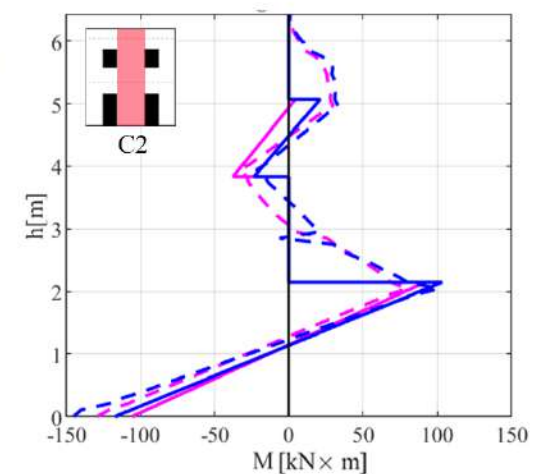


— EF Step 1 — EF Step 2 — EF Step 3 — EF Step 4
 - - FEM Step 1 - - FEM Step 2 - - FEM Step 3 - - FEM Step 4

Shear force - R1



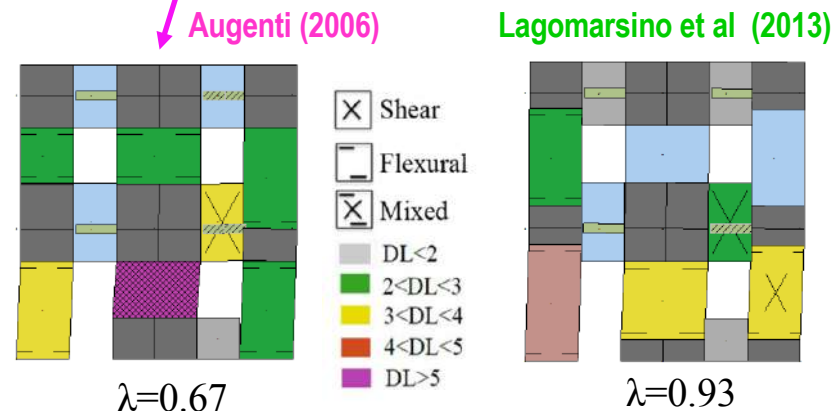
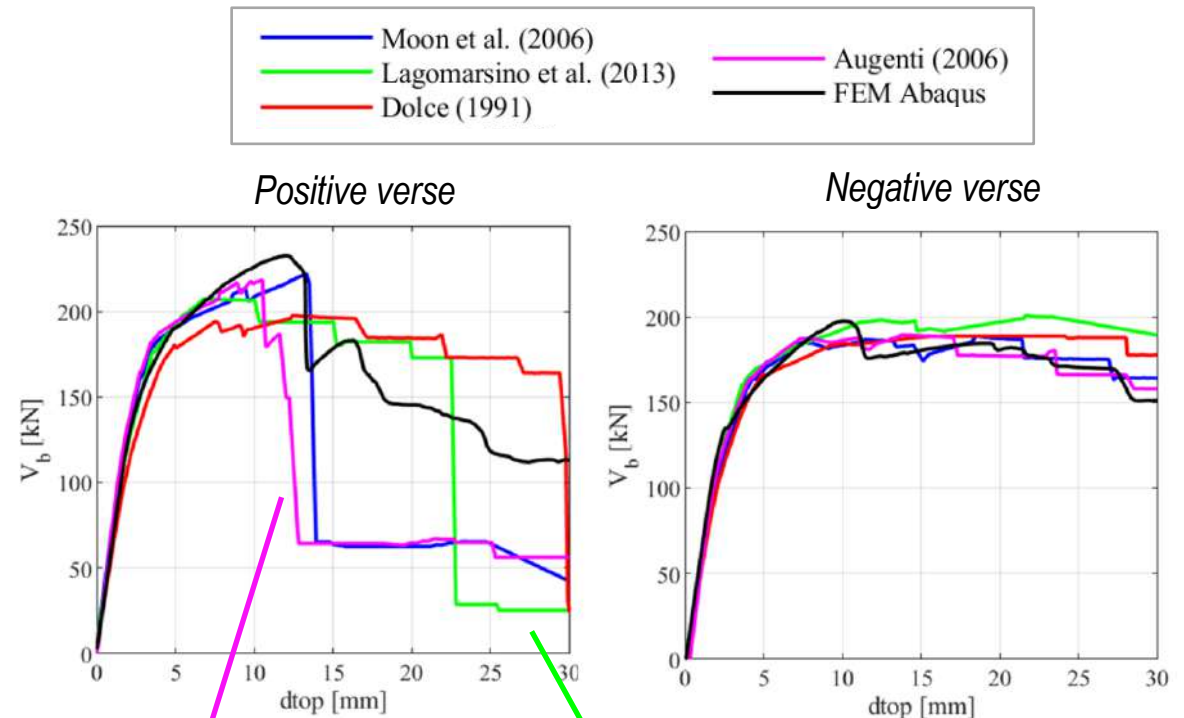
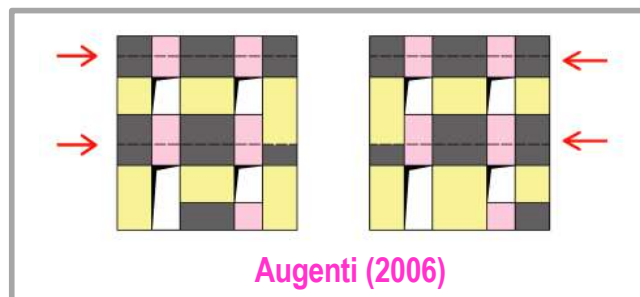
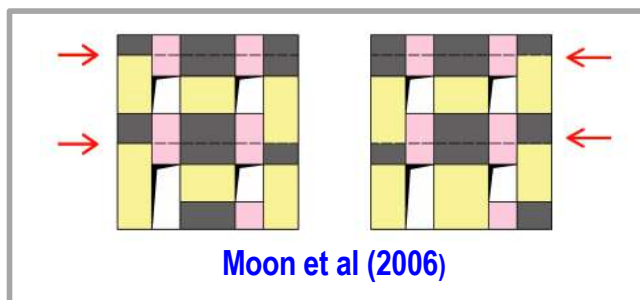
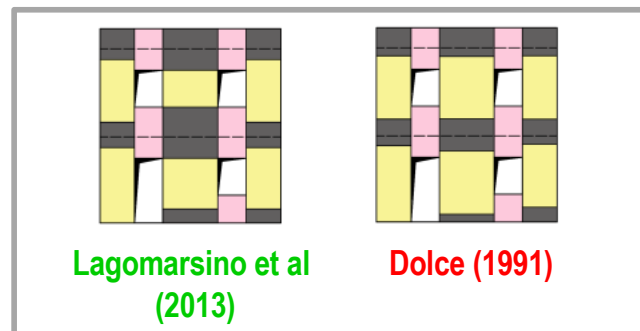
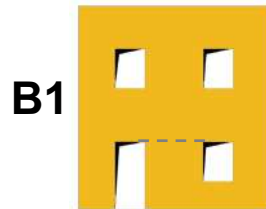
Bending Moment - C2



Reference: Camilletti 2019 PhD thesis, University of Genoa

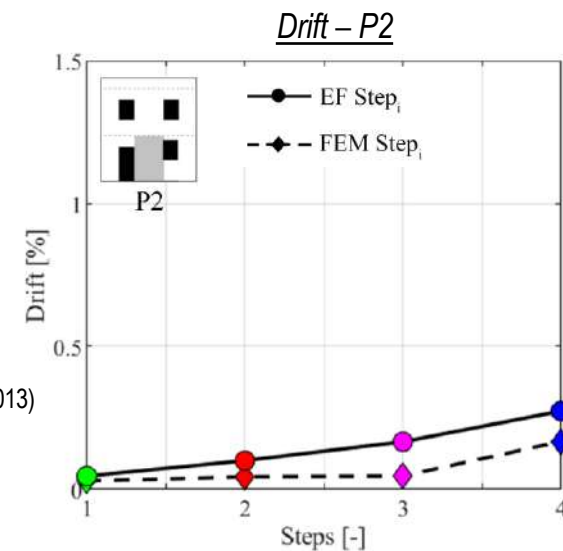
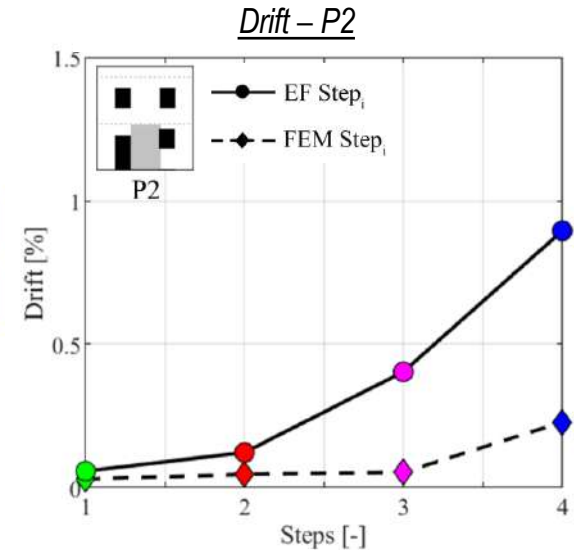
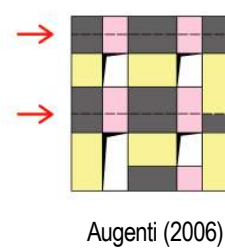
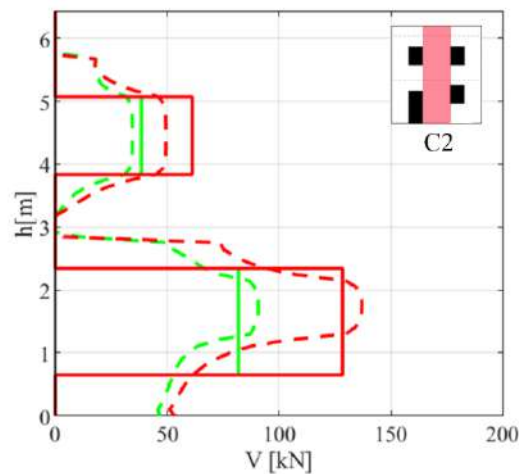
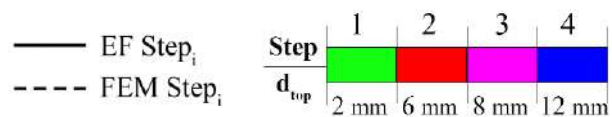
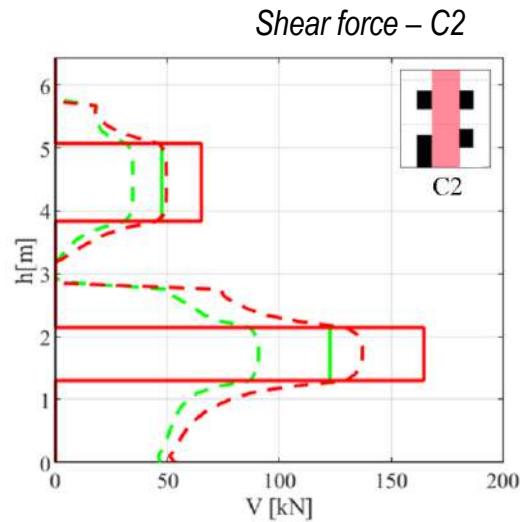
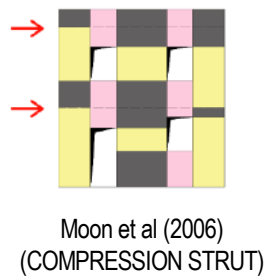
2D Issues: Equivalent frame idealization of URM walls

PROBLEM 1 - Identification of pier's effective height (*horizontal irregularity*)

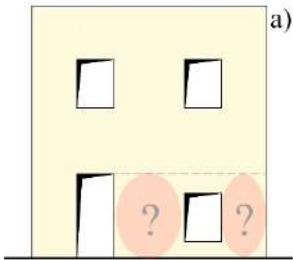


Reference: Camilletti 2019 PhD thesis, University of Genoa

2D Issues: Equivalent frame idealization of URM walls



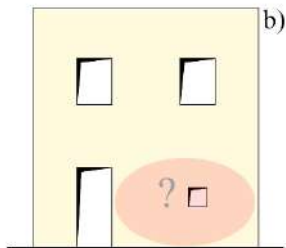
2D Issues: Equivalent frame idealization of URM walls



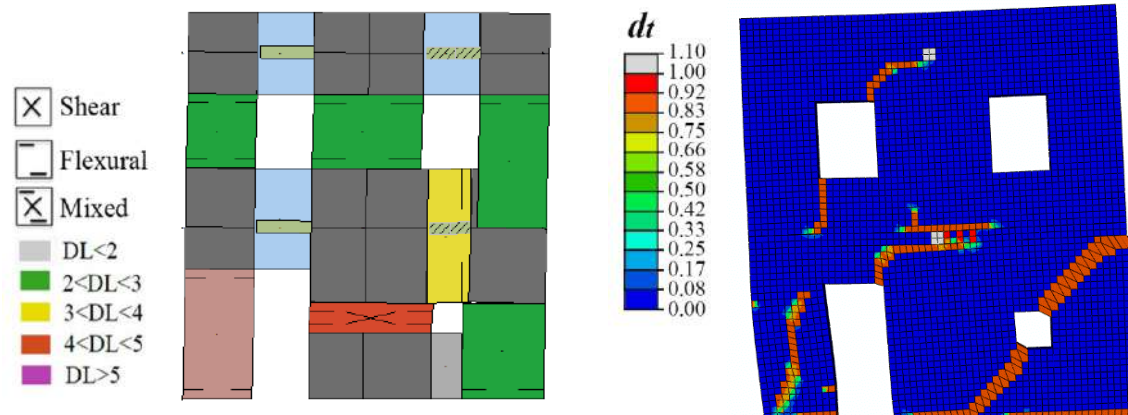
PROBLEM 1 - Identification of pier's effective height (*horizontal irregularity*)



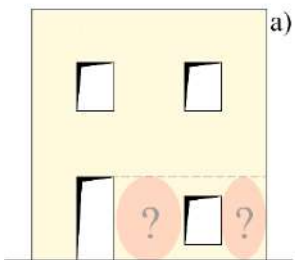
- **AUGENTI (2006) and MOON et al (2006) NOT RECOMMENDED**
- **DOLCE (1991) and LAGOMARSINO et al (2013) WITHOUTH CORRECTIVE MEASURES**



PROBLEM 2 – Presence of little openings



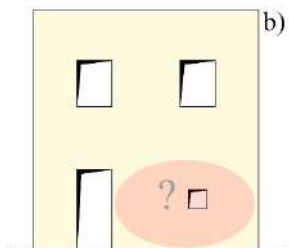
2D Issues: Equivalent frame idealization of URM walls



PROBLEM 1 - Identification of pier's effective height (*horizontal irregularity*)



- **AUGENTI (2006) and MOON et al (2006) NOT RECOMMENDED**
- **DOLCE (1991) and LAGOMARSINO et al (2013) WITHOUTH CORRECTIVE MEASURES**

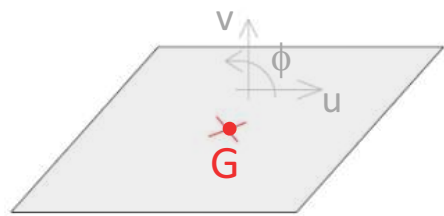


PROBLEM 2 – Presence of little openings



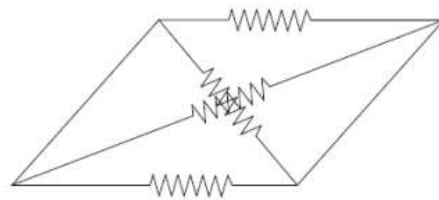
NEGLECT the OPENING in the STRUCTURAL MODEL

3D Issues: Diaphragms modelling

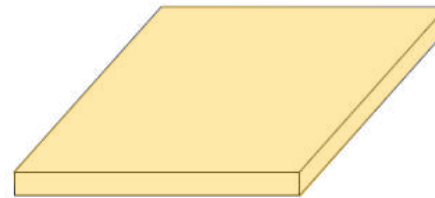


Rigid assumption

**OFTEN ADOPTED AS
DEFAULT BY SOFTWARE,
IN MANY CASES IS THE
ONLY OPTION**

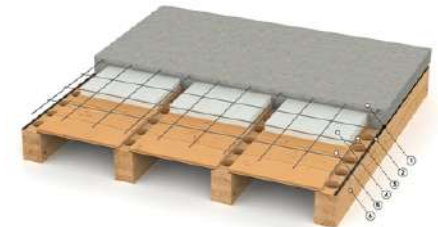


Set of equivalent
springs

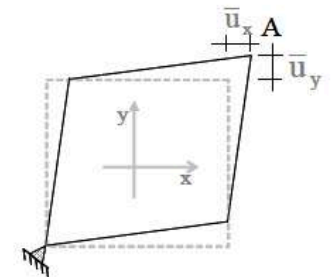
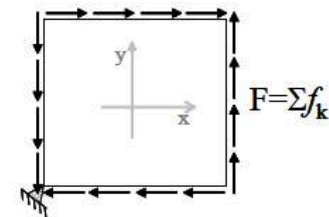
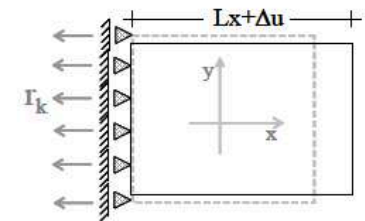
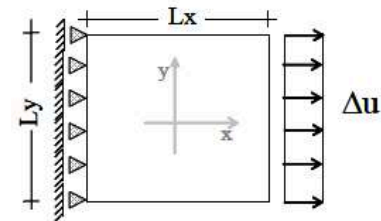


equivalent membranes

**MORE ADEQUATE FOR
DESCRIBING THE
EXISTING BUILDINGS**



Accurate modelling

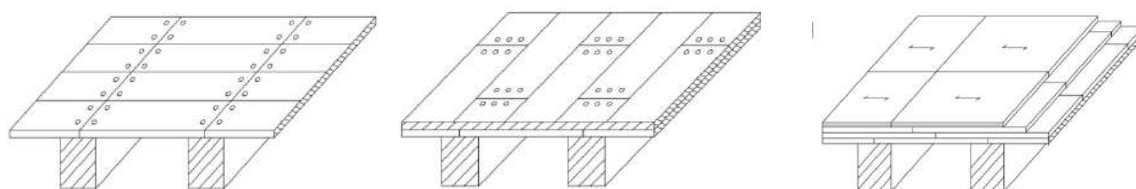


3D Issues: Diaphragms modelling

TIMBER FLOORS

FEMA Guidelines – ASCE 41-13

Default expected values for the in-plane stiffness of different kinds of diaphragm related to existing, enhanced or new configurations



Diaphragm type	G_d [kN/mm]
Single straight sheathing	0.35
Double straight sheathing	
Chorded	2.67
Un-chorded	1.24
Wood structural panel overlay on straight sheathing	
Un-blocked, un-chorded	0.87
Un-blocked, chorded	1.58
Blocked, un-chorded	1.24
Blocked, chorded	3.20

New Zealand guidelines

Provide formulae for the evaluation of the diaphragm stiffness depending, for each floor type, on the properties of each component.

Table 10.8: Shear stiffness values[†] for straight sheathed vintage flexible timber floor diaphragms (Giongo et al., 2014)

Direction of loading	Joist continuity	Condition rating	Shear stiffness [†] , G_d (kN/m)
Parallel to joists	Continuous or discontinuous joists	Good	350
		Fair	285
		Poor	225
Perpendicular to joists ^{††}	Continuous joist, or discontinuous joist with reliable mechanical anchorage	Good	285
		Fair	215
		Poor	170
	Discontinuous joist without reliable mechanical anchorage	Good	210
		Fair	170
		Poor	135

Note:

[†] Values may be amplified by 20% when the diaphragm has been railed using modern nails and nail guns

^{††} Values should be interpolated when there is mixed continuity of joists or to account for continuous sheathing at joist splice

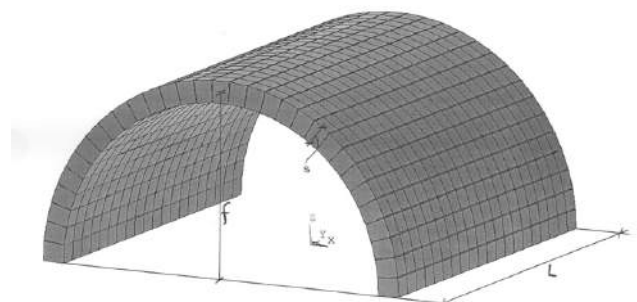
Table 10.9: Stiffness multipliers for other forms of flexible timber diaphragms (derived from ASCE, 2013)

Type of diaphragm sheathing		Multipliers to account for other sheathing types
Single straight sheathing		x 1.0
Double straight sheathing	Chorded	x 7.5
	Unchorded	x 3.5
Single diagonal sheathing	Chorded	x 4.0
	Unchorded	x 2.0
Double diagonal sheathing or straight sheathing above diagonal sheathing	Chorded	x 9.0
	Unchorded	x 4.5

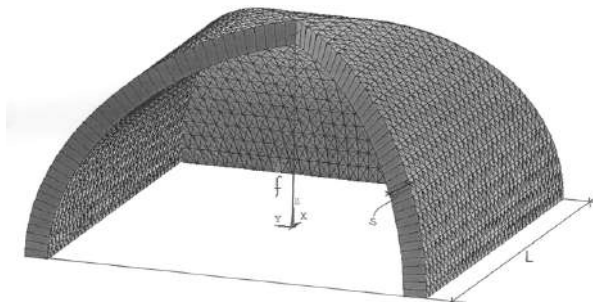
3D Issues: Diaphragms modelling

MASONRY VAULTS

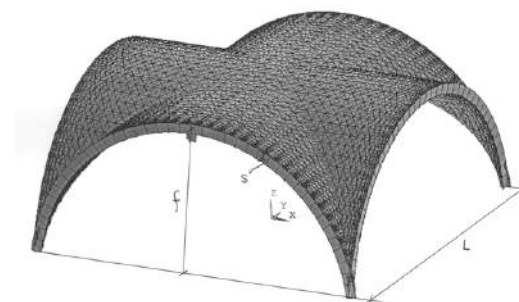
Linear and non linear parametric FEM simulations (Cattari et al. 2008, Proc. of 6th SAHC)



Barrel vault

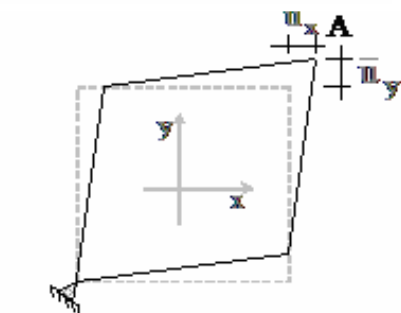
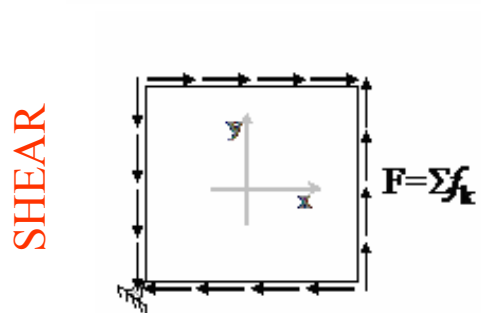
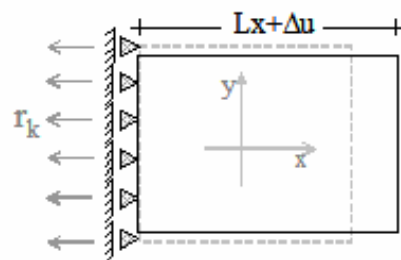
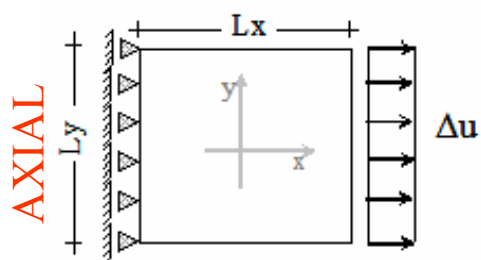


Cloister vault



Cross vault

Boundary configuration and loads



LINEAR NUMERICAL ANALYSES

Shear stiffness G_v/G

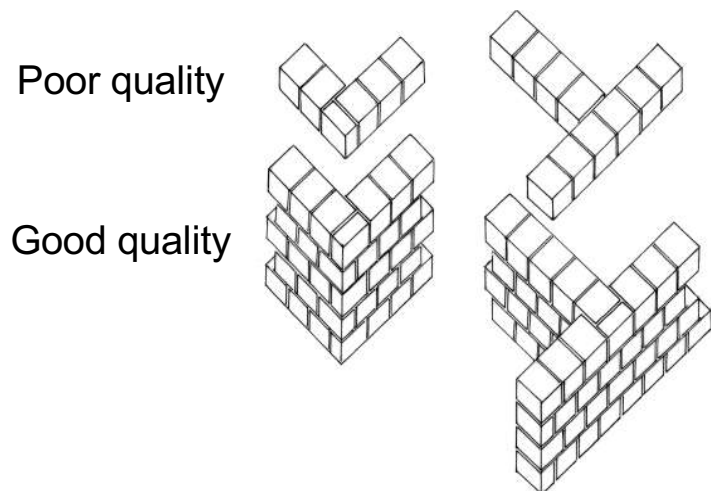
Analytical expressions aimed to take into account the shape effect and the boundary conditions as a function of the vault types

$$\frac{G_v}{G} = \left(b_1 \frac{s}{L} + b_2 \right) \left(\frac{f}{L} \right) + b_3 \frac{s}{L} + b_4$$

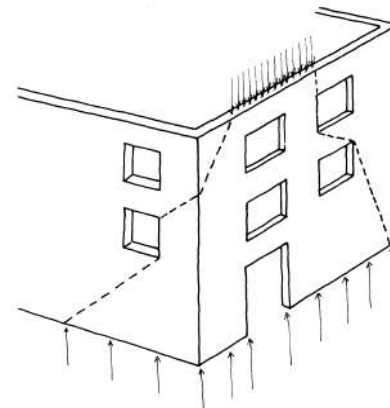
	Vault tipology		
	Barrel	Cloister	Cross
b_1	1.6433	-0.1633	-1.12
b_2	-1.8191	-1.3051	-4.1766
b_3	0.1133	1.9733	8.9033
b_4	1.1189	1.0339	0.7273
b_5	-	-	-34.323
b_6	-	-	5.6202

3D Issues: Connection between orthogonal walls

Quality of wall to wall connection

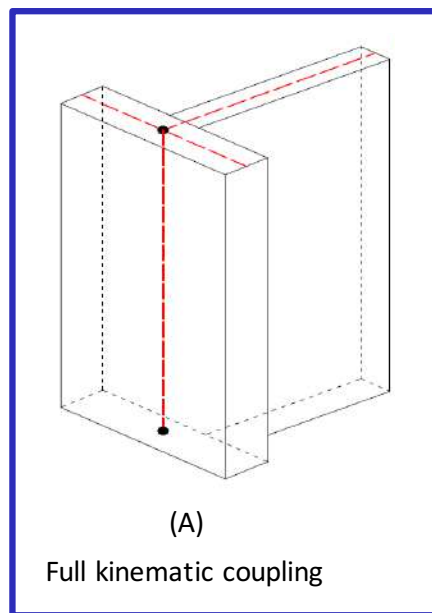


Redistribution of vertical actions among well connected walls

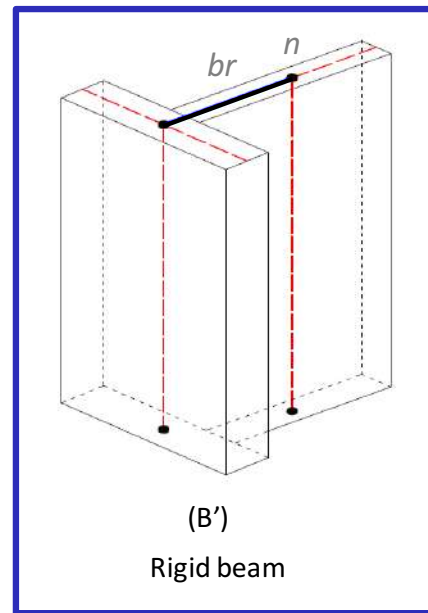
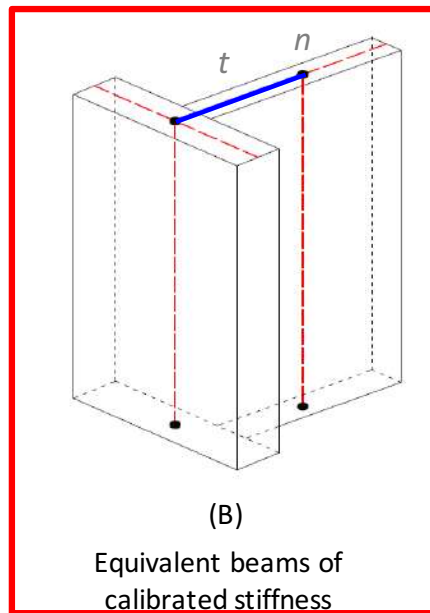


&

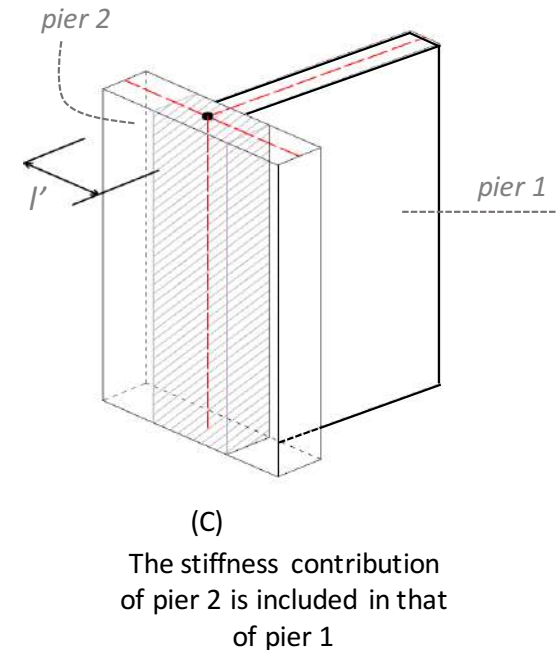
POSSIBLE MODELLING STRATEGY ADOPTED BY SOFTWARE



FULL COUPLING



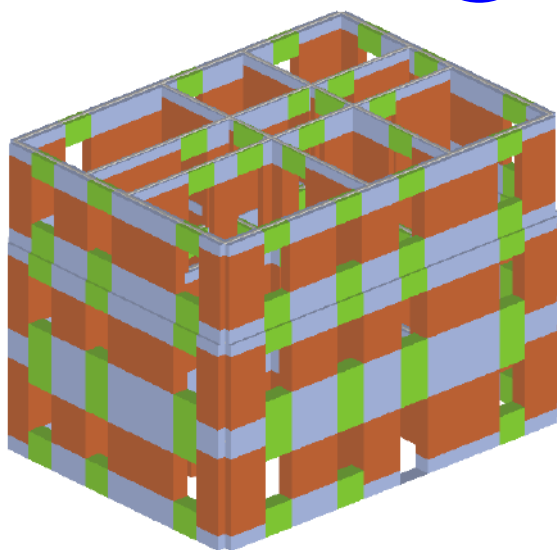
FULL COUPLING



Equivalent Frame Models – TREMURI PROGRAM

3D NONLINEAR STATIC AND
DYNAMIC ANALYSIS BY
EQUIVALENT FRAME MODEL

TREMURI



by Lagomarsino S., Penna A., Galasco A., Cattari S.

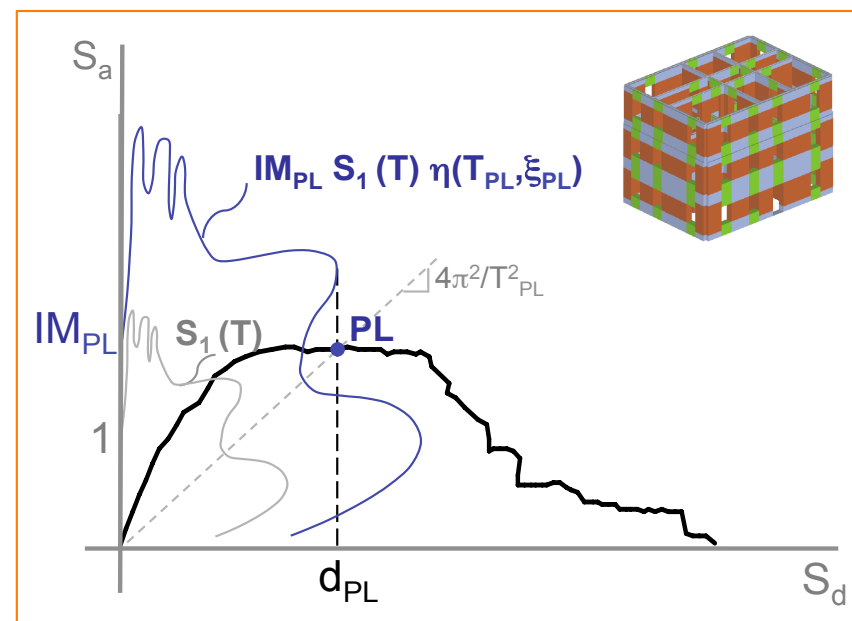
ask to: tremuri@gmail.com

3MURI

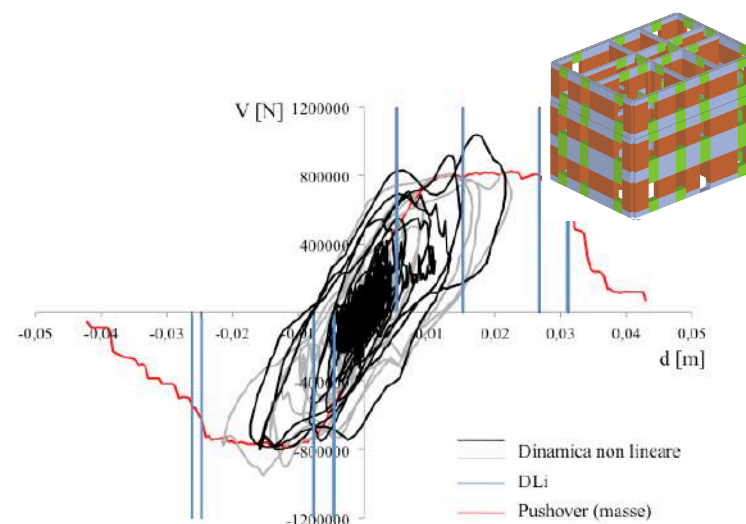


ask to: **STADATA s.r.l.** (www.stadata.com)

NON LINEAR DYNAMIC ANALYSIS

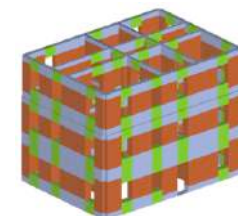


NON LINEAR DYNAMIC ANALYSIS



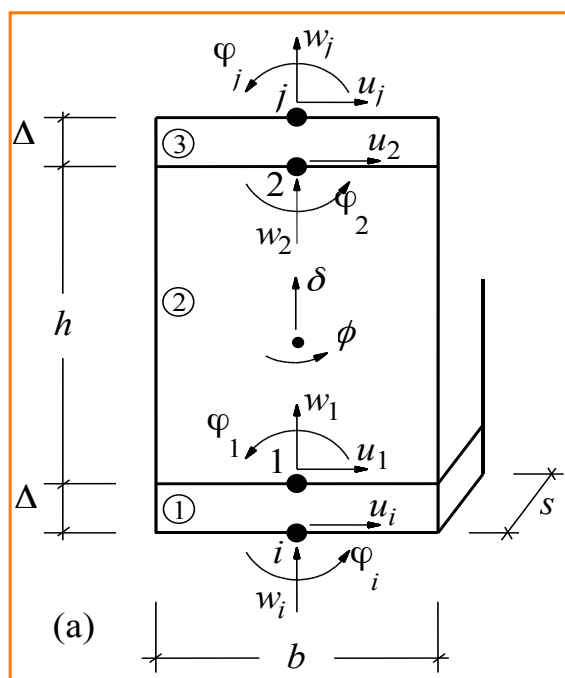


✓ CONSTITUTIVE MODELS IMPLEMENTED IN TREMURI FOR MASONRY PANELS:



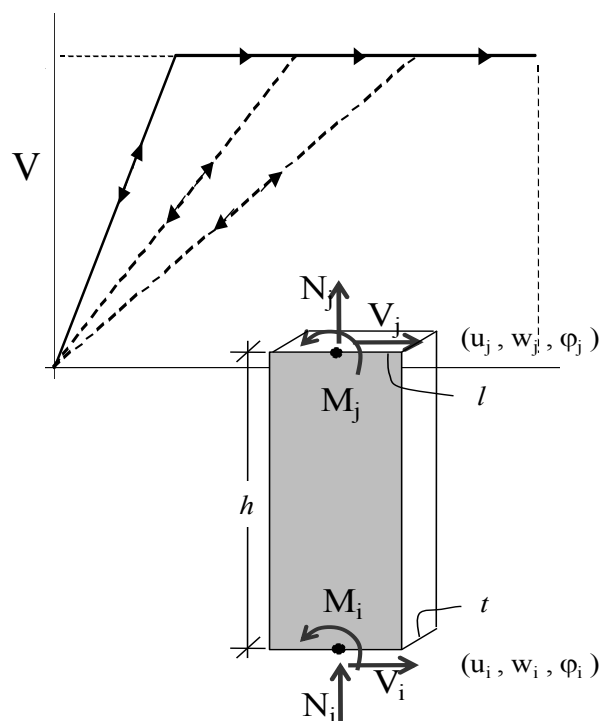
NON LINEAR MACROELEMENT

Gambarotta & Lagomarsino 1997;
Penna 2002;
Penna, Lagomarsino & Galasco
2013



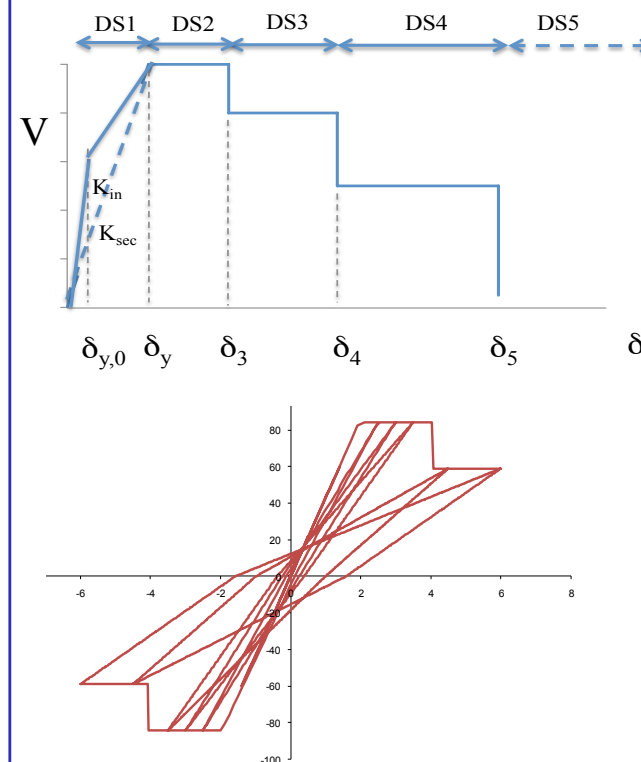
NON LINEAR BEAM Bi-linear relation

Galasco 2006
Lagomarsino, Penna, Galasco &
Cattari 2013



NON LINEAR BEAM Piecewise linear constitutive law

Cattari & Lagomarsino 2013



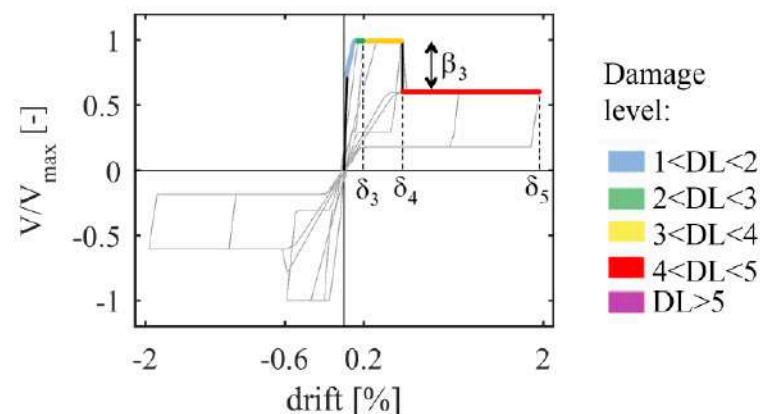
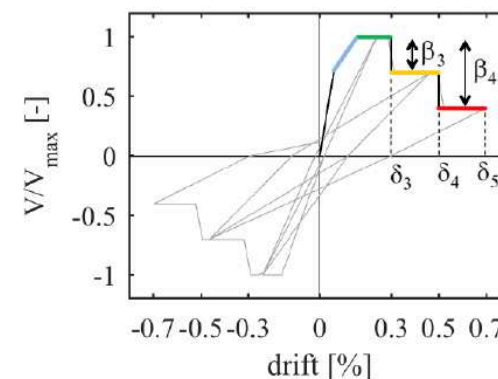
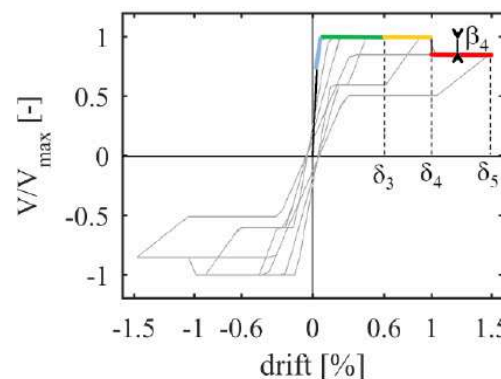
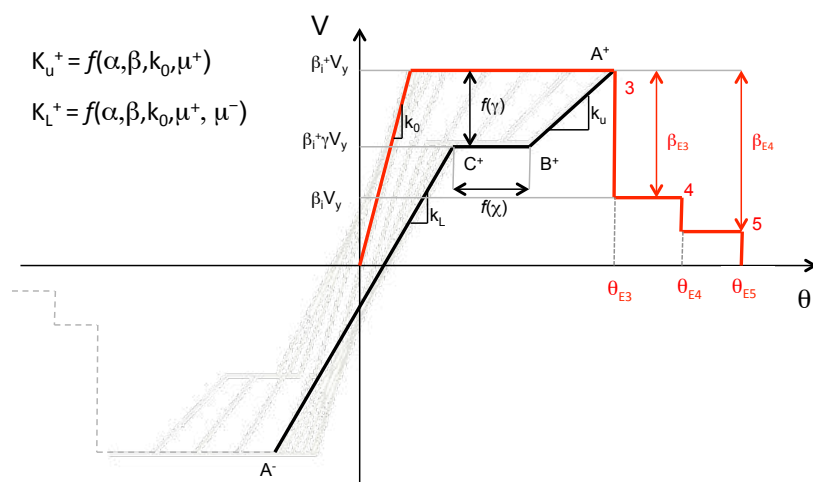
REF: Lagomarsino S, Penna A, Galasco A, Cattari S. (2013) TREMURI program: an equivalent frame model for the nonlinear seismic analysis of masonry buildings, *Engineering Structures*, 56, pp. 1787-1799, Elsevier, ISSN: 0141-0296

Non linear beam – *piecewise linear constitutive law*



Based on a phenomenological approach and allow to describe:

- ❑ the non linear response until very severe damage levels (from 1 to 5) through progressing strength decay (β_{Ei}) in correspondence of assigned values of drift (θ_{Ei});
- ❑ a quite accurate hysteretic response.



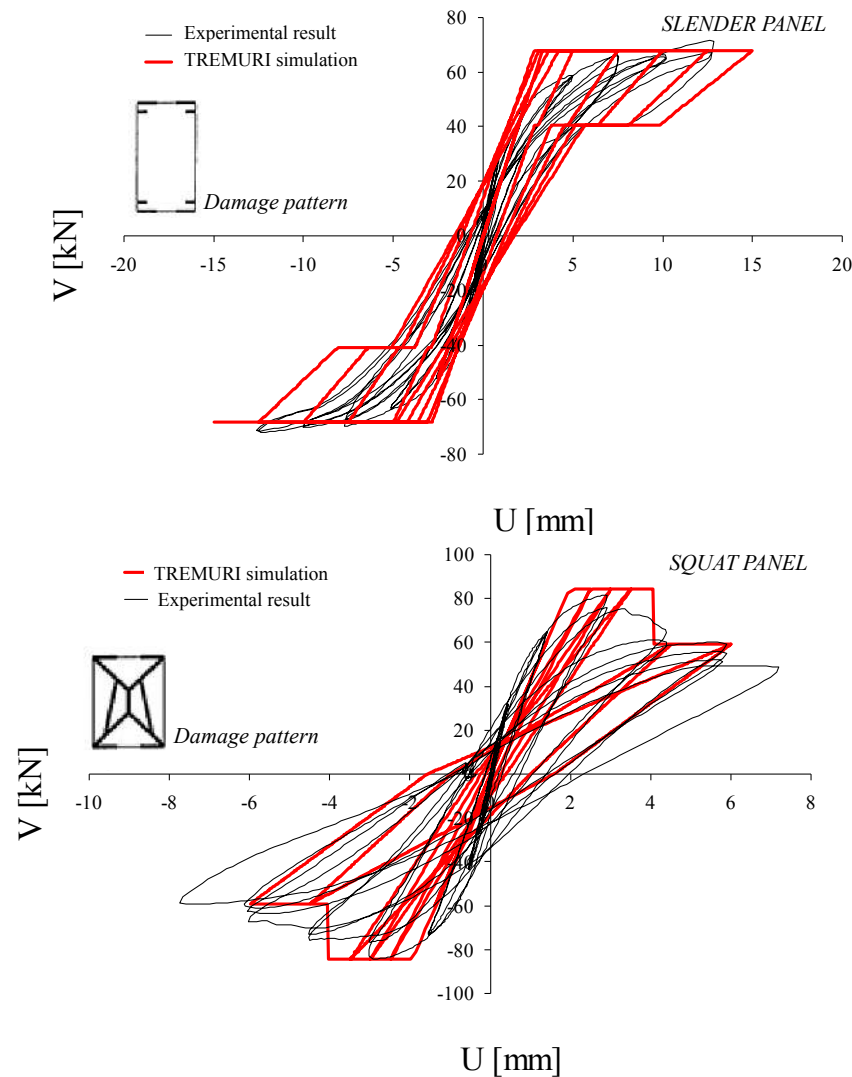
REF Cattari S., et al. (2018) Masonry Italian Code-Conforming Buildings. Part 2: Nonlinear Modelling and Time-History Analysis, *Journal of Earthquake Engineering*, Taylor and Francis, 22(sup2), 2010-2040

REFCattari S., Lagomarsino S. (2013) Masonry structures, pp.151-200, in : Developments in the field of displacement based seismic assessment, Edited by T. Sullivan and G.M.Calvi, Ed. IUSS Press (PAVIA) and EUCENTRE, pp.524, ISBN:978-88-6198-090-7.

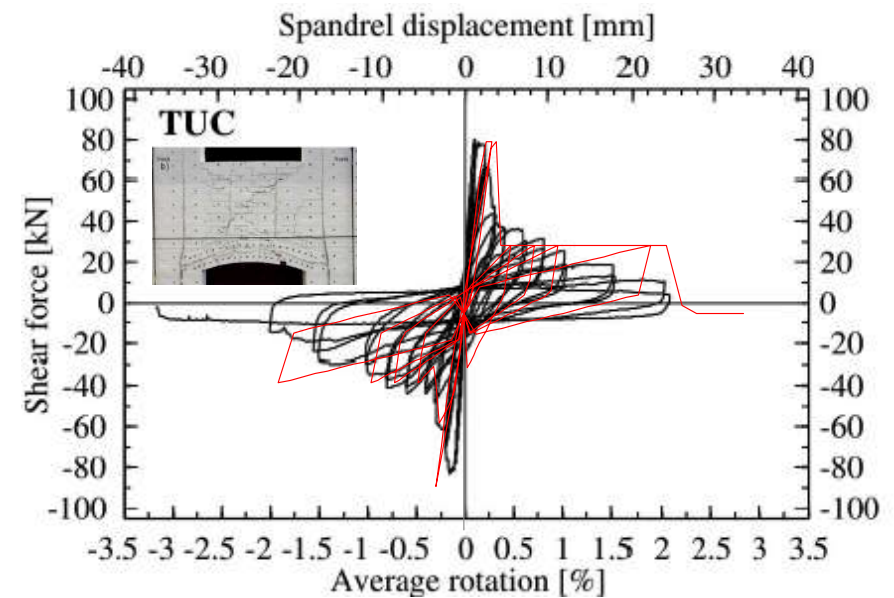
Non linear beam – *piecewise linear constitutive law*



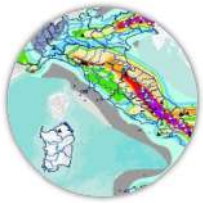
PIERS – Anthoine et al. 1995



SPANDRELS – Beyer & Dazio 2012

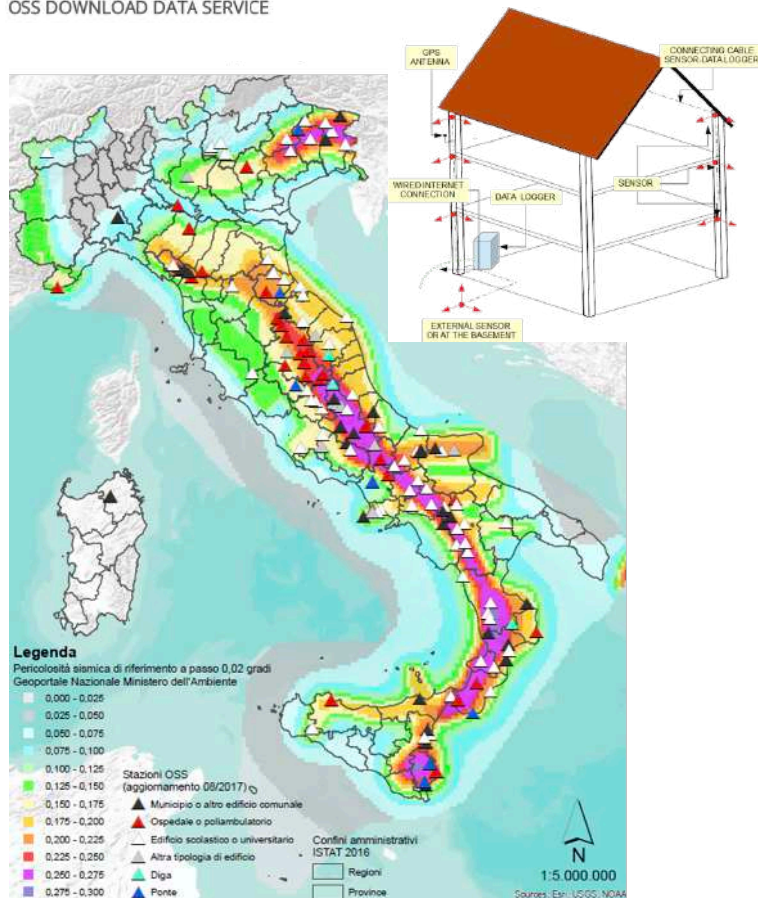


VALIDATION ON MONITORED URM BUILDINGS



OSS

Osservatorio Sismico delle Strutture
OSS DOWNLOAD DATA SERVICE

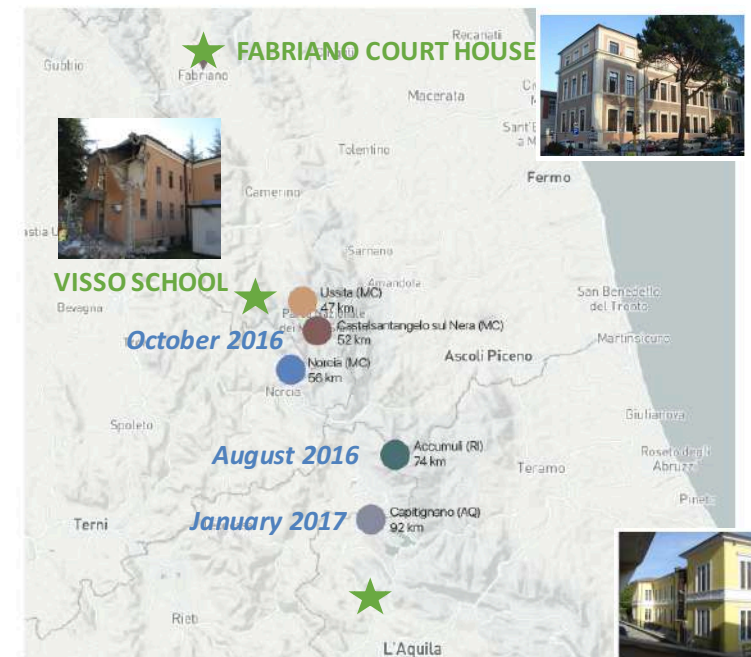


WORKGROUP -Task 4.1

Analysis of masonry buildings monitored by "OSS"

REFERENCE: S. Cattari et al. 2019 Discussion on data recorded by the Italian structural seismic monitoring network on three masonry structures hit by the 2016-2017 Central Italy earthquake, *Proc. of COMPDYN 2019*, Crete 24-26 June 2019.

- Città di Fabriano
- 24/08/2016 - h 01:36
- 26/10/2016 - h 17:10
- 26/10/2016 - h 19:18
- 30/10/2016 - h 06:40
- 18/01/2017 - h 10:14



Fabriano Courthouse

Built in 1940 – 4-story building - interstory height 4.00 m - gross area: 1220 m²



First level plan

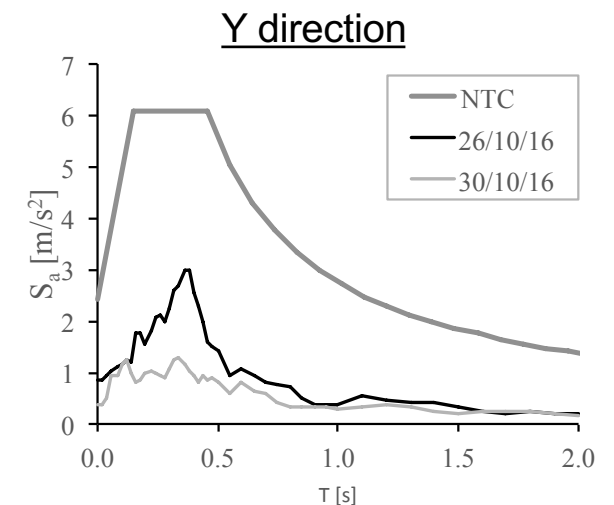
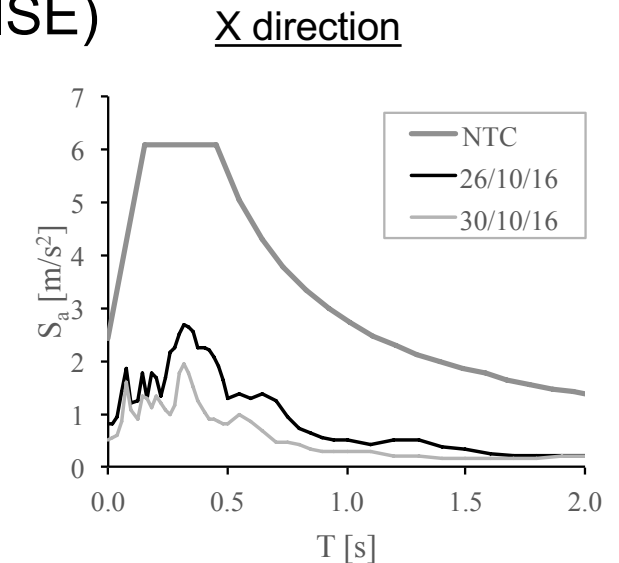
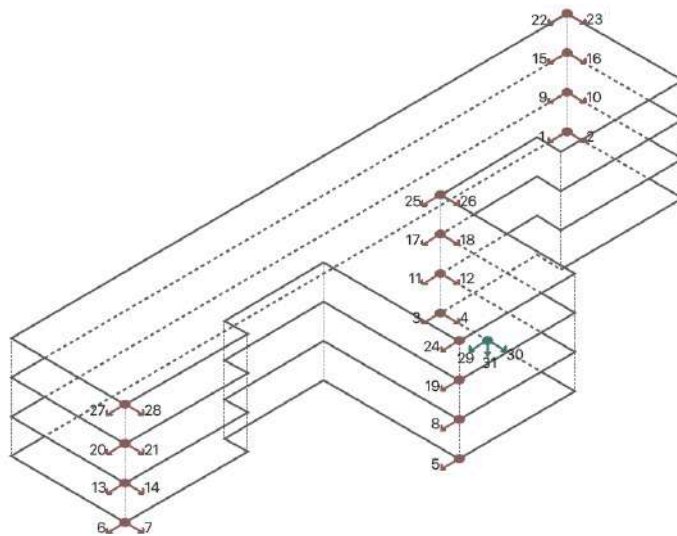


East facade



Fabriano Courthouse

MONITORING SISTEM & DATA AVAILABLE (RECORDINGS OF MAIN and SECONDARY EVENTS & AMBIENT VIBRATION NOISE)

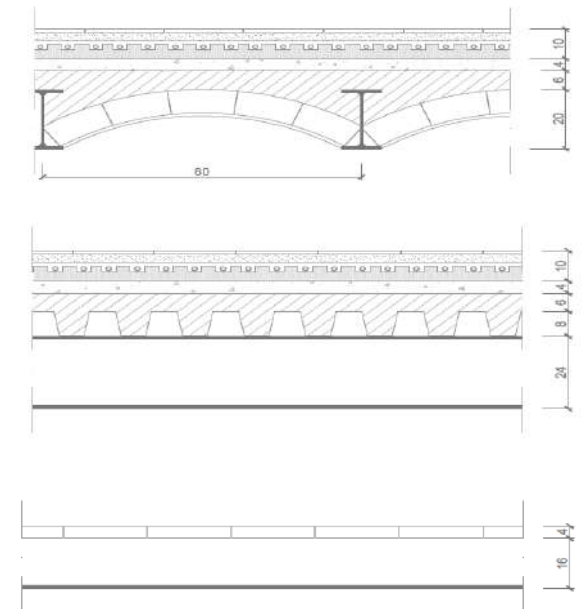
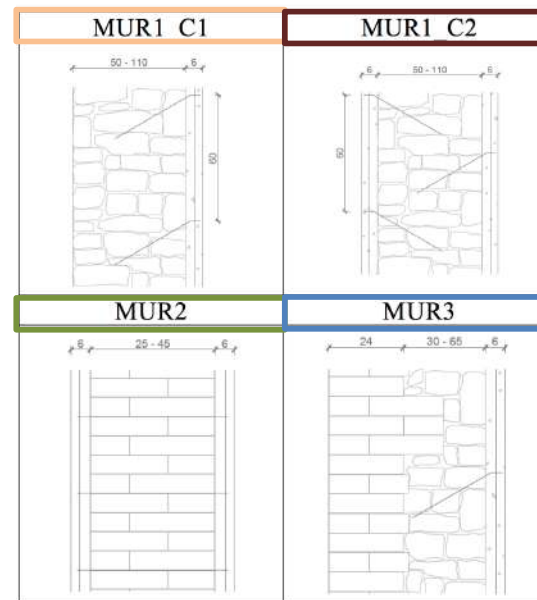
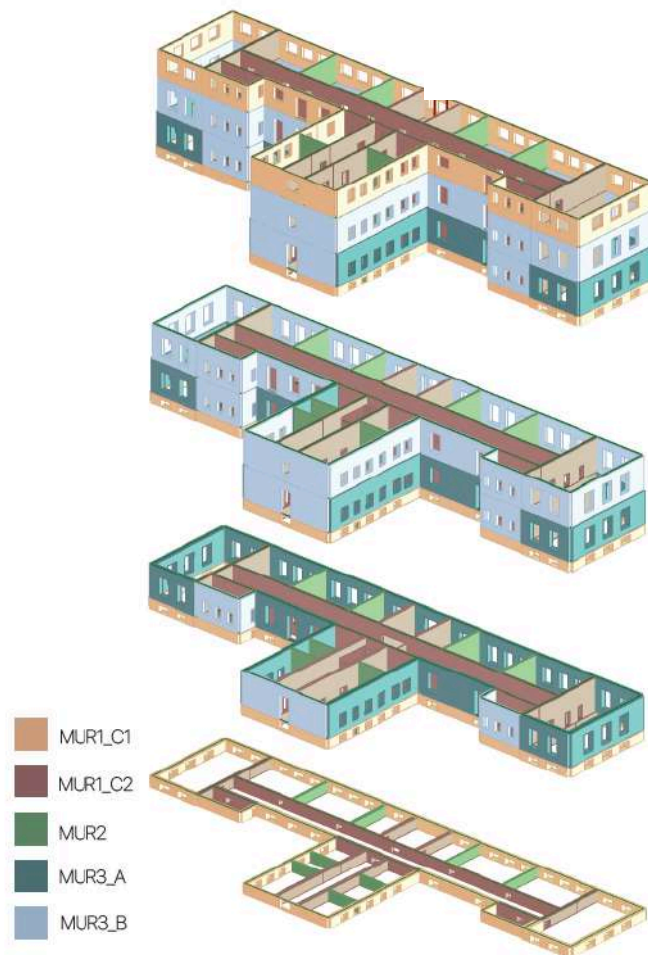


$T_R=712$ years – Soil B



Fabriano Courthouse

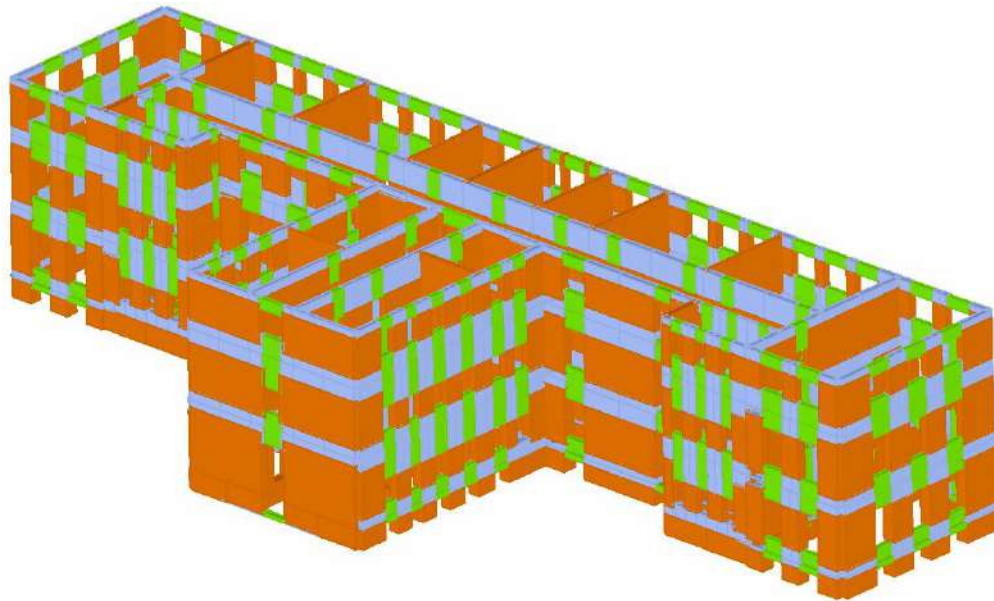
- Many kinds of strengthening interventions (date back to 1999) to masonry walls and to improve the wall-to-wall quality connection
- Many masonry types
- Many kinds of floors



Many uncertainties!
Interesting case for model calibration!!!

Fabriano Courthouse

CALIBRATION OF THE MODEL IN ELASTIC FIELD



UNCERTAINTIES CONSIDERED IN THE CALIBRATION PROCESS

16 aleatory uncertainties

5 type of different masonry types differentiated between piers & spandrels – raising up of last floor

Various epistemic uncertainties

- Flange effect
- Interaction with external stair (actual effectiveness of seismic joint)
- Role of basement
- Stiffness diaphragms

TARGET FOR THE CALIBRATION (BY UNIPD)

Mode B1 4.06 Hz

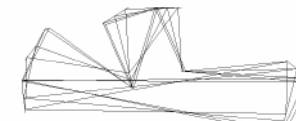
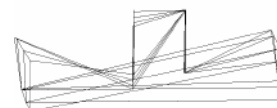
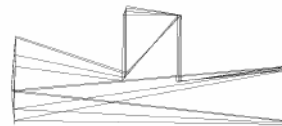
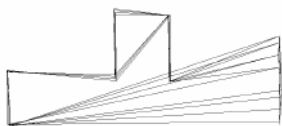
Mode B2 4.32 Hz

Mode Tx1 4.64 Hz

Mode Ty1 4.92 Hz

Mode R1 5.66 Hz

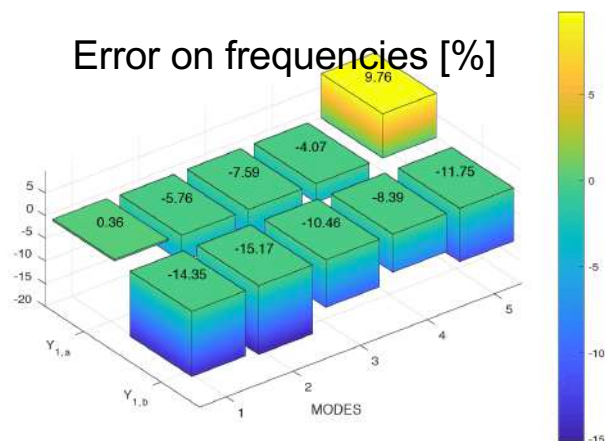
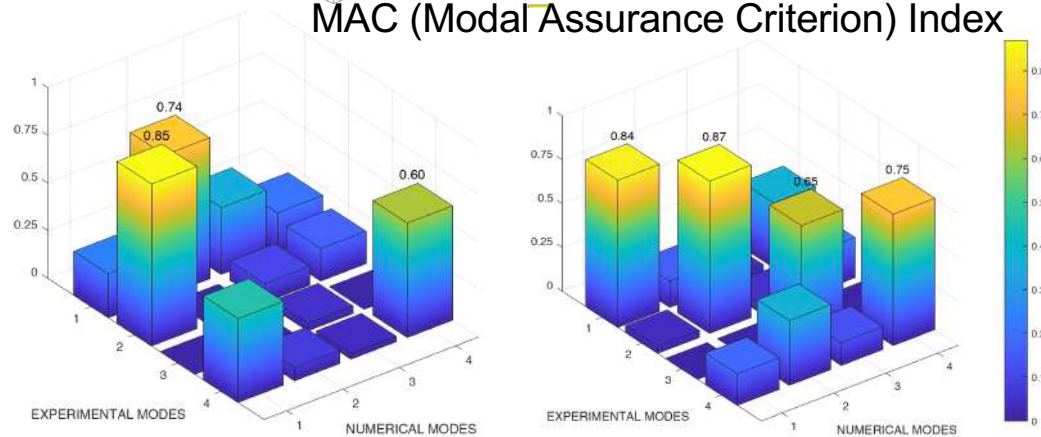
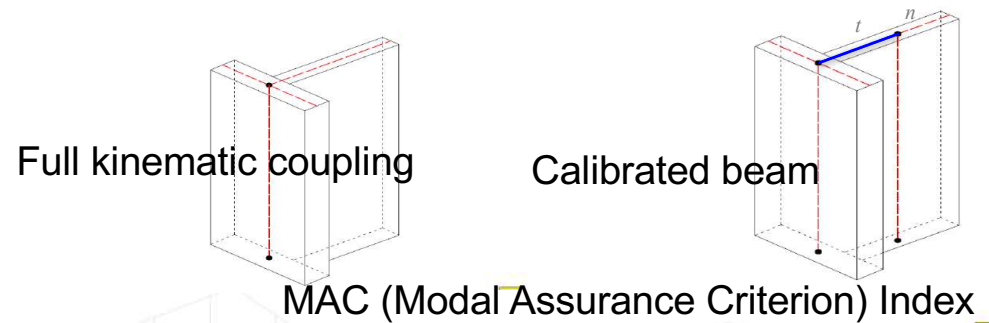
Mode R2 6.11 Hz



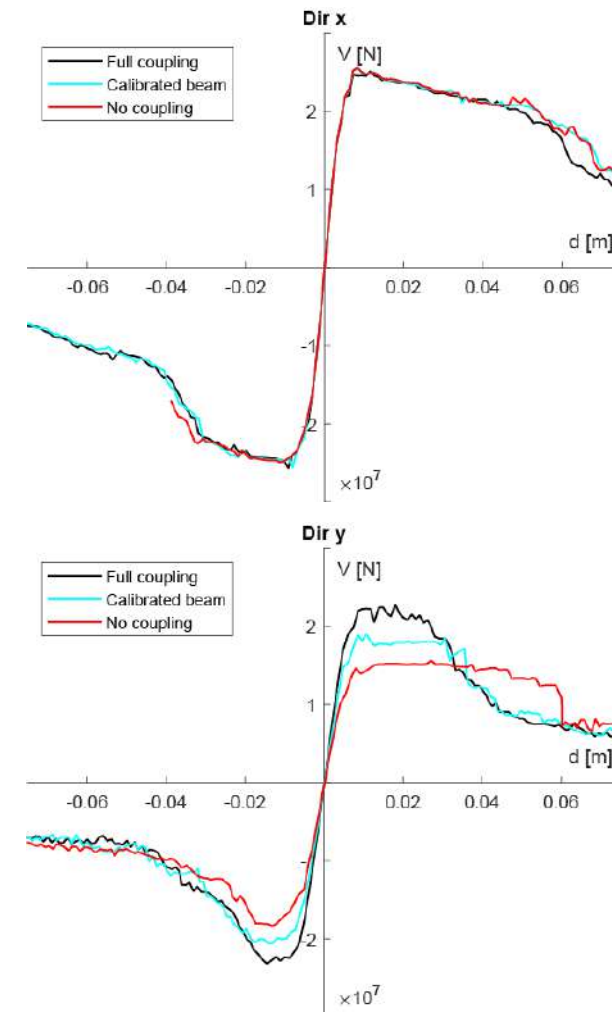


Fabriano Courthouse

CALIBRATION OF THE MODEL IN ELASTIC FIELD



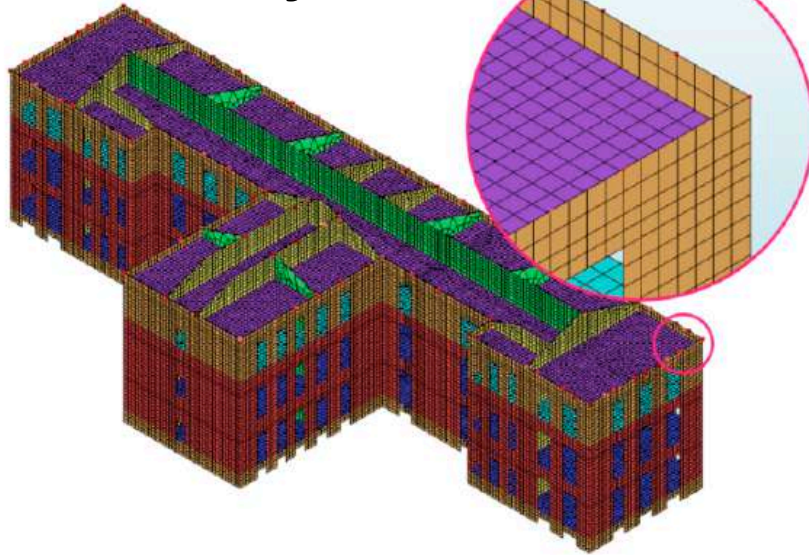
Repercussion of the correct assumption on NONLINEAR FIELD



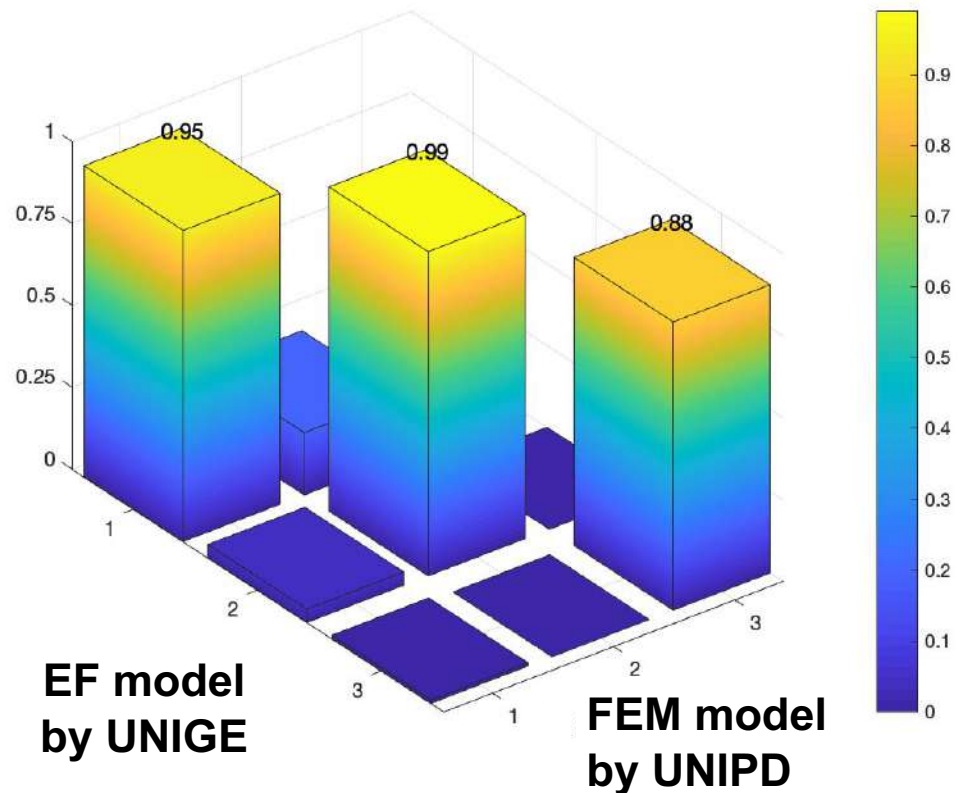
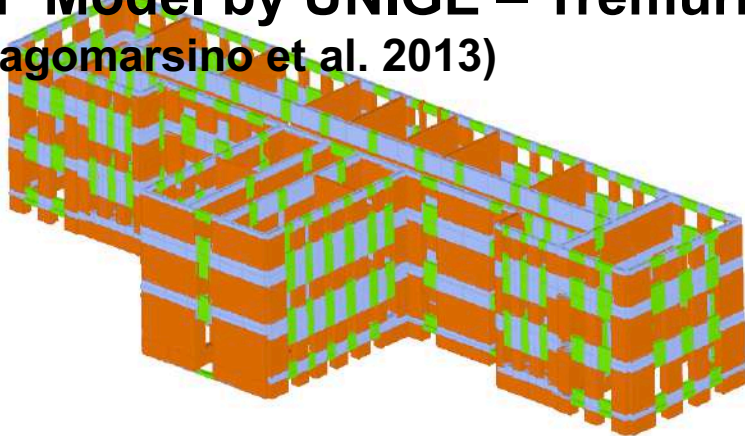
Fabriano Courthouse

CALIBRATION OF THE MODEL IN ELASTIC FIELD

FEM Model by UNIPD - Diana FEA



EF Model by UNIGE – Tremuri (Lagomarsino et al. 2013)

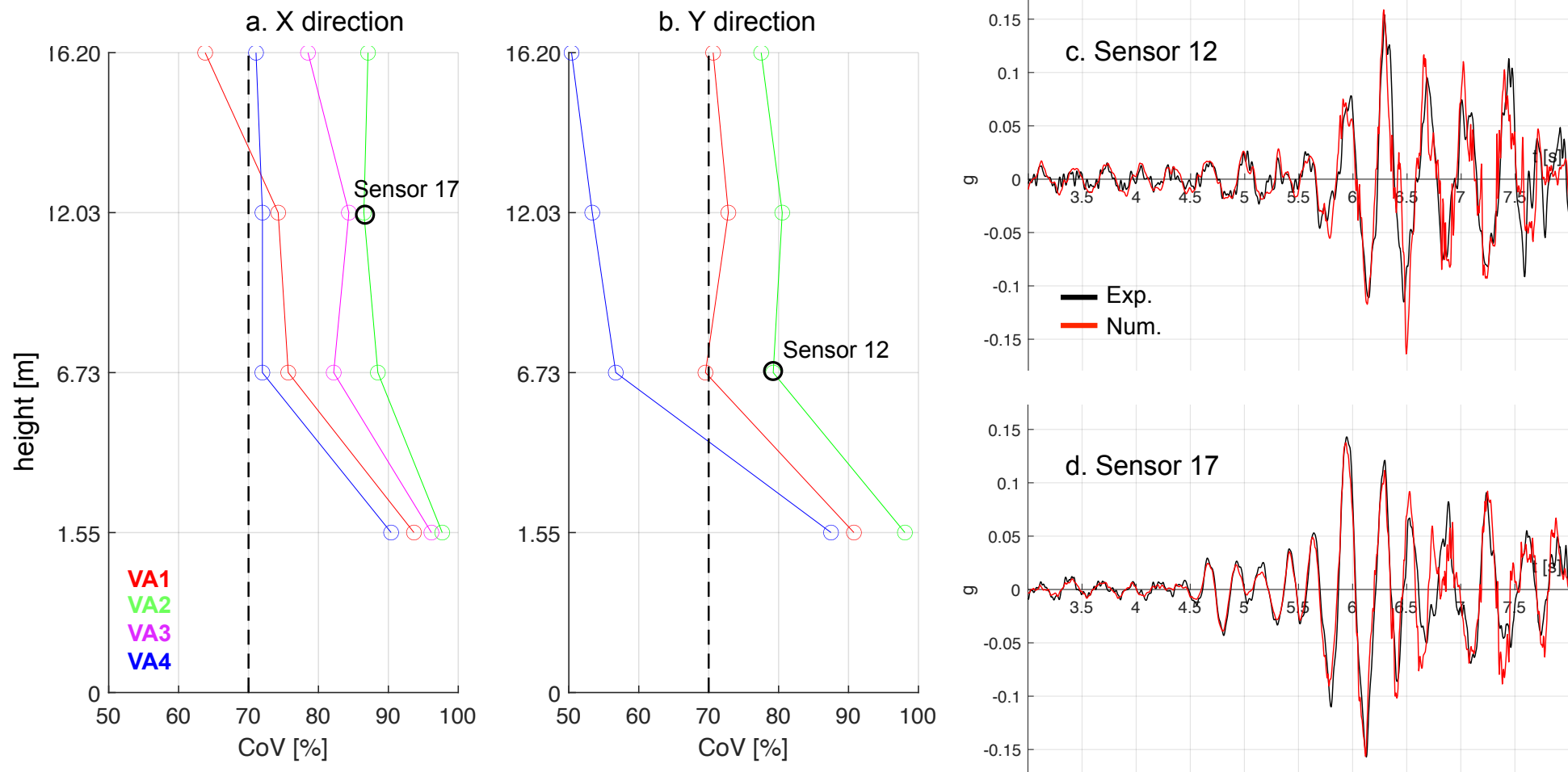


With analogous hypotheses and
by adopting mechanical
parameters with a maximum
difference of 20%



Fabriano Courthouse

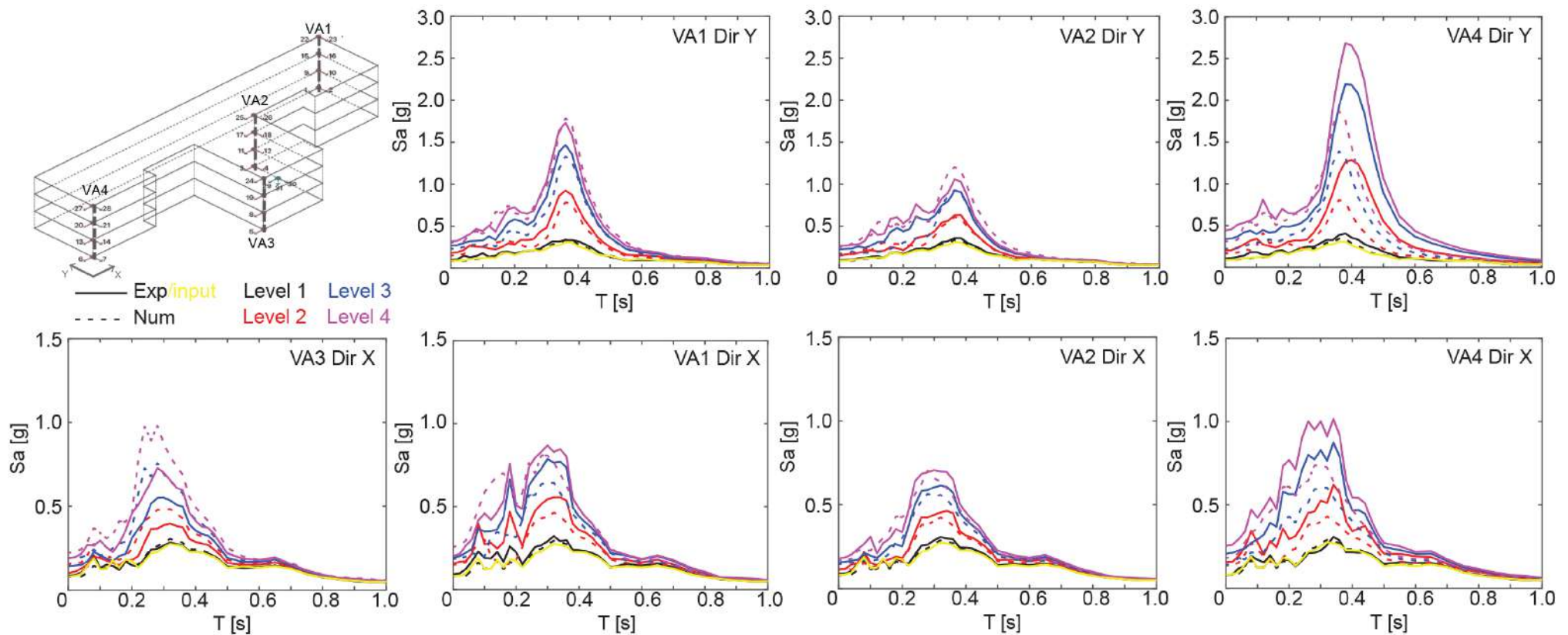
VALIDATION OF THE MODEL IN NONLINEAR FIELD – simulation of the actual response by performing nonlinear dynamic analyses



REF: Cattari et al. (2019) Calibrazione e validazione di modelli numerici da dati di monitoraggio permanente: il caso studio del Tribunale di Fabriano monitorato dall'Osservatorio Sismico delle Strutture, XVIII ANIDIS Conference, Ascoli Piceno.

Fabriano Courthouse

VALIDATION OF THE MODEL IN NONLINEAR FIELD – simulation of the actual response by performing nonlinear dynamic analyses

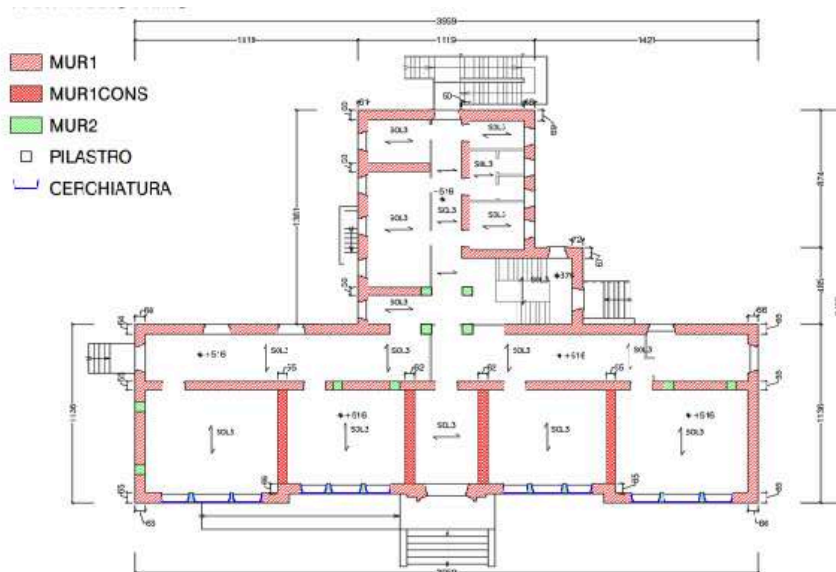


VALIDATION ON MONITORED URM BUILDINGS



The school of P. Capuzi in Visso

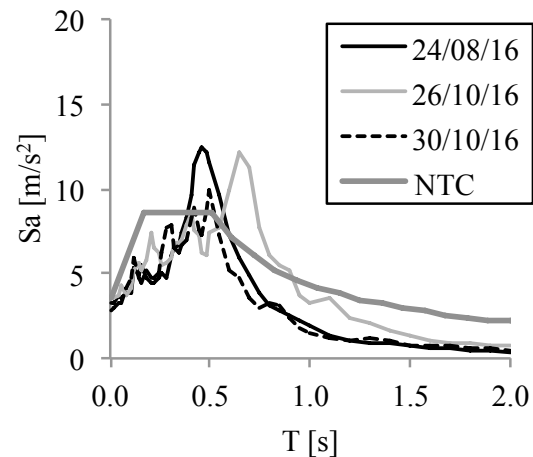
- Built in 1930
- Interstory height: 4.00 m
- Gross area: 520 m²
- T-shaped plan
- 3 story building
- Rigid floors
- Stone masonry



The school of P. Capuzi in Visso

- Significant damage accumulation effects after the subsequent shocks

X direction



24/8



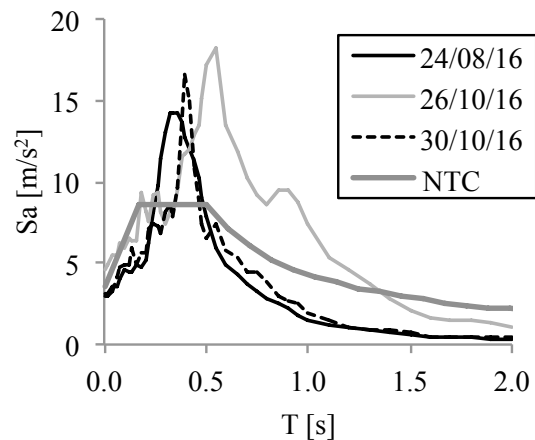
26/10



30/10



Y direction



24/8



26/10



30/10



$T_R=712$ years - Soil C

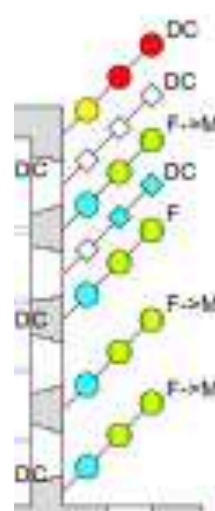
The school of P. Capuzi in Visso

- Reconstruction of damage accumulation effects through the photos available from DPC and the survey made by UNIGE RU

Final damage at 8/12/2016



Data on damage accumulation at scale of each element



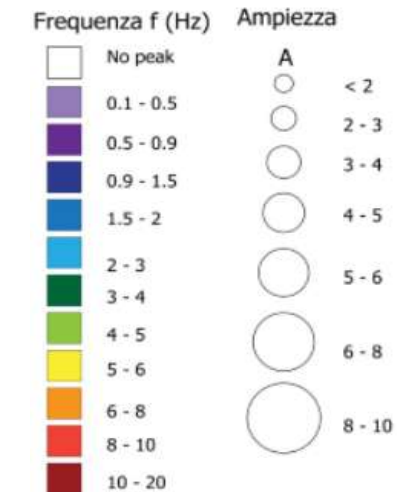
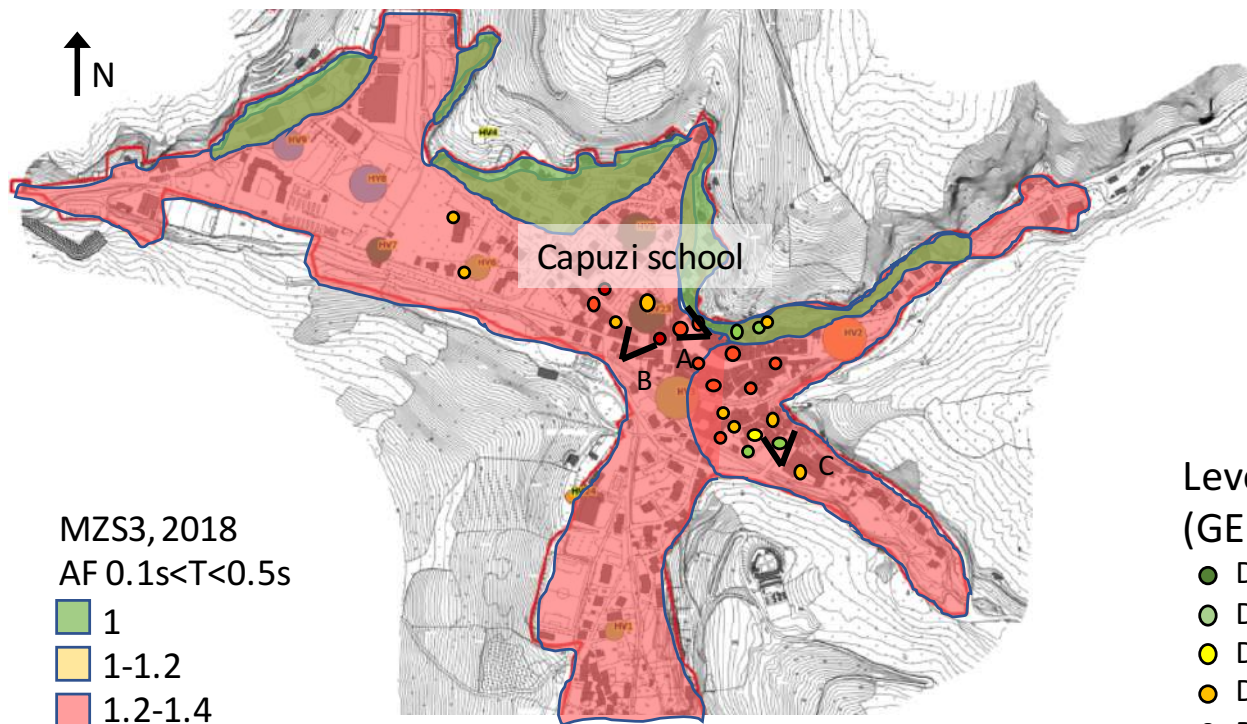
- ✓ The three dots refer to the three main events:
 - 24/08/2016
 - 26/10/2016
 - 30/10/2016
- ✓ The colour refer to the damage level
- ✓ The code (DC – *Diagonal cracking*; F – *flexural*; M – *mixed*) refers to the prevailing failure mode

VALIDATION ON MONITORED URM BUILDINGS



- Topographic & stratigrafic site amplifications were recognized at urban scale

HVSR MZS3, 2018



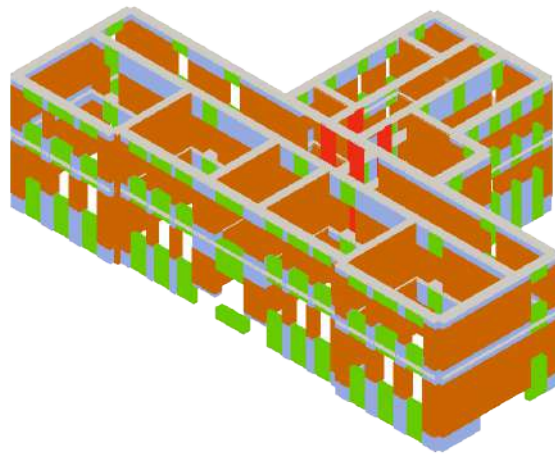
Level of damage after 24° August 2016
(GEER 1, 2017)

- D0-No damages
- D1-Cracking on non-structural elements
- D2-Major damage to non-structural elements
- D3-Significant damage to load-bearing elements
- D4-Partial structural collapse
- D5-Full collapse

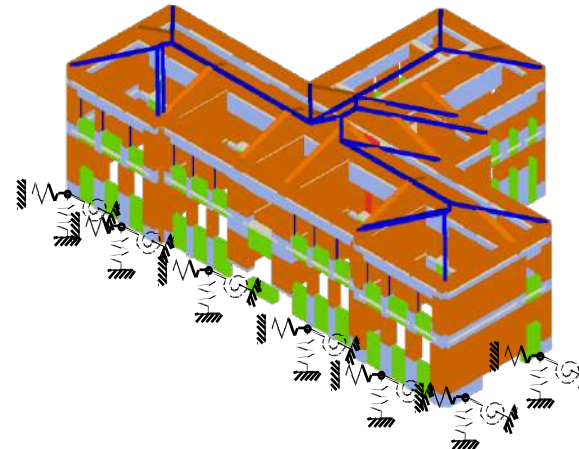


The school of P. Capuzi in Visso

CALIBRATION OF THE MODEL IN ELASTIC FIELD



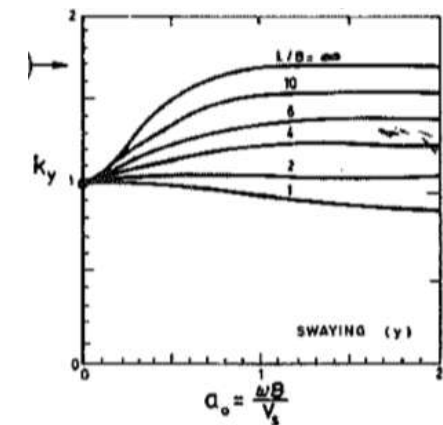
FIXED- BASE MODEL



COMPLIANT- BASE MODEL

	Dynamic identification procedure				Back-analysis			
	Impedances (G_0)				Impedances (G_{deg})			
	Area I		Area II		Area I		Area II	
	$\mu_{area\ I}$	$\sigma_{area\ I}$	$\mu_{area\ II}$	$\sigma_{area\ II}$	$\mu_{area\ I}$	$\sigma_{area\ I}$	$\mu_{area\ II}$	$\sigma_{area\ II}$
$K_x(kN/m)$	2.9E+05	0.32	7.9E+05	0.21	2.2E+05	0.36	3.5E+05	0.64
$K_y(kN/m)$	4.1E+05	0.45	6.7E+05	0.12	3.0E+05	0.44	2.3E+05	0.43
$K_z(kN/m)$	5.9E+05	0.44	1.4E+06	0.41	3.7E+05	0.44	3.7E+05	0.90
$K_{r,x}(kNm)$	3.5E+05	1.85	2.3E+06	0.08	2.5E+05	1.85	2.7E+05	1.37
$K_{r,y}(kNm)$	2.8E+05	1.38	4.2E+06	0.58	2.0E+05	1.38	6.3E+05	1.97

(Gazetas 1991)

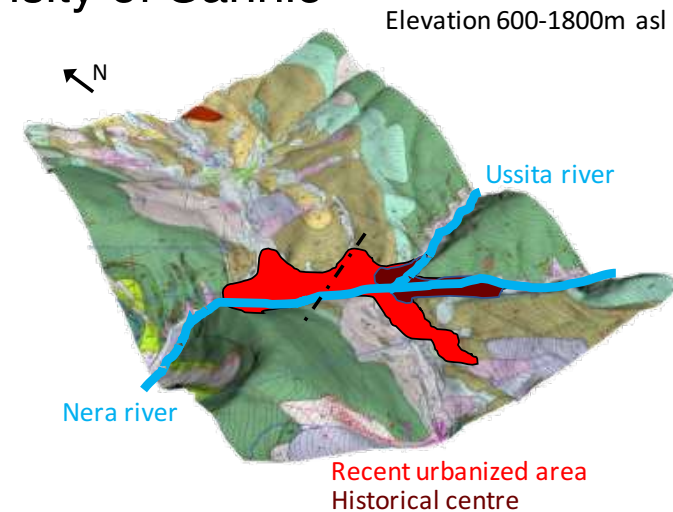
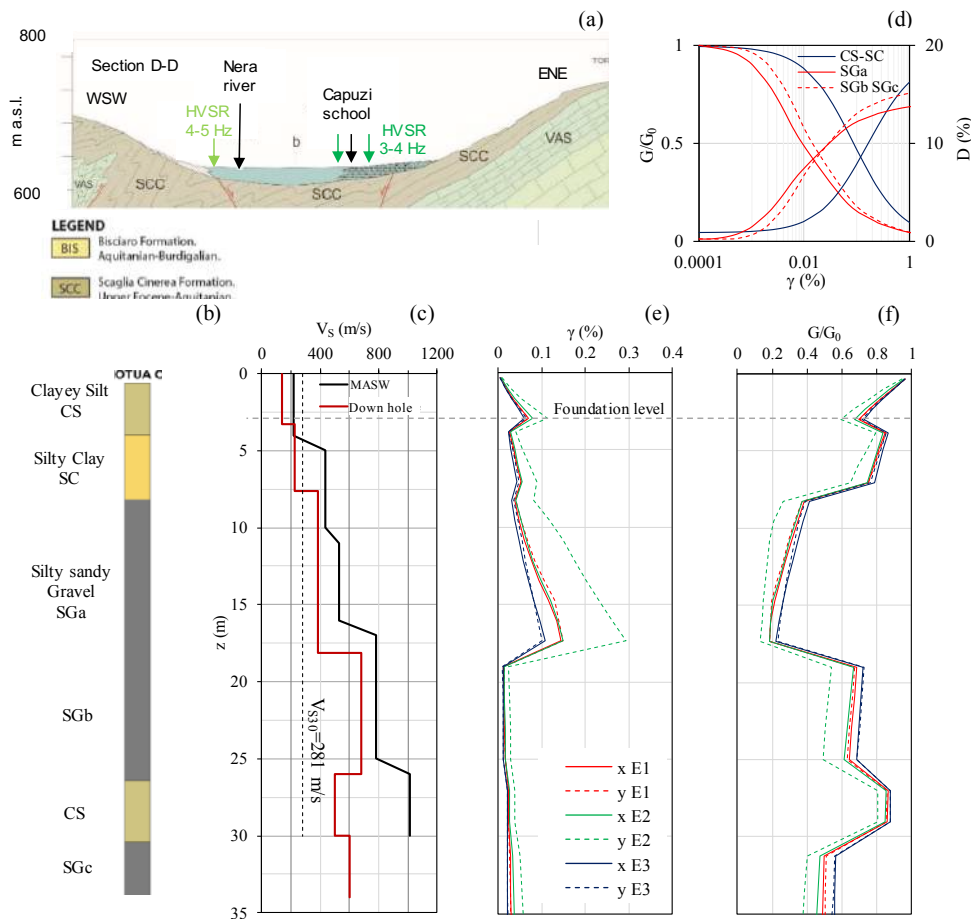


VALIDATION ON MONITORED URM BUILDINGS



The school of P. Capuzi in Visso

- Soil characterization in both linear and nonlinear field by prof. F. Silvestri & F.de Silva from University of Napoli and S.Sica from Univerisity of Sannio



GC = Gravel & Clay
SCC = Scaglia Cinerea, VAS = Scaglia Variegata

	z_{min} (m)	z_{max} (m)	V_s (m/s)	G (MPa)
CS_a	0	3.2	136	38
SC_b	3.2	8	226	104
SG_a	8	18	383	314
SG_b	18	26	683	999
CS_b	26	30	500	510
SG_c	30	40	602	776
Bedrock	40	—	1300	3790

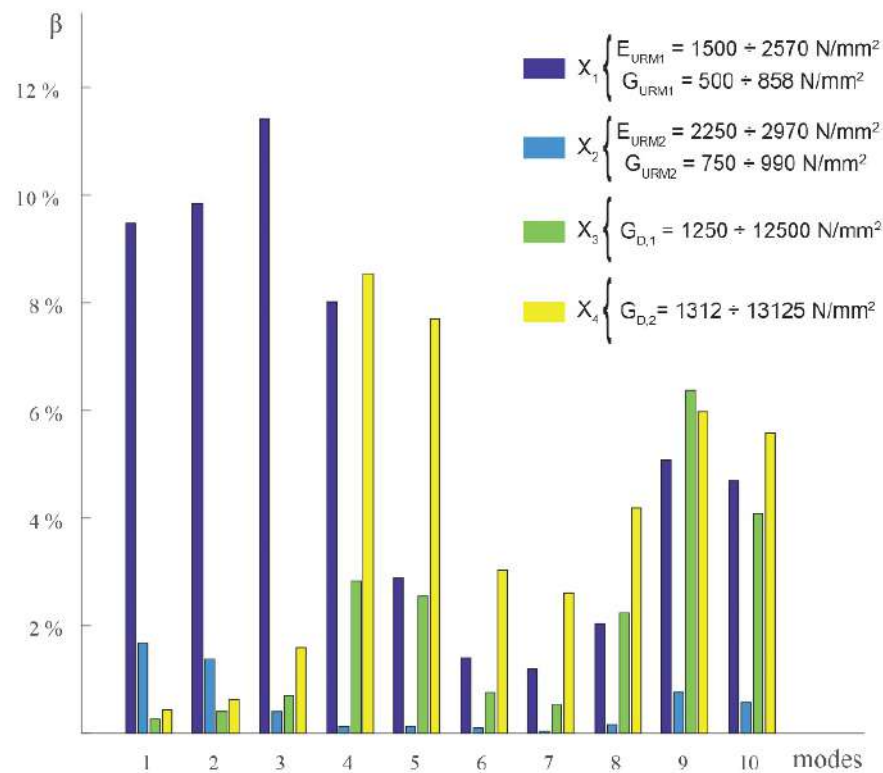
REF: F. de Silva, A. Piro, A. Brunelli, S. Cattari, F. Parisi, S. Sica, F. Silvestri, On the Soil-structure interaction in the seismic response of a monitored masonry school building struck by the 2016-2017 Central Italy earthquake, Proc. of COMPDYN conference 2019. Crete 24-26 June 2019, 2019.

REF: S. Cattari, D. Sivori, A. Brunelli, S. Sica, A. Piro, F. de Silva, F. Parisi, F. Silvestri, Soil-structure interaction effects on the dynamic behaviour of a masonry school damaged by the 2016-2017 Central Italy earthquake sequence, Proceedings of the 7th International Conference on Earthquake Geotechnical Engineering (VII ICEGE). Rome, Italy, June 17-20, 2019



The school of P. Capuzi in Visso

CALIBRATION OF THE MODEL IN ELASTIC FIELD



Random variables :

- elastic and shear moduli of masonry
- shear modulus of the equivalent membrane that simulate the actual stiffness of diaphragms

	URM ₁ (strengthened)	URM ₂	SOL ₁	SOL ₂
E [MPa]	2574 (2970)	2701	/	/
G [MPa]	858 (991)	901	12500	26300
τ_0 [MPa]	0.096 (0.111)	0.114	/	/
f_m [MPa]	4.94 (5.7)	4.8	/	/

τ_0 : diagonal shear strength of masonry; f_m : Compressive strength of masonry

Epistemic uncertainties:

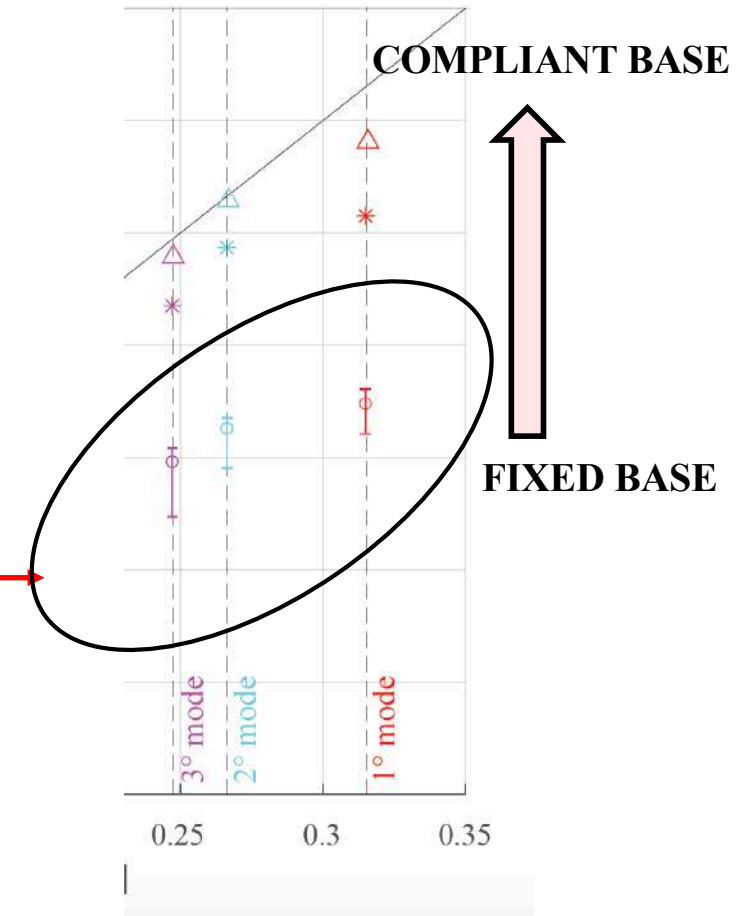
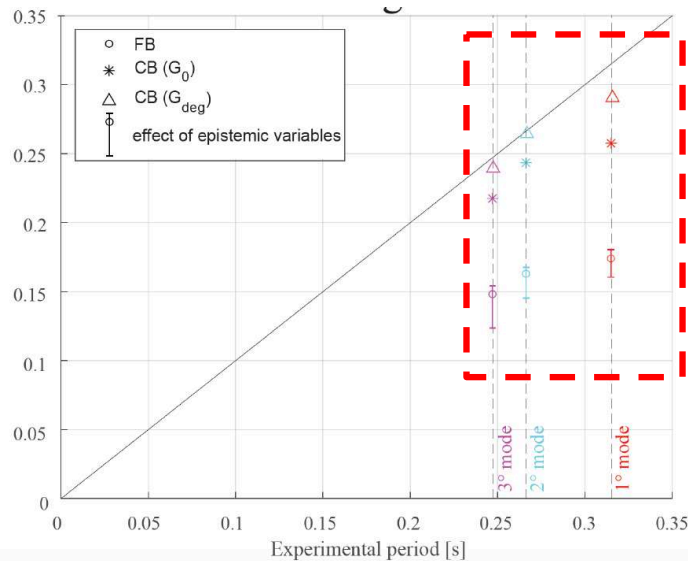
- Actual height of foundation system
- flange effect (coupling effectiveness between orthogonal walls)
- roof modelling
- stiffness of r.c. tie beams

+ Role of soil on the structural response

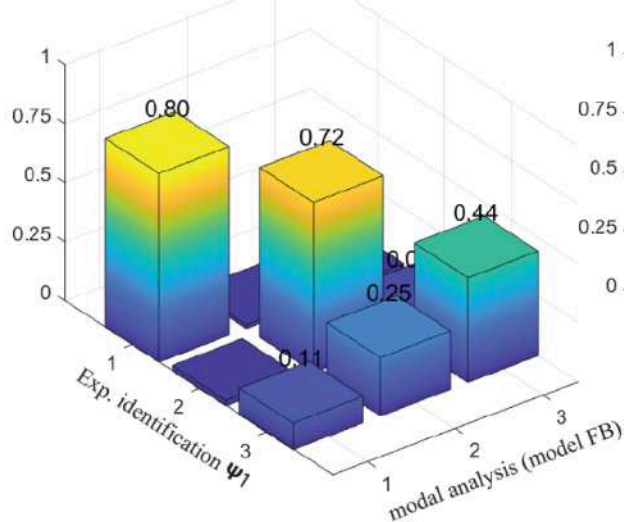


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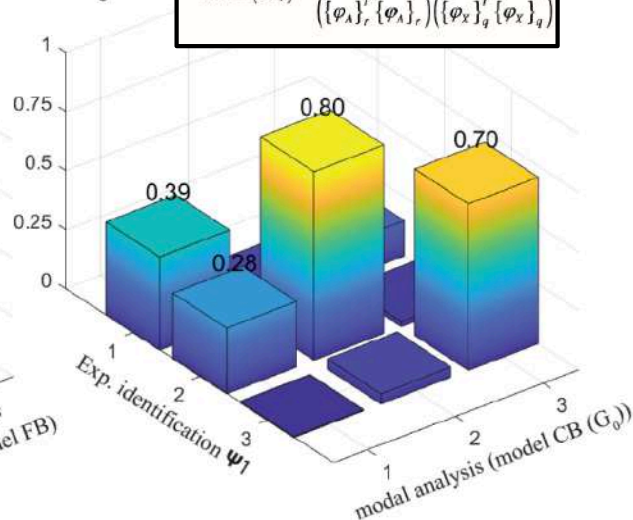
THE MODEL IN ELASTIC FIELD



FB (Fixed estimate)



CB (G_0)



$$MAC(r, q) = \frac{|\{\varphi_A\}_r^T \{\varphi_A\}_q|^2}{(\{\varphi_A\}_r^T \{\varphi_A\}_r)(\{\varphi_A\}_q^T \{\varphi_A\}_q)}$$

	1° mode	2° mode	3° mode
	T [s]	T [s]	T [s]
Ψ_2	0.315	0.267	0.247



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VALIDATION OF THE MODEL IN NON LINEAR FIELD

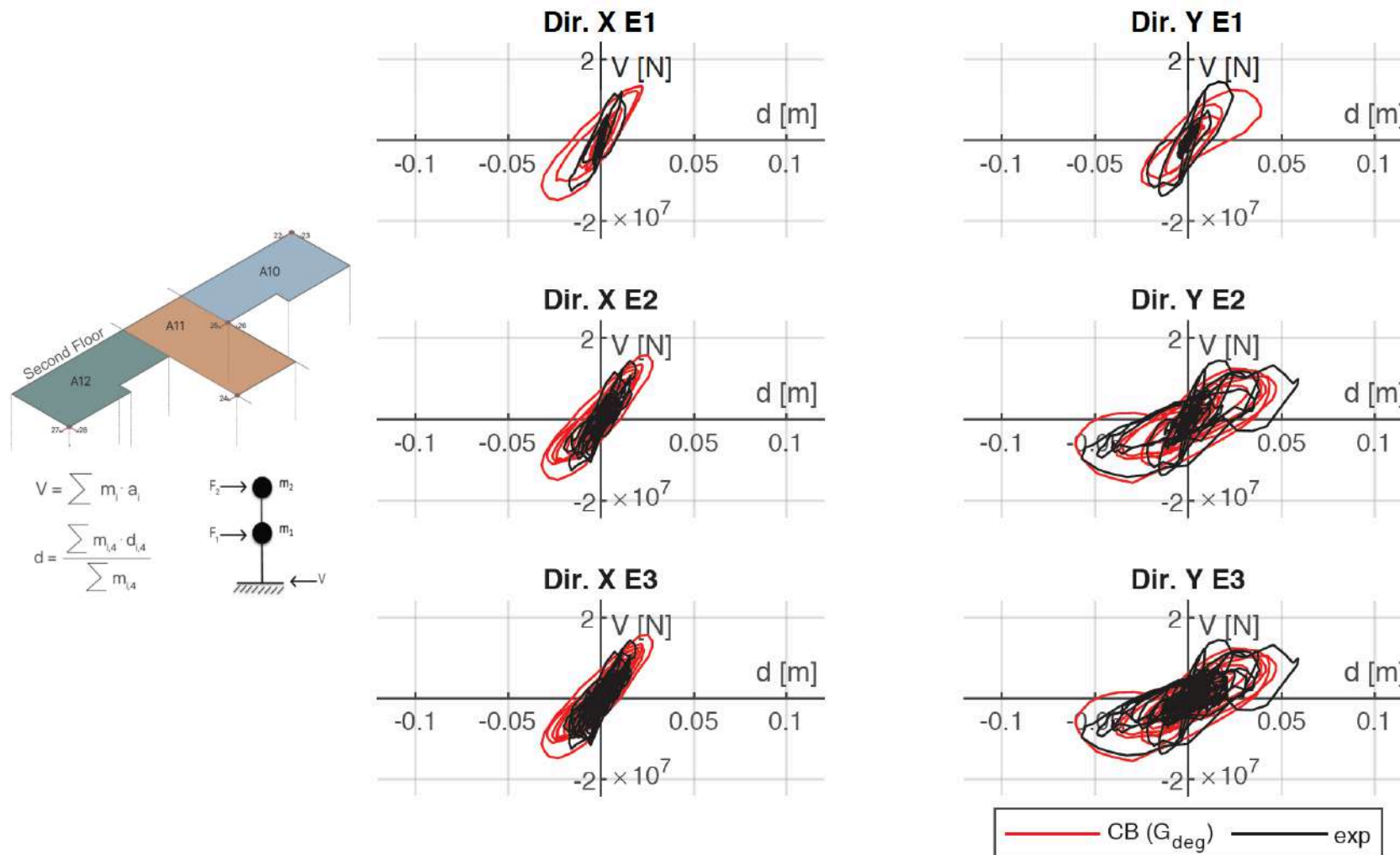
Pier/Spandrel	SHEAR (S)				FLEXURAL (F)			
	Backbone curve		Hysteretic response		Backbone curve		Hysteretic response	
	$\theta_{i,S}$ [%]	$\beta_{E,i}$ [%]	c_1	0.8/0.2	$\theta_{i,F}$ [%]	$\beta_{E,i}$ [%]	c_1	0.9/0
DL3	0.45/(*)	0.6/0.7	c_2	0.8/0	0.48/0.35	1	c_2	0.8/
DL4	0.70/1.50	0.2/0.7	c_3	0/0.3	0.8/1.50	0.85/0.70	c_3	0.6/0
DL5	2.23/2.00	0/0			2.72/2.00	0/0	c_4	0.5/0

(*) in case of spandrels, θ_3 has been defined starting from the value of drift corresponding to the yielding point of the element and assuming then a ductility equal to 4, similarly to what suggested in Beyer et al., 2014.

**ACCORDING TO EXPERIMENTAL DATA & REFERENCE
VALUE OF LITERATURE !!**

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VALIDATION IN NON LINEAR FIELD - INERTIAL FORCES ACTIVATED



Brunelli et al. (2020) NUMERICAL SIMULATION OF THE SEISMIC RESPONSE OF A MONITORED MASONRY SCHOOL BUILDING STRUCK BY THE 2016-2017 CENTRAL ITALY EARTHQUAKE INVESTIGATING THE ROLE OF THE SOIL-STRUCTURE INTERACTION, BULLETIN OF EARTHQUAKE ENGINEERING, TO BE SUBMITTED.

VALIDATION ON MONITORED URM BUILDINGS

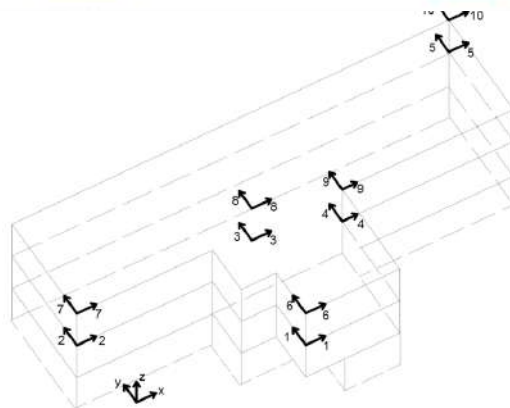


The school of P. Capuzi in Visso

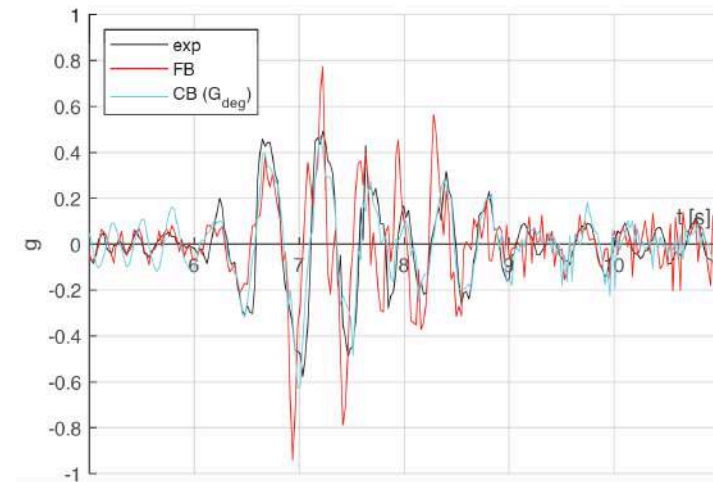
THE MODEL IN NON LINEAR FIELD – SIMULATED ACCELEROGRAMS

	FB									CB (G_{deg})								
	1 st floor				2 nd floor			1 st floor				2 nd floor						
	E1	E2	E3		E1	E2	E3	E1		E2		E3	E1	E2	E3			
1	75%	61%	63%	6	84%	47%	56%	1	92%	65%	62%	6	85%	58%	44%	Dir X		
2	82%	67%	55%	7	84%	79%	65%	2	83%	89%	81%	7	83%	88%	79%			
3	89%	84%	76%	8	86%	82%	73%	3	85%	92%	88%	8	82%	88%	85%			
4	85%	68%	70%	9	83%	82%	76%	4	86%	78%	87%	9	82%	86%	84%			
5	69%	66%	57%	10	66%	63%	58%	5	71%	76%	71%	10	66%	70%	70%			
1	64%	50%	21%	6	62%	45%	21%	1	80%	76%	36%	6	75%	68%	56%	Dir Y		
2	30%	28%	18%	7	37%	31%	18%	2	49%	67%	50%	7	49%	58%	53%			
3	78%	75%	48%	8	79%	71%	53%	3	88%	86%	70%	8	89%	79%	74%			
4	79%	76%	43%	9	84%	66%	43%	4	90%	86%	65%	9	88%	75%	81%			
5	77%	62%	33%	10	78%	65%	34%	5	81%	75%	58%	10	79%	73%	57%			

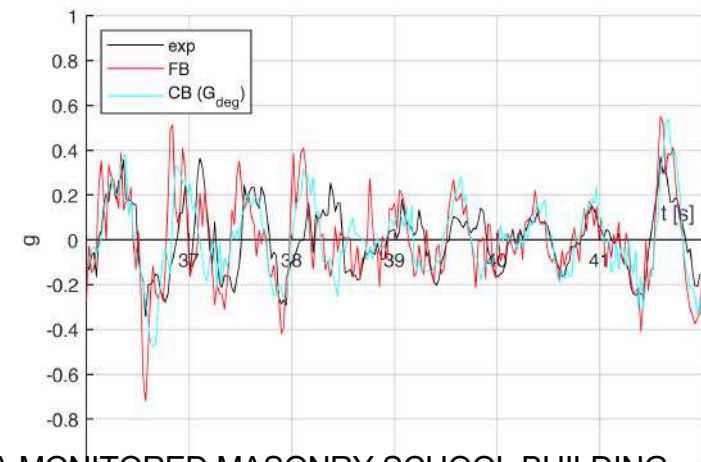
■ CoV $\geq 70\%$
■ $40\% \leq \text{CoV} < 70\%$
■ CoV $< 40\%$



Dir. X E1 Sensor 1



Dir. X E2 Sensor 1

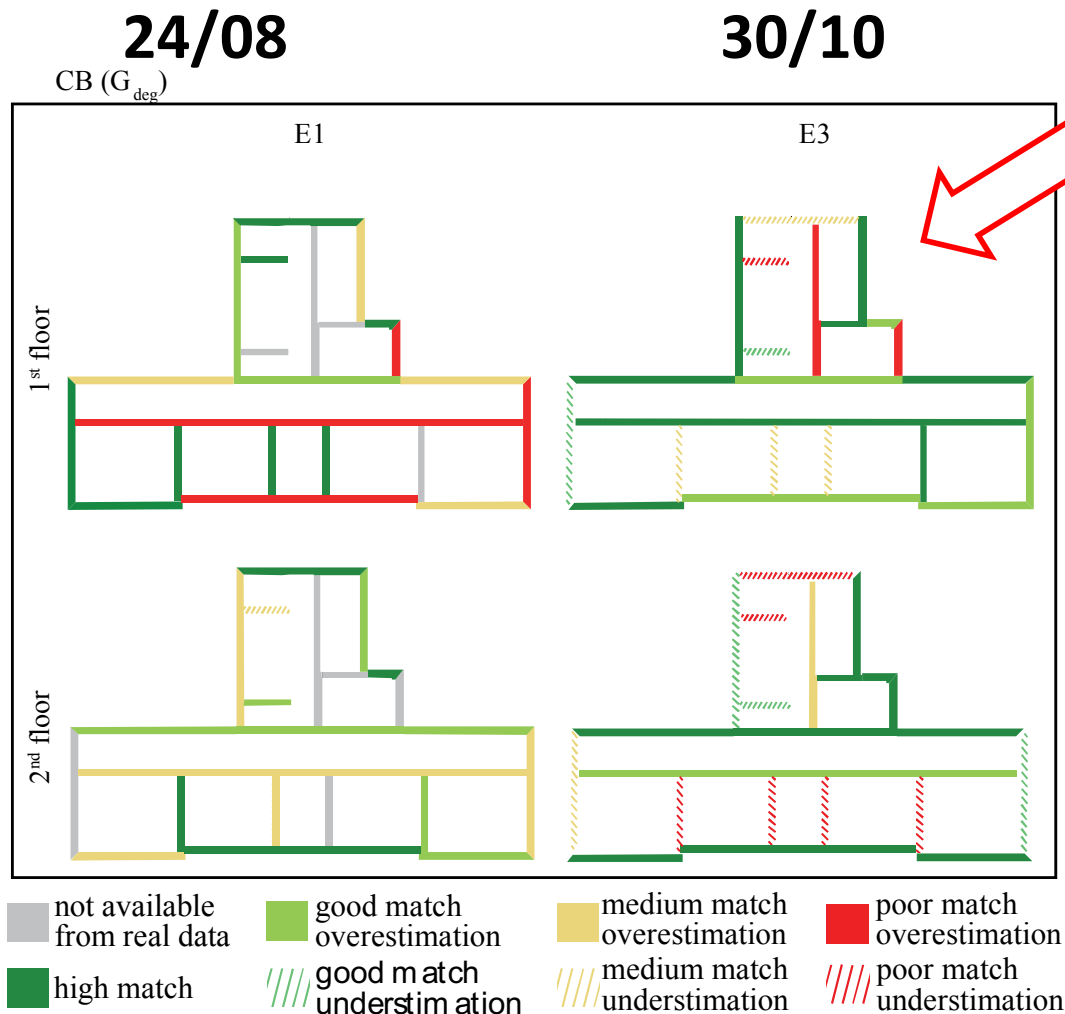


Brunelli et al. (2020) NUMERICAL SIMULATION OF THE SEISMIC RESPONSE OF A MONITORED MASONRY SCHOOL BUILDING STRUCK BY THE 2016-2017 CENTRAL ITALY EARTHQUAKE INVESTIGATING THE ROLE OF THE SOIL-STRUCTURE INTERACTION, BULLETIN OF EARTHQUAKE ENGINEERING, TO BE SUBMITTED.

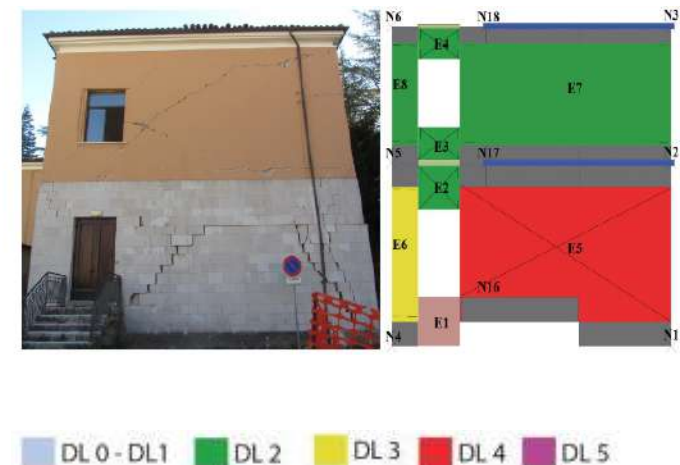
VALIDATION ON MONITORED URM BUILDINGS



The school of P. Capuzi in Visso THE MODEL IN NON LINEAR FIELD



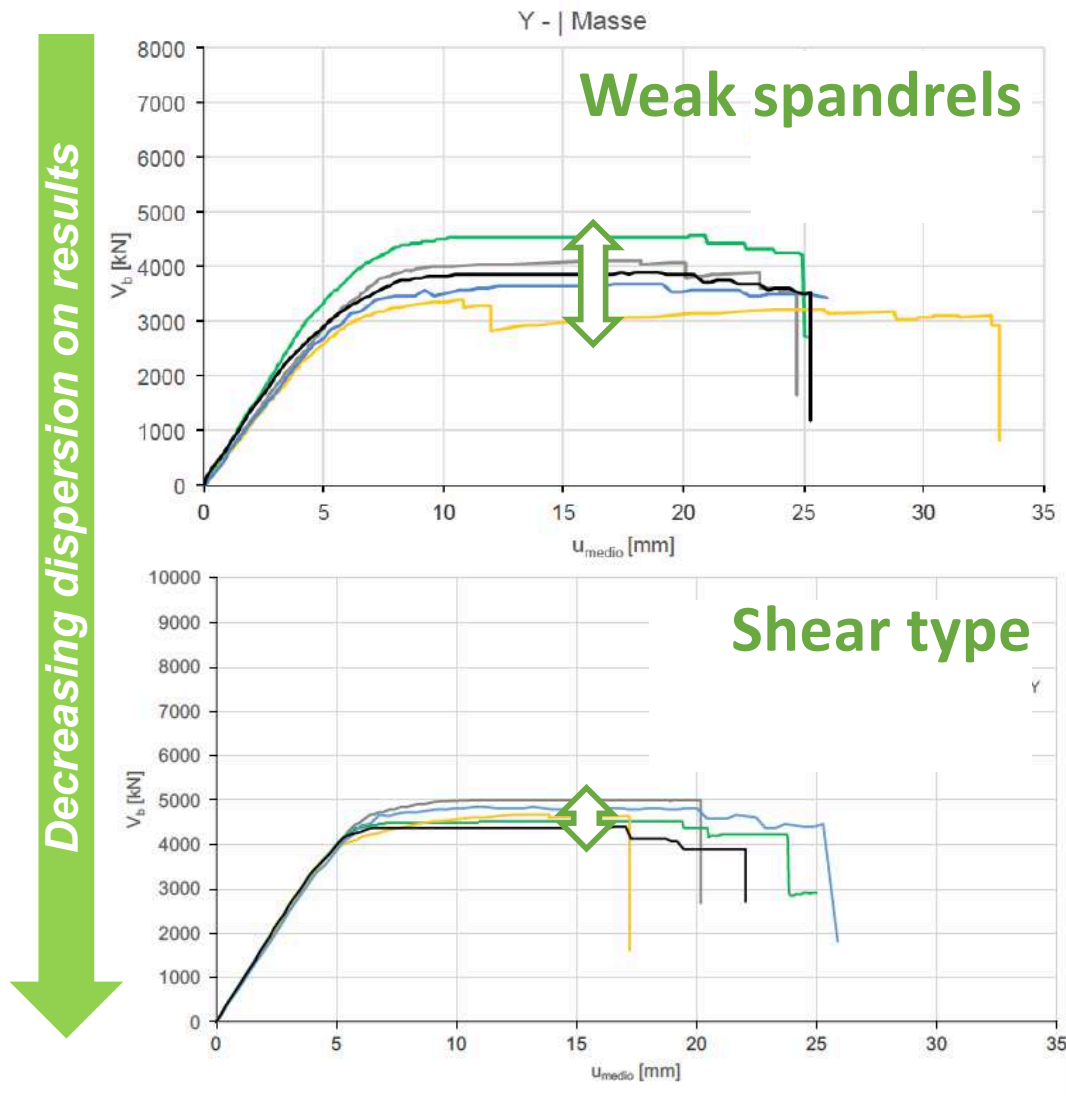
After E3 – 30/10



Brunelli et al. (2020) NUMERICAL SIMULATION OF THE SEISMIC RESPONSE OF A MONITORED MASONRY SCHOOL BUILDING STRUCK BY THE 2016-2017 CENTRAL ITALY EARTHQUAKE INVESTIGATING THE ROLE OF THE SOIL-STRUCTURE INTERACTION, BULLETIN OF EARTHQUAKE ENGINEERING, TO BE SUBMITTED.

...WHAT ABOUT THE RELIABILITY OF BLIND PREDICTION ?

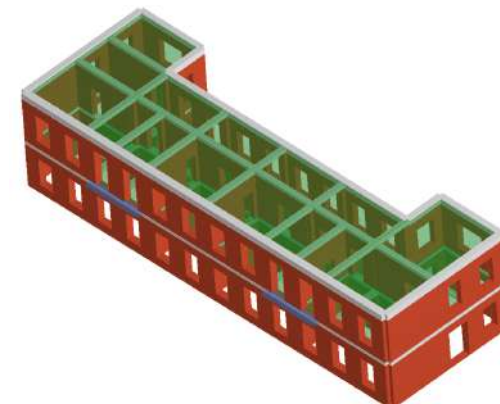
Task 10.3 of ReLUIS project 2019: Numerical **Models Reliability** through **Benchmark Structures**:
Pizzoli case-study



URM Benchmark Workgroup

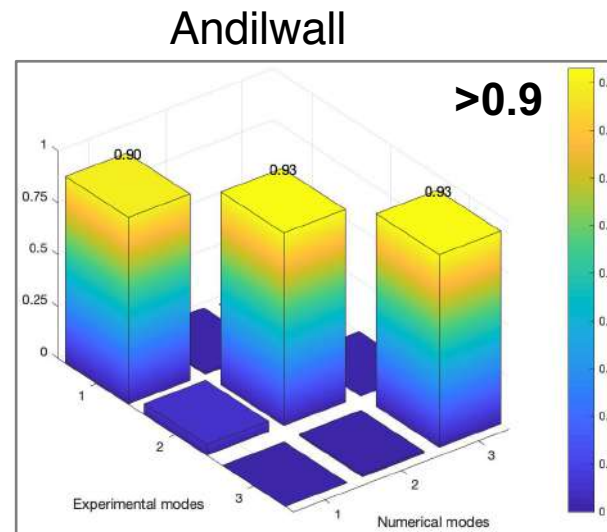
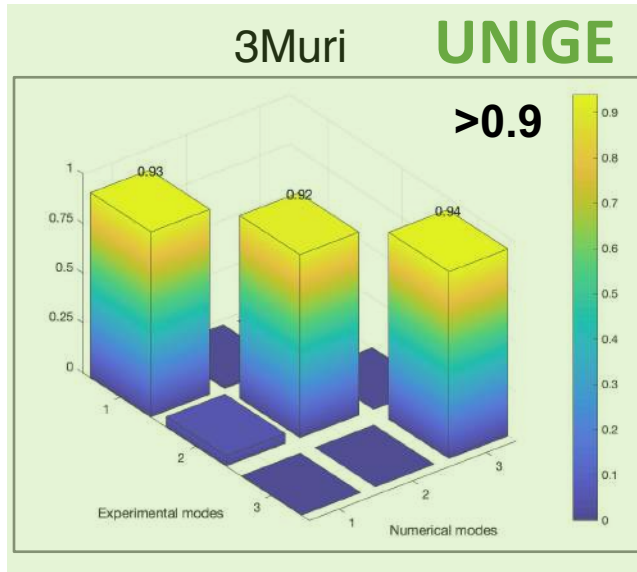


- **Config. C: strong spandrels – spandrels coupled to r.c. ring beam**



...WHAT ABOUT THE RELIABILITY OF BLIND PREDICTION ?

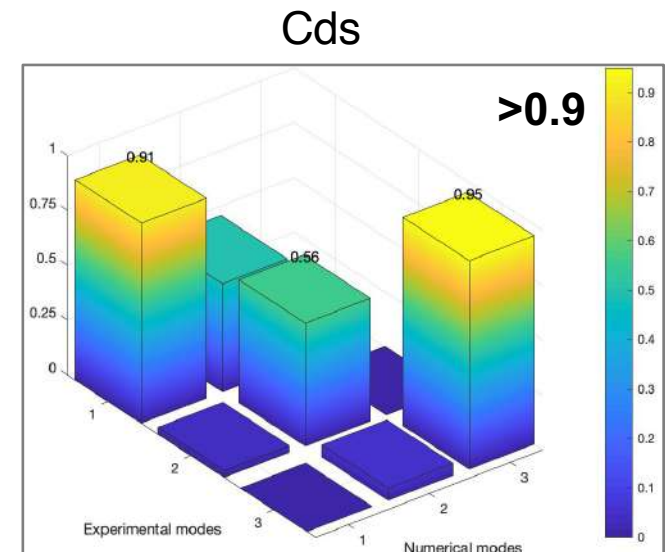
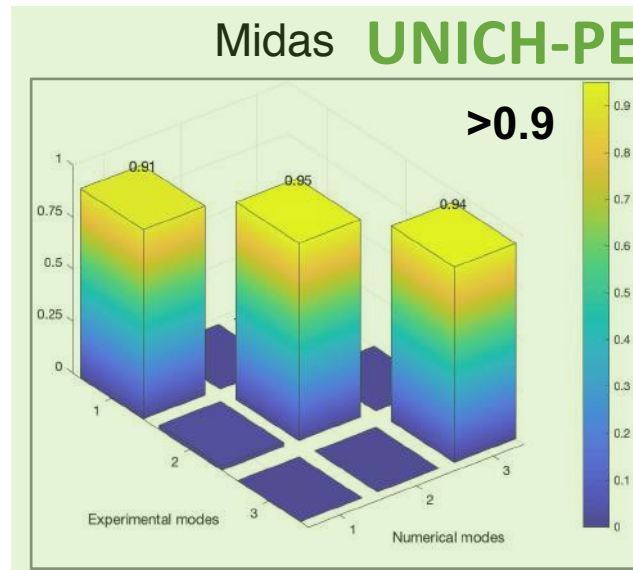
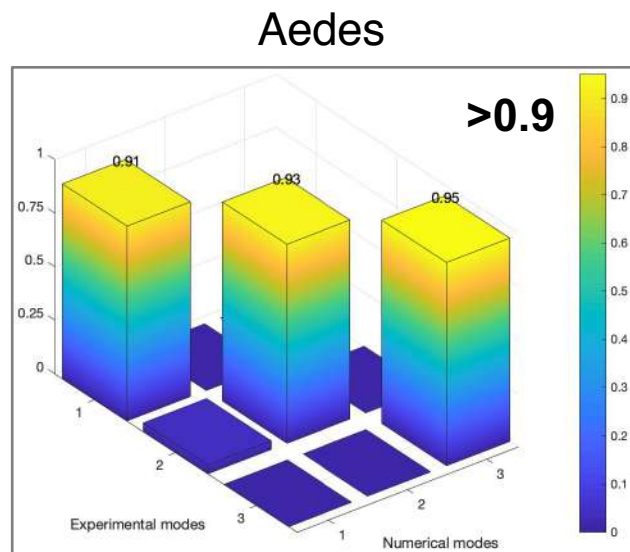
Equivalent frame models



Parameters adopted for the “**blind prediction**” by the **BENCHMARK WORKGROUP**

E= 2262 MPa
G=754 MPa

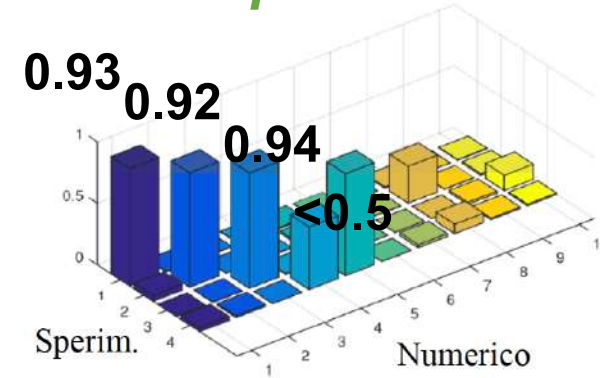
Uncracked Values for stone masonry proposed by NTC 2008 (mean values plus meliorative coefficients)



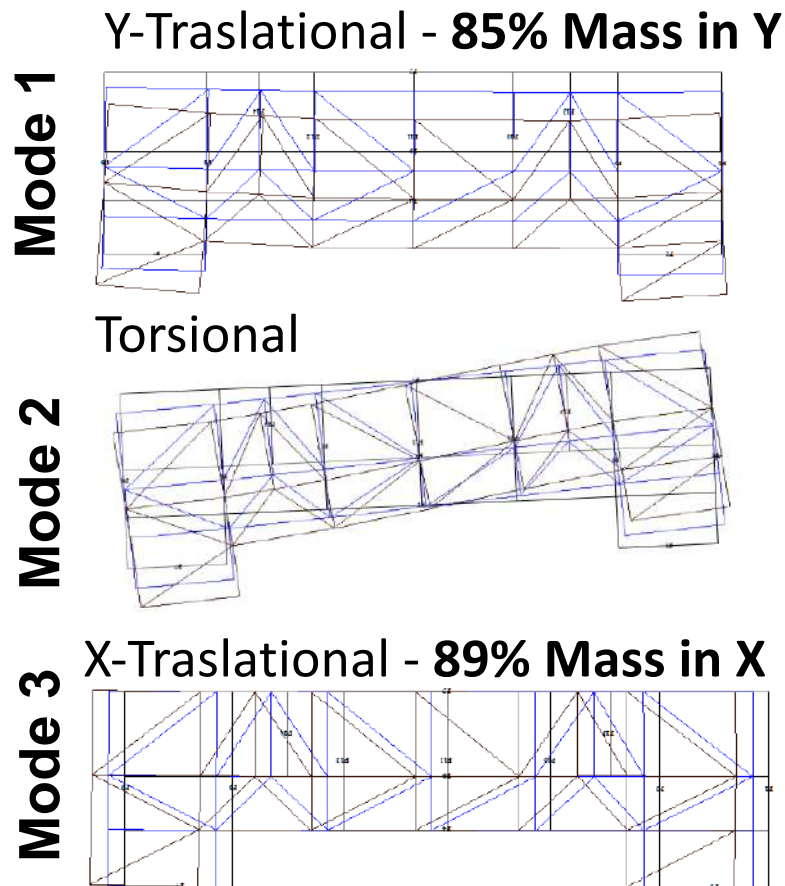
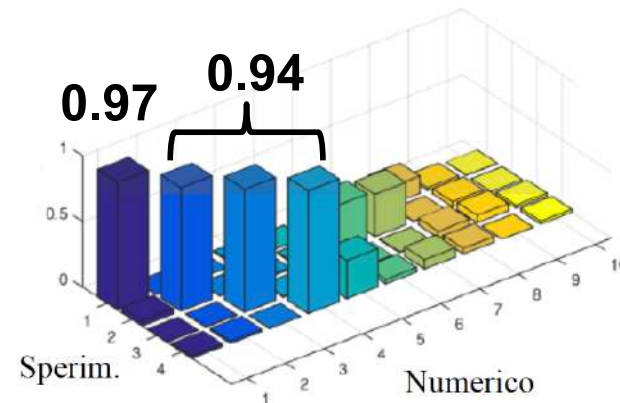
...WHAT ABOUT THE RELIABILITY OF BLIND PREDICTION ?

Parameters	<i>Blind Prediction</i>	UNIGE RU	UNICH-PE RU
E [Mpa]	2262	2488	2550
G [Mpa]	754	829	840

Blind prediction



Using cracked stiffness for rc slabs



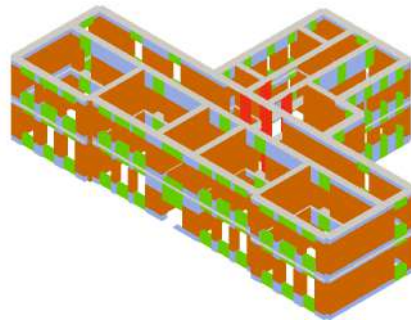
...WHAT ABOUT THE RELIABILITY OF BLIND PREDICTION ?



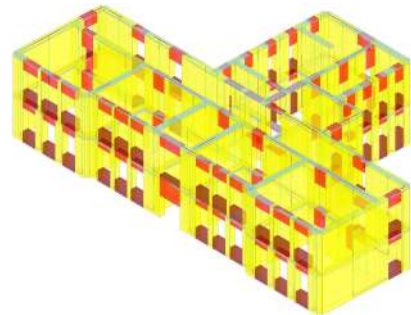
Equivalent frame models (6)

A B C D E F

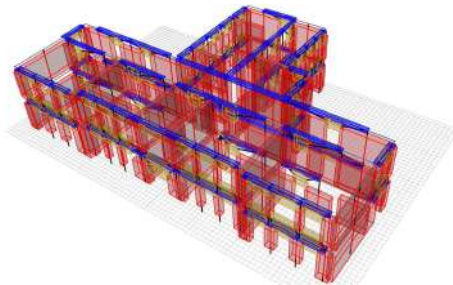
3Muri



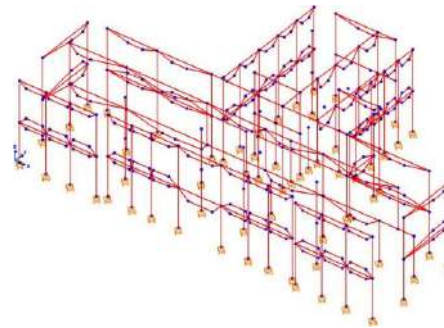
AEDES



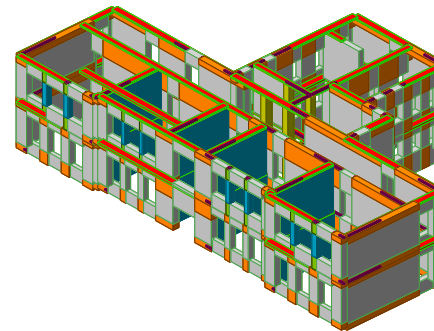
ANDILWALL



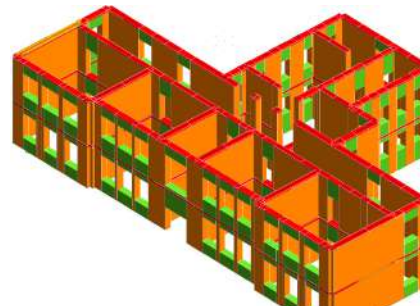
SAP 2000



MIDAS-GEN
(Plasticità concentrata)



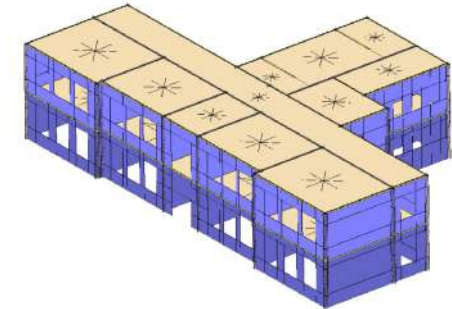
CDS



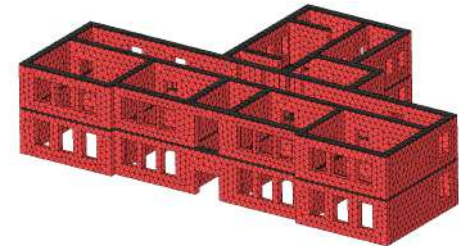
Finite element models (2) & Plane discrete macro models (1)

G H I

3DMacro



ABAQUS

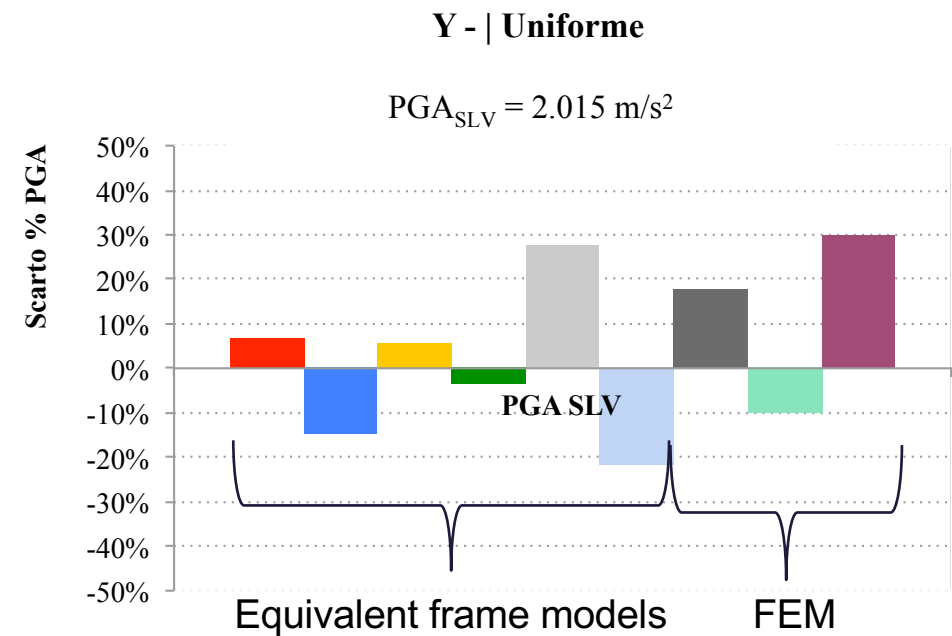
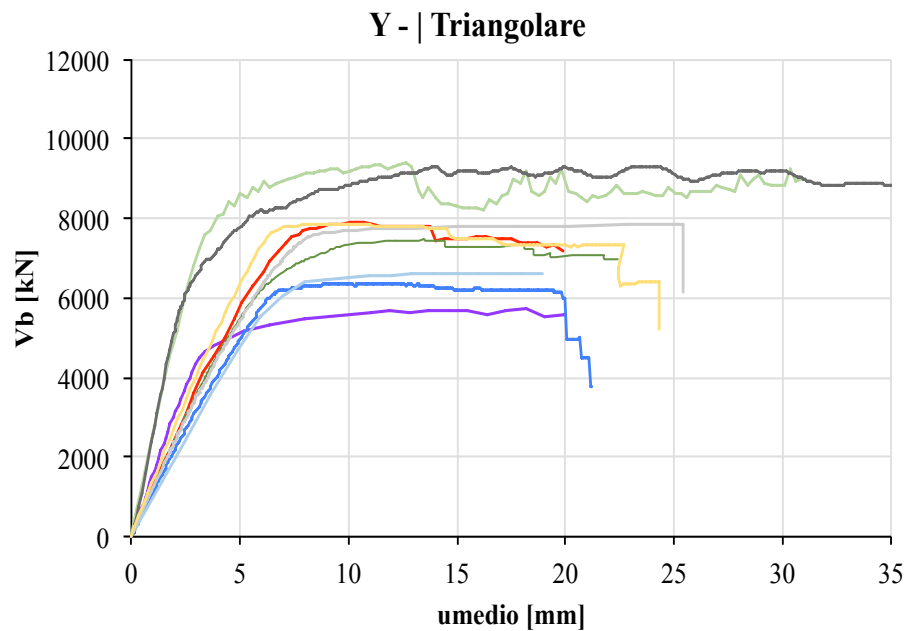


MIDAS-FEA



REF: Cattari et al. 2019, ANIDIS Conference

...WHAT ABOUT THE RELIABILITY OF BLIND PREDICTION ?

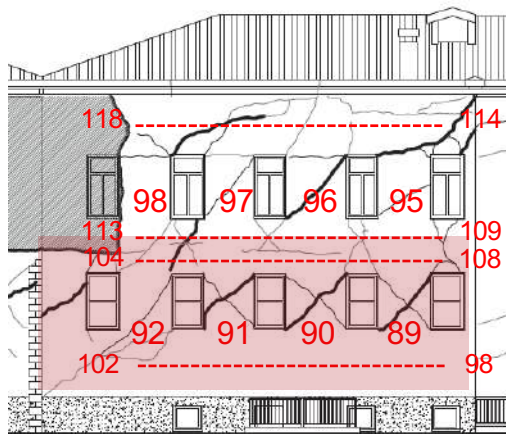


REF: Cattari et al. 2019, Uso dei codici di calcolo per l'analisi sismica nonlineare di edifici in muratura: confronto dei risultati ottenuti con diversi software su un caso studio reale, *ANIDIS Conference*

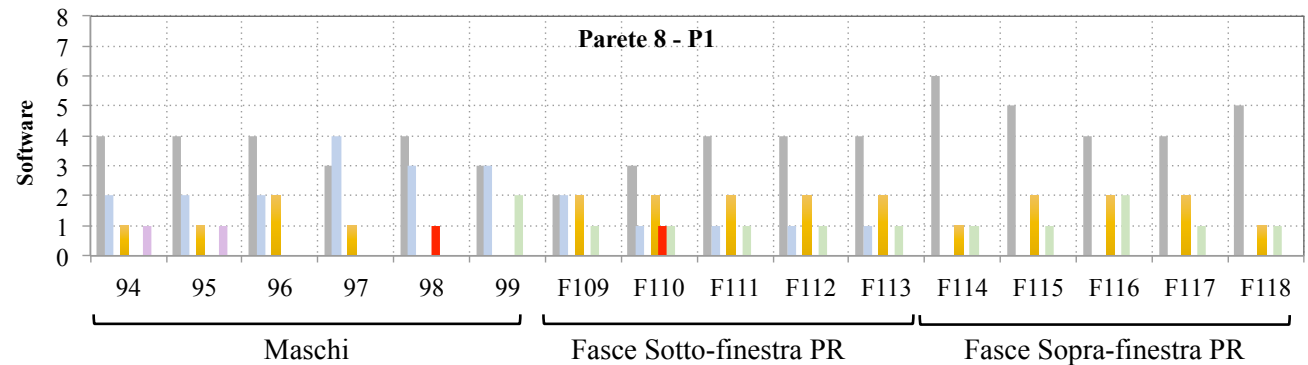
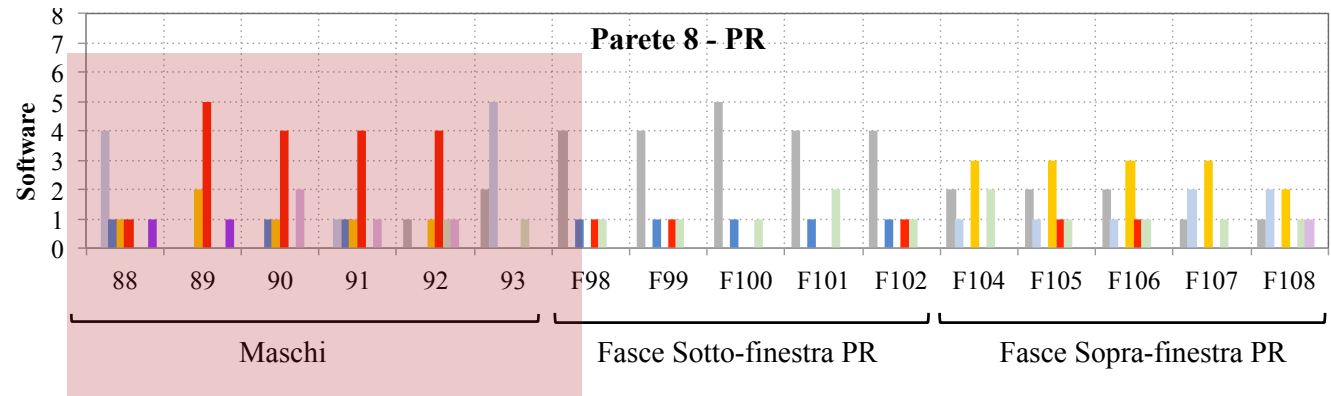
...WHAT ABOUT THE RELIABILITY OF BLIND PREDICTION ?



Y+ | UNIFORM



Figures illustrate the number of software in agreement in predicting the same failure mode at element scale (the colour indicate the prevailing failure mode if flexural or diagonal cracking)



■ E ■ PF-P ■ R(PF)-P ■ V-P ■ R(V)-P ■ T-P ■ MISTA-P ■ MISTA-R

PF= Flexural ; V= diagonal cracking; P= plastic;
R=attainment of the ultimate drift

REF: Cattari et al. 2019, ANIDIS Conference



- ❑ IMPORTANCE TO BE AWARE OF THE HYPHOTESSES WHICH THE MODEL ADOPTED IS FOUNDED ON IN ORDER TO ASSESS ITS RELIABILITY WITH RESPECT THE BUILDING EXAMINED
- ❑ CAPABILITY OF EQUIVALENT FRAME MODEL TO SIMULATE THE NONLINEAR RESPONSE OF URM 3D BUILDINGS WITH A LIMITED COMPUTATIONAL EFFORT (ALSO TO PERFORM NONLINEAR DYNAMIC ANALYSES)
- ❑ USE OF NONLINEAR ANALYSIS AS TOOL TO ASSESS THE PLAN OF INVESTIGATION (BY POINTING OUT THE PARAMETERS THAT MOST AFFECT THE RESPONSE ON WHICH CONCENTRATE TESTS AND SURVEY) AND TO ORIENTATE THE CHOICE OF MOST EFFECTIVE STRENGTHENING INTERVENTIONS

THANK YOU FOR YOUR
KIND ATTENTION!



Serena Cattari

serena.cattari@unige.it



**Università
di Genova**

**DICCA - Department of Civil, Chemical and
Environmental Engineering**